

The Performance and Robustness of Interest-Rate Rules in Models of the Euro Area^{*,†}

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Abstract

In this paper, we examine the performance and robustness of optimised interest-rate rules in four models of the euro area which differ considerably in terms of size, degree of aggregation, relevance of forward-looking behavioural elements and adherence to micro-foundations. Our findings are broadly consistent with results documented for models of the U.S. economy: backward-looking models require relatively more aggressive policies; rules that are optimal in such models tend to perform reasonably well in forward-looking models, while the reverse is not necessarily true; and a robust rule (i.e., one that performs satisfactorily in all models) does not seem to be readily available.

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† The paper summarises the results of a project evaluating the performance of monetary policy rules in a number of small to medium-size models developed by Eurosystem staff which have been regularly used for policy analysis. We would like to thank Keith Küster, Sergio Nicoletti Altimari, Frank Smets, Volker Wieland and Raf Wouters for comments and helpful discussions. The opinions expressed here are those of the authors and do not necessarily reflect views of the European Central Bank or of the Banca d'Italia. Any remaining errors are of course the sole responsibility of the authors.

1 Introduction

The design of robust monetary policy rules has attracted considerable interest in recent macroeconomic research. This interest largely reflects the increased awareness on the part of policy-makers and academics alike that, when evaluating the possible consequences of alternative monetary policies, the existing uncertainties about the structure of the economy need to be given due account. As a result, a large body of research has been oriented towards identifying the characteristics of monetary policy rules that perform ‘reasonably well’ across a range of potentially non-nested and competing macroeconomic models.¹ While this line of research has primarily focused on models of the U.S. economy, no systematic study has yet been conducted for the euro area.²

In an attempt to fill this gap, we concentrate on the euro area and examine the performance and robustness of monetary policy rules using a rather diverse set of macroeconomic models of the euro area economy. Such an examination seems particularly relevant as the single monetary policy of the European Central Bank (ECB) has to focus on the euro area as a whole being a new and still relatively unexplored economic entity and with models of the euro area having been developed only very recently. Specifically, our analysis relies on four models of the euro area economy which have been built by staff of the Eurosystem in recent years. These models differ considerably in terms of size, degree of aggregation, relevance of forward-looking behavioural elements and adherence to micro-foundations. They thus cover a wide range of features that are *a priori* considered to be of high relevance in the context of evaluating the robustness of monetary policy rules.³ One of our main goals is to ascertain which of the various features with respect to which these models differ are of importance when designing rules suitable for model-based evaluations of monetary policy, and which features are, by contrast, arguably less important.

¹For an early claim in this respect see McCallum (1988).

²Earlier studies of the performance of interest-rate rules across alternative models of the U.S. economy are provided in Bryant, Hooper and Mann (1993) and Taylor (1999). More recent studies have been undertaken by Levin, Wieland and Williams (2003) and Levin and Williams (2003). The study of Côté et al. (2002) focuses on models of the Canadian economy.

³Indeed, Svensson (2003) argues that models used to analyse simple monetary policy rules, such as the Taylor rule, were too similar in structure (i.e., of the ‘New-Keynesian’ variety) to constitute a true test of their robustness.

In terms of methodology, our analysis builds on recent work by Levin, Wieland and Williams (1999, 2003) and Levin and Williams (2003) – henceforth referred to as LWW (1999, 2003) and LW (2003), respectively.⁴ This methodology involves implementing simple reaction functions describing the response of the short-term nominal interest rate to inflation and the output gap, either observed or forecast, and then optimising over the respective response coefficients. The performance of these optimised interest-rate rules is then evaluated across alternative, potentially competing models with regard to their ability to stabilise inflation and output around their targets, while avoiding undue fluctuations in the nominal interest rate itself.

Of course, variables other than inflation and the output gap may enter the interest-rate rule, such as the exchange rate or monetary and financial-market indicators. However, the literature tends to suggest that including information variables of this kind in the policy rule yields relatively modest gains in model-based evaluations because they are typically highly correlated with the interest rate itself or closely related with the measures of inflation and the output gap entering the rule (although this result may not hold in sufficiently complex models). Furthermore, simple rules with a feedback to a small set of variables are arguably more robust to model mis-specification and uncertainty than rules based on a larger set of variables, which might over-fit specific model characteristics.

From an institutional viewpoint, the advantage of simple interest-rate rules is clearly their transparency and, thus, the ease with which they may be communicated to and be monitored by the outside world. While it is unlikely that monetary policy-makers will follow their literal execution, such rules may nonetheless be a useful benchmark for assessing the actual conduct of monetary policy. Likewise, from an empirical point of view, simple interest-rate rules seem to match the data well for the United States as well as a number of European countries (see Clarida et al., 1998). More recently, evidence for the euro area as a whole has been provided by Gerdesmeier and Roffia (2003).

⁴There are alternative approaches to analysing the consequences of uncertainty about the structure of the economy (see for example Giannoni, 2002, Giannoni and Woodford, 2002, Hansen and Sargent, 2002, Onatski and Stock, 2002, Onatski and Williams, 2003, and Tetlow and von zur Muehlen, 2001). This co-existence of alternative approaches reflects that there has not yet emerged a consensus on how to address the issue of model uncertainty.

The findings of our analysis are broadly consistent with the results documented for models of the U.S. economy: backward-looking models require relatively more aggressive policies; rules that are optimal in such models tend to perform reasonably well in forward-looking models, while the reverse is not necessarily true; and a robust rule (i.e., one that performs satisfactorily in all models) does not seem to be readily available. In the course of collecting these results, we highlight a number of model features, notably the degree of forward-lookingness, which play a crucial role in shaping the operating characteristics of optimised interest-rate rules. This in turn suggests that future empirical research that aims at casting light on these features may considerably enhance the reliability and usefulness of interest-rate rules for model-based evaluations of monetary policy.

The remainder of this paper is organised as follows. Section 2 outlines the set of euro area models used in our analysis and illustrates the implied differences in inflation and output-gap dynamics in response to a monetary policy shock. Section 3 briefly describes the methodology used for evaluating the performance of interest-rate rules and provides a set of optimised benchmark rules for each of the euro area models under examination. Section 4 evaluates the robustness of these benchmark rules when there is uncertainty about the true structure of the euro area economy, as represented by the co-existence of possibly competing models, while Section 5 identifies the operating characteristics of rules that perform reasonably well at least across subsets of our models. Section 6 reports additional sensitivity analysis and Section 7 concludes.

2 The Models of the Euro Area

To examine the performance of monetary policy rules across a range of potentially competing models of the euro area economy, we utilise a set of four macroeconomic models which differ considerably in terms of variable and country coverage, relevance of forward-looking behavioural elements and adherence to micro-foundations. All models are estimated with aggregate euro area-wide data, except one which separately models the three largest euro area economies. Two of the models are entirely or at least predominantly backward looking,

while forward-looking elements abound in the other two. All models are consistent with basic economic principles, however there is only one in our set of models that is strictly based on the assumption of optimising agents. Hence, the models under examination cover a fairly broad range of different modelling strategies.

In the remainder of this section, we briefly present the four models of the euro area and illustrate the implied differences in inflation and output-gap dynamics in response to a monetary policy shock.

2.1 An Outline of the Euro Area Models

The Coenen-Wieland Model

The Coenen-Wieland (CW) model (see Coenen and Wieland, 2000) is a small-scale model of aggregate supply and aggregate demand which is designed to capture the broad characteristics of inflation and output dynamics in the euro area. Since its development, the model has been mainly used as a laboratory for evaluating the performance of alternative monetary policy strategies.

The supply side of the model incorporates price and wage staggering, with wage setters negotiating long-term nominal wage contracts with reference to past contracts that are still in effect and future contracts that will be negotiated over the life of the current contract. If wage setters expect the output gap to be positive, they adjust the current contract wages upward. Consequently, inflation depends on own leads and lags, excess-demand conditions as well as transitory contract wage shocks, the latter representing ‘cost-push’-type shocks. There are two versions of the supply side which feature distinct types of staggered wage contracts: the nominal wage contracting specification due to Taylor (1980) and the relative real wage contracting specification by Fuhrer and Moore (1995).⁵ The two specifications differ with respect to the degree of inflation persistence that they induce, with Fuhrer-Moore-type contracts giving more weight to past inflation developments. In this paper, the

⁵While the two types of specification represent rules for price and wage-setting that are not explicitly derived from a framework with optimising agents, they need not be necessarily inconsistent with such a framework. More recently, Taylor-type contracts have been analysed within more fully fleshed-out dynamic general equilibrium models (see for example Chari et al., 2000, or King and Wolman, 1999). Fuhrer-Moore-type contracts, however, have typically been criticised for lacking micro-foundations.

version with Taylor-type contracts is used.⁶

A simple aggregate demand relationship relates the output gap, measured as the deviation of actual output from a smooth trend, to several lags of itself, the ex-ante long-term real interest rate and a transitory demand shock. The long-term real rate is determined jointly by a term-structure relationship and the Fisher equation. The short-term nominal interest rate is the instrument of monetary policy and changes in the latter affect aggregate demand through the impact on the ex ante long-term real interest rate.

The Smets-Wouters Model

The Smets-Wouters (SW) model (see Smets and Wouters, 2003) is an extended version of the standard New-Keynesian DSGE closed-economy model with sticky prices and wages. The model is estimated by Bayesian techniques using seven euro area macroeconomic time series: real GDP, consumption, investment, employment, real wages, inflation and the nominal short-term interest rate.

The model features three types of economic agents: households, firms and the monetary-policy authority. Households maximise a utility function with two arguments (goods and leisure) over an infinite life horizon. Consumption appears in the utility function relative to a time-varying external habit variable. Labour is differentiated over households, so that there is some monopoly power over wages, which results in an explicit wage equation and allows for the introduction of sticky nominal wages à la Calvo (1983). Households also rent capital services to firms and decide how much capital to accumulate given certain capital adjustment costs. As the rental price of capital goes up, the capital stock can be used more intensively according to some cost schedule. Firms produce differentiated goods, decide on labour and capital inputs, and set prices, again à la Calvo. The Calvo model in both wage and price setting is augmented by the assumption that those prices and wages that can not be freely set are partially indexed to past inflation. Prices are therefore set as a function

⁶See Coenen (2003) for an evaluation of the performance of monetary policy rules across the two variants with Taylor and Fuhrer-Moore-type contracts, respectively. This paper shows that a cautious monetary policy-maker is well-advised to design interest-rate policies under the assumption that the inflation process is characterised by a high degree of persistence – as induced by Fuhrer-Moore-type contracts – when he is faced with uncertainty about the prevailing degree of inflation persistence.

of current and expected real marginal cost, but are also influenced by past inflation. Real marginal cost depends on wages and the rental rate of capital. The short-term nominal interest rate is the instrument of monetary policy.⁷

The stochastic behaviour of the model is driven by ten exogenous shocks: five shocks arising from technology and preferences, three cost-push shocks and two monetary-policy shocks. The first set of shocks is assumed to follow first-order autoregressive processes, whereas the second set is assumed to follow serially uncorrelated processes. Consistent with the DSGE set up, potential output is defined as the level of output that would prevail under flexible prices and wages in the absence of cost-push shocks.

The Area-Wide Model

The Area-Wide Model (AWM, see Fagan et al., 2001) is a medium-size structural macroeconomic model that treats the euro area as a single economy.⁸ It has a long-run neo-classical equilibrium with a vertical Phillips curve but with some short-run frictions in price and wage setting and factor demands. Consequently, activity is demand-determined in the short run but supply-determined in the long run. In the latter, employment converges to a level consistent with the exogenously given level of equilibrium unemployment and factor demands are consistent with the solution of the firms' profit-maximisation problem. Stock-flow adjustments are accounted for by, for example, the inclusion of a wealth term in consumption. At present, the treatment of expectations in the model is quite limited. With the exception of the exchange rate (determined by uncovered interest parity) and the long-term nominal interest rate (modelled by a term-structure relationship), the model embodies backward-looking expectations.

As to the mechanisms through which monetary policy affects the economy, aggregate demand in the AWM is presently influenced only by short-term real interest rates. Long-term nominal rates determine government debt payments but do not explicitly enter investment

⁷Extending the study of Coenen (2003), Angeloni et al. (2003) utilise the SW model to analyse the design of monetary policy when the monetary policy-maker is uncertain about the degree of nominal as well as real persistence. The results of this analysis confirm the conclusions of the earlier study.

⁸For an examination of optimal monetary policy in the context of the AWM alone see Dieppe et al. (2004).

decisions. The expectations channel in principle allows monetary policy to influence inflation via wage and price-setting behaviour. In addition to these influences, further effects enter through the exchange rate. Apart from an indirect effect of exchange rates on domestic demand, there is also a direct exchange-rate effect on consumer price inflation through the price for imported goods. The output gap is defined as the ratio of actual output to potential output, which is based on an aggregate Cobb-Douglas production function with constant returns to scale and Hicks-neutral technical progress. For this, the trend total factor productivity has been estimated within-sample by applying the Hodrick-Prescott filter to the Solow residual derived from the production function.

A Dis-aggregate Euro Area Model

The Dis-aggregate Euro Area Model (DEAM) used in Angelini et al. (2002) and Monteforte and Siviero (2002) is a multi-country version of the simple backward-looking two-equation model in Rudebusch and Svensson (1999). It consists of an aggregate supply equation and an aggregate demand equation for each of the three largest economies in the euro area; i.e., Germany, France and Italy, which jointly account for over 70 per cent of euro area GDP. The first equation, interpretable as a Phillips curve, determines inflation in each country as a function of lagged inflation and the output gap, as well as inflation ‘imported’ from the other two countries. The sum of the coefficients on lagged and imported inflation is constrained to equal unity (a restriction accepted by the data), so that a long-run vertical Phillips curve exists for all countries. The second equation represents an IS curve and relates the output gap of each country, modelled as the deviation of actual output from a smooth trend, to its own lagged values, the short-term real interest rate, as well as the output gaps in the other two countries (a design meant to capture the trade linkages among euro area economies). Euro area inflation and the aggregate output gap are determined via identities as weighted averages of the corresponding individual country variables. Finally, the area-wide short-term nominal interest rate is the instrument of monetary policy.

As the model allows for simultaneous cross-country linkages, it was estimated with 3SLS using data on inflation, output and nominal interest rates. Not all cross-country terms are

significant in all equations, resulting in a clear causal pattern, with the German economy affecting the other two comparatively more, and with the Italian economy being essentially recursive. Furthermore, the estimation results indicate that there exists a significant degree of heterogeneity among the three economies included in the model.⁹ Accordingly, the results in Angelini et al. (2002) suggest that monetary policy effectiveness may be considerably enhanced if country-specific information is used.

2.2 Differences in Monetary Policy Transmission

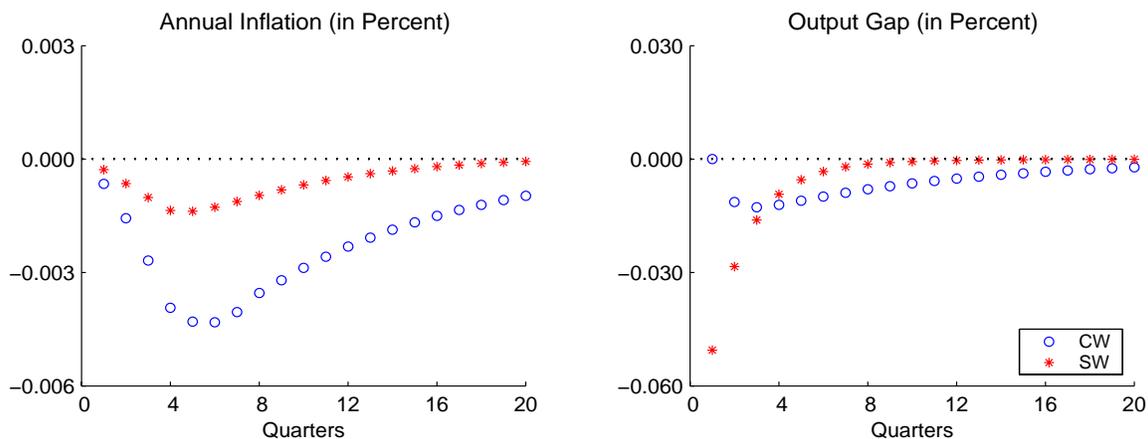
Figure 1 provides a comparison of the effects of an unexpected one-quarter tightening of monetary policy by 100 basis points in the four different models of the euro area, with the monetary policy-maker following the interest-rate rule proposed by Taylor (1993) thereafter. Panel A of the figure depicts the dynamic responses of annual inflation and the output gap for the largely forward-looking models (CW and SW), while panel B shows the responses for the predominantly backward-looking models (AWM and DEAM).

Qualitatively, the tightening of policy has the same consequences in the four models. As the short-term nominal interest rate rises unexpectedly, demand falls short of potential and inflation falls below the monetary policy-maker's target, with the dynamic adjustment being drawn out lastingly. Quantitatively, however, the responses exhibit some noticeable differences. Most importantly, the disinflation effect is considerably larger and more persistent in the backward-looking models with the timing of the peak effect on inflation noticeably delayed relative to that on the output gap. By contrast, in the forward-looking models the timing of the peak effect on inflation is much closer to that on the output gap with the reversion to base of both inflation and the output gap being relatively more rapid and smoother. Differences in the responses of the output gap, notably in the initial periods, largely reflect differences in the employed output-gap concepts. Overall, this suggests that the degree of forward-lookingness is of utmost relevance for explaining the differences in inflation and output-gap dynamics across models.

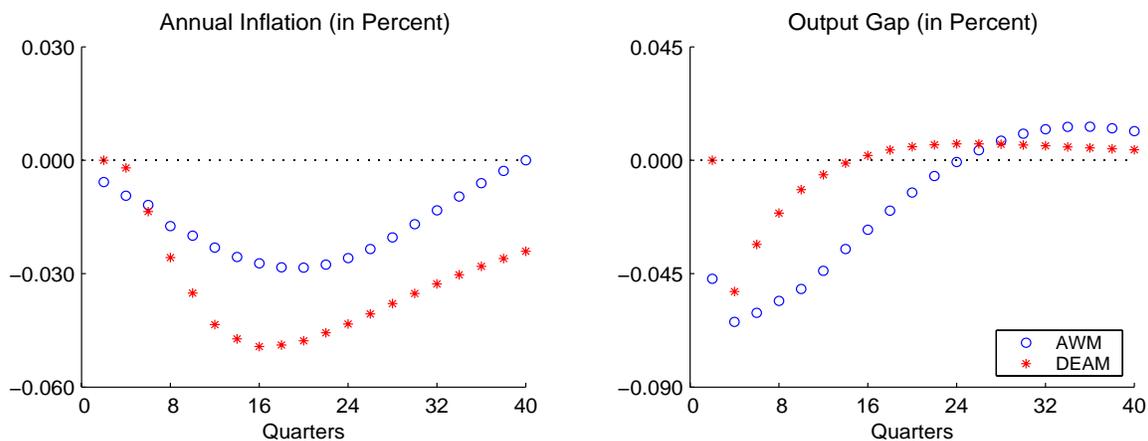
⁹Angelini et al. (2002) also report estimates of an aggregate companion of the DEAM (referred to as Aggregate Euro Area Model, AEAM), consisting of just two equations. Both statistical and economic criteria indicate that the DEAM is to be preferred to the AEAM.

Figure 1: Responses to an Interest-Rate Shock (100 Basis Points) under Taylor's Rule

A. The Forward-Looking Euro Area Models



B. The Backward-Looking Euro Area Models



Based on the documented patterns of the dynamic responses to the monetary policy shock under Taylor's rule, we summarise that a given interest-rate rule may perform quite differently in terms of inflation and output-gap stabilisation, depending on the characteristics of the particular euro area model used. Hence, it is evident why monetary policy-makers

should be concerned about the design of the interest-rate rule to be used in model-based analyses.

3 Evaluating the Performance of Interest-Rate Rules

We now proceed to describe the methodology which we will use to evaluate the stabilisation performance of alternative monetary policies across our set of models of the euro area economy. Our starting point is an evaluation of simple interest-rate rules which respond to outcomes or forecasts of annual inflation and the output gap and allow for inertia due to dependence on the lagged short-term nominal interest rate.

3.1 The Methodology

Following the approach in LWW (2003), we consider a three-parameter family of simple interest-rate rules,

$$i_t = \rho i_{t-1} + (1 - \rho)(r^* + E_t[\tilde{\pi}_{t+\theta}]) + \alpha E_t[\tilde{\pi}_{t+\theta} - \pi^*] + \beta E_t[y_{t+\kappa}],$$

where i_t denotes the short-term nominal interest rate, r^* is the equilibrium real interest rate, $\tilde{\pi}_t = p_t - p_{t-4}$ is the annual inflation rate, π^* denotes the monetary policy-maker's inflation target, and y_t is the output gap.¹⁰ Under rational expectations, the operator $E_t[\cdot]$ indicates the model-consistent forecast of a particular variable, using information available in period t .¹¹ The integer parameters θ and κ denote the length of the forecast horizons for inflation and the output gap, respectively. This specification accommodates forecast-based rules (with forecast horizons $\theta, \kappa > 0$) as well as outcome-based rules ($\theta = \kappa = 0$) and simplifies to the one proposed by Taylor (1993) if $\theta = \kappa = 0$ and $\rho = 0$.¹²

For fixed inflation and output-gap forecast horizons θ and κ , the above family of interest-rate rules is defined by the response coefficients ρ , α and β . The coefficients α and β

¹⁰Even in the case where the multi-country model DEAM is used, both inflation and the output gap are to be interpreted as area-wide variables, reflecting the assumption that the policy-maker is concerned with area-wide developments.

¹¹We employ the AIM algorithm of Anderson and Moore (1985), which uses the Blanchard and Kahn (1980) method for solving linear rational expectations models, to compute model-consistent expectations.

¹²In the special case with $\rho = 1$, the rule represents a first-difference rule, a class of rules which LWW (2003) advocate as being robust when examining the performance of simple interest-rate rules in a set of different U.S. macroeconomic models. Orphanides and Williams (2002) emphasise that first-difference rules are also robust to mis-perceptions about the equilibrium real interest rate r^* .

represent the policy-maker’s short-term reaction to inflation in deviation from target and the output gap, respectively, while ρ determines the inertia of the interest-rate response, commonly interpreted as the desired degree of policy ‘smoothing’. The latter plays a particularly important role for model-based evaluations of interest-rate rules. In particular, the degree to which the optimal policy in any given model embodies smoothing tends to depend largely on the expectation formation mechanism embedded in that model. Typically, if expectations are backward looking, values of ρ at or above unity can perform poorly since they may engender un-dampened oscillations in the model economy due to instrument instability (see, e.g., Rudebusch and Svensson, 1999, and Batini and Nelson, 2001). By contrast, models with largely forward-looking expectations, notably small optimising New-Keynesian models, tend to favour a comparatively high degree of smoothing because the inertial adjustment of the short-term interest rate enables the policy-maker to steer expectations and thereby to stabilise the economy more effectively.

In our evaluation of the stabilisation performance of variants of the above family of interest-rate rules, we assume that the monetary policy-maker has a standard loss function equal to the weighted sum of the unconditional variances of inflation, the output gap and changes in the short-term nominal interest rate,

$$\mathcal{L} = \text{Var}[\pi_t] + \lambda \text{Var}[y_t] + \mu \text{Var}[\Delta i_t].$$

Here, inflation is measured by the annualised one-quarter inflation rate, $\pi_t = 4(p_t - p_{t-1})$. The weight $\lambda \geq 0$ refers to the policy-maker’s preference for reducing output variability relative to inflation variability, and the weight $\mu \geq 0$ on the variability of changes in the short-term nominal interest rate, $\Delta i_t = i_t - i_{t-1}$, reflects a desire to avoid undue fluctuations in the nominal interest rate itself.¹³ Establishing this loss function is consistent with the assumption that the policy-maker aims at stabilising inflation around the inflation target π^* and actual output around potential, with the concern regarding excessive interest-rate

¹³For an explicit derivation of the policy-maker’s loss function \mathcal{L} from quadratic intertemporal preferences the reader is referred to Rudebusch and Svensson (1999). In Svensson’s terminology, the case of $\lambda = \mu = 0$ corresponds to ‘strict’ inflation targeting, while ‘flexible’ inflation targeting is characterised by $\lambda, \mu > 0$ (see Svensson, 1999).

variability typically justified by financial stability considerations.¹⁴

For fixed inflation and output-gap forecast horizons θ and κ , the three-parameter family of interest-rate rules defined above is optimised by minimising the policy-maker's loss function \mathcal{L} with respect to the coefficients ρ , α and β .¹⁵ In this context, we repeatedly need to compute the unconditional variances of the models' endogenous variables for a given interest-rate rule. In preparation for these computations, we first identify the series of historical shocks that would be consistent with the alternative models under rational expectations. Based on the covariance matrix of the historical shocks, it is then possible to calculate the unconditional covariance matrix of the endogenous variables for any given interest-rate rule by applying standard methods to the reduced-form solution of the model including that rule.¹⁶

In the subsequent analysis, we will consider four alternative values for the relative weight on output-gap variability, namely $\lambda = 0, 1/3, 1$ and 3 . Regarding the weight on the variability of interest-rate changes, we will concentrate the analysis on a fixed value of $\mu = 0.10$. We shall briefly discuss additional results for a lower weight of $\mu = 0.01$ in the sensitivity analysis towards the end of paper. There, we will also report on results for interest-rate rules which only allow for a response to lagged inflation and the lagged output gap; i.e., with $\theta = \kappa = -1$. Such rules have been proposed as a proxy for actual policy-making in 'real time' (see McCallum, 1988).

3.2 The Performance of Optimised Benchmark Rules

As benchmarks for evaluating the performance of simple interest-rate rules across our set of models, we focus on two types of rules: outcome-based rules with $\theta = \kappa = 0$, and forecast-based rules which relate the interest rate to the one-year-ahead forecast of inflation and the

¹⁴It is recognised that it would be beneficial to use a welfare criterion derived as an approximation of the representative agent's utility function (see for example Rotemberg and Woodford, 1997). The weights in this approximate welfare criterion would be functions of the parameters of the structural model itself. However, to the extent that the models used in this paper, with the exception of the SW model, are lacking micro-foundations, a well-defined welfare criterion does not exist.

¹⁵For the DEAM the loss function is obtained by weighing the loss functions associated with the individual country blocks, reflecting the assumption that the policy-maker is concerned with area-wide developments.

¹⁶The exception is the SW model, for which the covariance matrix of shocks is estimated jointly with the model's structural parameters.

Table 1: The Stabilisation Performance of Optimised Interest-Rate Rules

A. The Forward-Looking Euro Area Models											
θ	κ	λ	CW				SW				
			ρ	α	β	$\% \Delta \mathcal{L}$	ρ	α	β	$\% \Delta \mathcal{L}$	
0	0	0	0.97	0.81	0.10	2	1.03	0.81	0.08	3	
		1/3	0.81	0.49	0.86	5	1.00	0.64	1.53	8	
		1	0.79	0.30	1.55	4	0.99	0.43	3.05	6	
		3	0.77	0.23	2.50	3	0.92	0.11	5.87	5	
4	0	0	1.59	4.36	-0.25	5	1.96	6.59	-0.05	6	
		1/3	0.83	1.18	0.84	6	1.01	1.19	1.50	9	
		1	0.79	0.76	1.55	4	1.00	0.79	2.99	7	
		3	0.77	0.59	2.49	3	0.99	0.53	5.64	5	
B. The Backward-Looking Euro Area Models											
θ	κ	λ	AWM				DEAM				
			ρ	α	β	$\% \Delta \mathcal{L}$	ρ	α	β	$\% \Delta \mathcal{L}$	
0	0	0	0.44	1.14	1.13	26	0.31	5.52	3.65	54	
		1/3	0.39	0.93	2.37	20	0.28	5.78	3.89	53	
		1	0.44	0.65	3.69	18	0.25	5.71	4.26	51	
		3	0.50	0.40	5.79	15	0.19	5.59	5.01	47	
4	0	0	0.47	2.22	0.55	15	0.55	3.99	0.56	20	
		1/3	0.37	2.47	1.67	13	0.51	4.06	0.74	21	
		1	0.39	2.49	3.00	12	0.46	4.18	1.05	23	
		3	0.42	2.38	5.12	11	0.36	4.39	1.75	24	

Notes: For each choice of the inflation and output-gap forecast horizons (θ and κ), for each preference parameter (λ) and for each model, this table indicates the optimised interest-rate response coefficients (ρ , α and β) and the percentage-point change in the policy-maker's loss function ($\% \Delta \mathcal{L}$) compared with the loss under the fully optimal policy.

contemporaneous output gap with $\theta = 4$ and $\kappa = 0$.

Table 1 reports the optimised response coefficients of the two types of rules for alternative values of the preference parameter λ , together with an indication of their stabilisation performance. The latter is measured in relative terms as the percentage-point change in the policy-maker’s loss function, $\% \Delta \mathcal{L}$, compared with the loss under the fully optimal policy.^{17,18} Panel A in Table 1 indicates the results for the largely forward-looking models (CW and SW), while panel B shows the results for the predominantly backward-looking models (AWM and DEAM).

We start with the results for the forward-looking models in panel A, and observe that, regardless of the policy-maker’s preference for output stabilisation, the optimised rules are characterised by a substantial degree of interest-rate smoothing, as captured by the high coefficient on the lagged interest rate, ρ . Interestingly, with a low weight on output stabilisation and, in particular, with the inflation forecast horizon extending one year into the future, the magnitude of ρ tends to exceed unity, notably for the SW model. This feature is commonly referred to as ‘super-inertia’ in the interest rate. Not surprisingly, as the weight on output stabilisation increases, the coefficient on the output gap, β , rises while the coefficient on inflation, α , falls. As to the stabilisation performance of the optimised interest-rate rules, we observe that the performance of monetary policy deteriorates fairly little when the policy-maker follows a relatively simple optimised interest-rate rule rather than the fully optimal policy. The value of the policy-maker’s loss function never rises by more than 9 percentage points. We also observe that there is no discernible stabilisation gain from following forecast-based as opposed to outcome-based rules.

Turning to the backward-looking models in panel B, a number of differences are noteworthy. First, the optimised interest-rate rules embody only a mild degree of smoothing, with ρ varying between 0.4 and 0.5 for the AWM and between 0.2 and 0.6 for the DEAM. This discrepancy largely reflects the fact that expectations, notably those determining long-term interest rates, do not play a dominant role in either model. Thus, there is no scope for

¹⁷For the CW and SW models, as well as the AWM, the fully optimal policy corresponds to the optimal policy under commitment. See Finan and Tetlow (1999) for details on computing the optimal policy under commitment for large rational expectations models using AIM.

¹⁸Details regarding the level of the loss function, \mathcal{L} , and measures of the unconditional variability of the individual target variables can be found in Table A of the appendix.

increasing the effectiveness of monetary policy by an inertial adjustment of the short-term rate. Second, the optimised response coefficients α and β are typically quite a bit larger than for the forward-looking models, in particular for the DEAM. This mirrors the fact that, in backward-looking models, inflation and the output gap are much harder to stabilise and that, as a result, the policy-maker has to respond more aggressively to any signs of rising inflation and cumulating output gaps. Third, the stabilisation performance of simple interest-rate rules deteriorates quite substantially when compared with the outcomes under the fully optimal policy, albeit less dramatically for the AWM. In the extreme case when the policy-maker does not attach any weight to output stabilisation, the loss under the optimised outcome-based rule exceeds the loss associated with the fully optimal policy by more than 50 percentage points for the DEAM, while the loss increases by about 25 percentage points for the AWM. In the case of the AWM, the comparatively poor performance of simple optimised rules is likely due to the model's relatively high degree of dis-aggregation and its rather complex lag structure (see Finan and Tetlow, 1999, for a similar observation based on the Federal Reserve Board's FRB/U.S. model). Similarly, the DEAM departs from the rest of the models to the extent that it is the only model in which the three largest euro area economies are modelled separately. Finally, contrary to the results for the forward-looking models, there are substantial gains from using forecast-based rather than outcome-based rules, with the maximum difference in the reported percentage-point changes in the loss function equal to 11 for the AWM and 34 for the DEAM. We attribute these improvements in performance to the information-encompassing nature of forecast-based rules, with the inflation forecast incorporating information about incipient risks to future inflation arising from a possibly larger set of underlying determinants (see Batini and Haldane, 1999) and the transmission lag of monetary policy (see Batini and Nelson, 2001).

4 Evaluating the Robustness of Interest-Rate Rules

In the previous section, we implicitly assumed that the policy-maker knows the 'true' model of the euro area economy when optimising variants of the three-parameter family of interest-

rate rules for any given model. While the optimised rules typically succeeded in stabilising inflation and output satisfactorily for that given model, we now proceed to analyse to which extent the optimised rules are robust to model uncertainty, in the sense of performing also reasonably well across the other, possibly competing models of the euro area.

4.1 The Performance of Optimised Rules across Models

Table 2 summarises our findings regarding the stabilisation performance of the optimised benchmark rules documented in Table 1 above across our set of models. Here, performance is measured by the percentage-point change in the policy-maker's loss function, $\% \Delta \mathcal{L}$, when the rule optimised for any particular model i is evaluated in the possibly competing model $j \neq i$, relative to the loss under the fully optimal policy for model j . Panel A in Table 2 reports the findings for the rules optimised for the forward-looking models, while panel B documents those for the backward-looking ones.

Starting with the rules optimised for the forward-looking models in panel A, we observe that rules which are optimised for the CW model also perform satisfactorily when evaluated in the SW model, and vice versa. For example, with $\theta = \kappa = 0$ and $\lambda = 1/3$, implementing the CW-based rule in the SW model leads to an increase in the loss function of about 15 percentage points, relative to the loss associated with the fully optimal policy for the SW model. When compared to the performance of the interest-rate rule optimised for the SW model itself (see Table 1 above), the loss increases by about 7 percentage points. Similarly, when implementing the SW-based rule in the CW model the increase in the loss function amounts to 13 and 8 percentage points, depending on the benchmark for comparison. By contrast, when evaluating the CW and SW-based rules in the backward-looking models, the performance of monetary policy tends to deteriorate quite substantially. For the AWM, the loss increases by about 50 percentage points relative to the fully optimal policy when CW-based rules are implemented and by more than 100 percentage points on average for SW-based rules. The deterioration is found to be particularly dramatic if the policy-maker puts zero weight on output stabilisation since the CW and SW-based rules do not succeed in stabilising the AWM any longer. Finally, when evaluated in the DEAM, the performance

Table 2: The Robustness of Optimised Interest-Rate Rules in Models of the Euro Area

A. Rules Optimised for the Forward-Looking Euro Area Models								
θ	κ	λ	CW rule evaluated in			SW rule evaluated in		
			SW	AWM	DEAM	CW	AWM	DEAM
0	0	0	6	∞	∞	3	∞	∞
		1/3	15	56	684	13	202	419
		1	18	54	8228	23	110	969
		3	25	58	∞	38	85	∞
4	0	0	9	∞	∞	6	∞	∞
		1/3	15	52	155	14	232	∞
		1	17	45	318	23	122	1106
		3	25	51	763	43	72	∞

B. Rules Optimised for the Backward-Looking Euro Area Models								
θ	κ	λ	AWM rule evaluated in			DEAM rule evaluated in		
			CW	SW	DEAM	CW	SW	AWM
0	0	0	20	36	1157	87	56	94
		1/3	11	24	4859	58	39	43
		1	14	23	∞	53	55	24
		3	ME	23	∞	52	97	17
4	0	0	25	40	205	40	37	27
		1/3	13	30	238	16	35	30
		1	13	31	261	20	64	41
		3	16	31	303	29	120	56

Notes: For each choice of the inflation and output-gap forecast horizons (θ and κ), for each preference parameter (λ) and for each model, this table indicates the percentage-point change in the policy-maker's loss function ($\%\Delta\mathcal{L}$) when the rule optimised for model i is evaluated in model $j \neq i$, compared with the loss under the fully optimal policy for model j . The notation "ME" indicates that the implemented rule yields multiple equilibria; the notation " ∞ " indicates that the implemented rule results in instability.

of CW and SW-based rules is even worse, generating even higher increases in relative losses and resulting in instability more often.

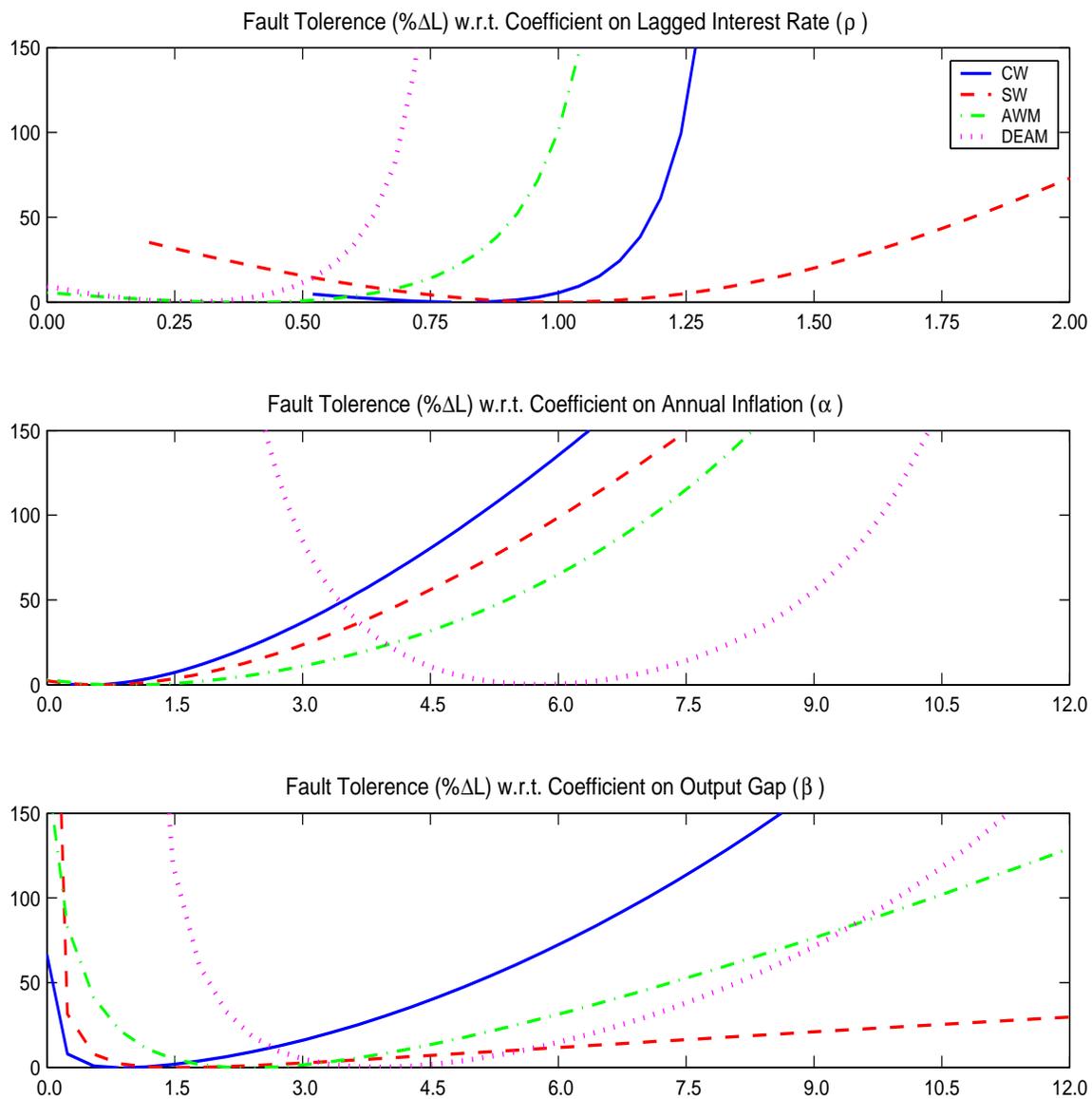
Turning to the rules optimised for the backward-looking models in panel B, we observe that the AWM-based rules typically result in reasonable stabilisation outcomes when evaluated in the CW or the SW model. The exception is the outcome-based rule for $\lambda = 3$ which yields multiple equilibria when implemented in the CW model. By contrast, the AWM-based rules do not perform satisfactorily in the DEAM and may occasionally even generate instability. Finally, the DEAM-based rules result in a substantial deterioration in the performance of monetary policy when evaluated in any of the three other models, although the deterioration exceeds 100 percentage points only in exceptional cases. Interestingly, for forecast-based rules the deterioration is found to be somewhat more benign.

Based on these results, we conclude that simple interest-rate rules that are designed for the largely forward-looking euro area models tend to perform poorly in predominantly backward-looking ones, while the reverse is not necessarily true. The fault-tolerance analysis undertaken in the next section will help cast some further light on the reasons underlying these findings.

4.2 A Fault-Tolerance Analysis of Optimised Rules

Fault-tolerance analysis of optimised interest-rate rules, as proposed by LW (2003), is deemed to provide useful insights into the reasons that underlie our earlier findings. Fault-tolerance analysis is a concept borrowed from engineering and involves, in the present context, appraising the increase in the loss function that results when a single parameter of an optimised interest-rate rule is varied, holding the other parameters constant at their optimised values. A highly *fault tolerant* model is one for which the parameters of the rule may vary over a relatively broad range of values without resulting in a large deterioration of its performance. By contrast, an intolerant model would be a model whose performance deteriorates dramatically as soon as one deviates only modestly from some optimised parameter value (i.e., the loss function exhibits strong curvature with respect to sub-optimal variations in some parameter). Clearly, if one is dealing with a set of relatively tolerant models, there is a fair chance to find a robust policy rule. If all models are intolerant, then a robust rule may not exist.

Figure 2: Fault-Tolerance Analysis of Outcome-Based Interest-Rate Rules



Notes: For $\lambda = 1/3$ and for each model, the figure indicates the percentage-point change in the policy-maker's loss function ($\% \Delta \mathcal{L}$) under the optimised outcome-based interest-rate rule ($\theta = \kappa = 0$) as a single parameter (ρ , α or β) of the optimised rule is varied, holding the other two parameters fixed at their respective optimised values.

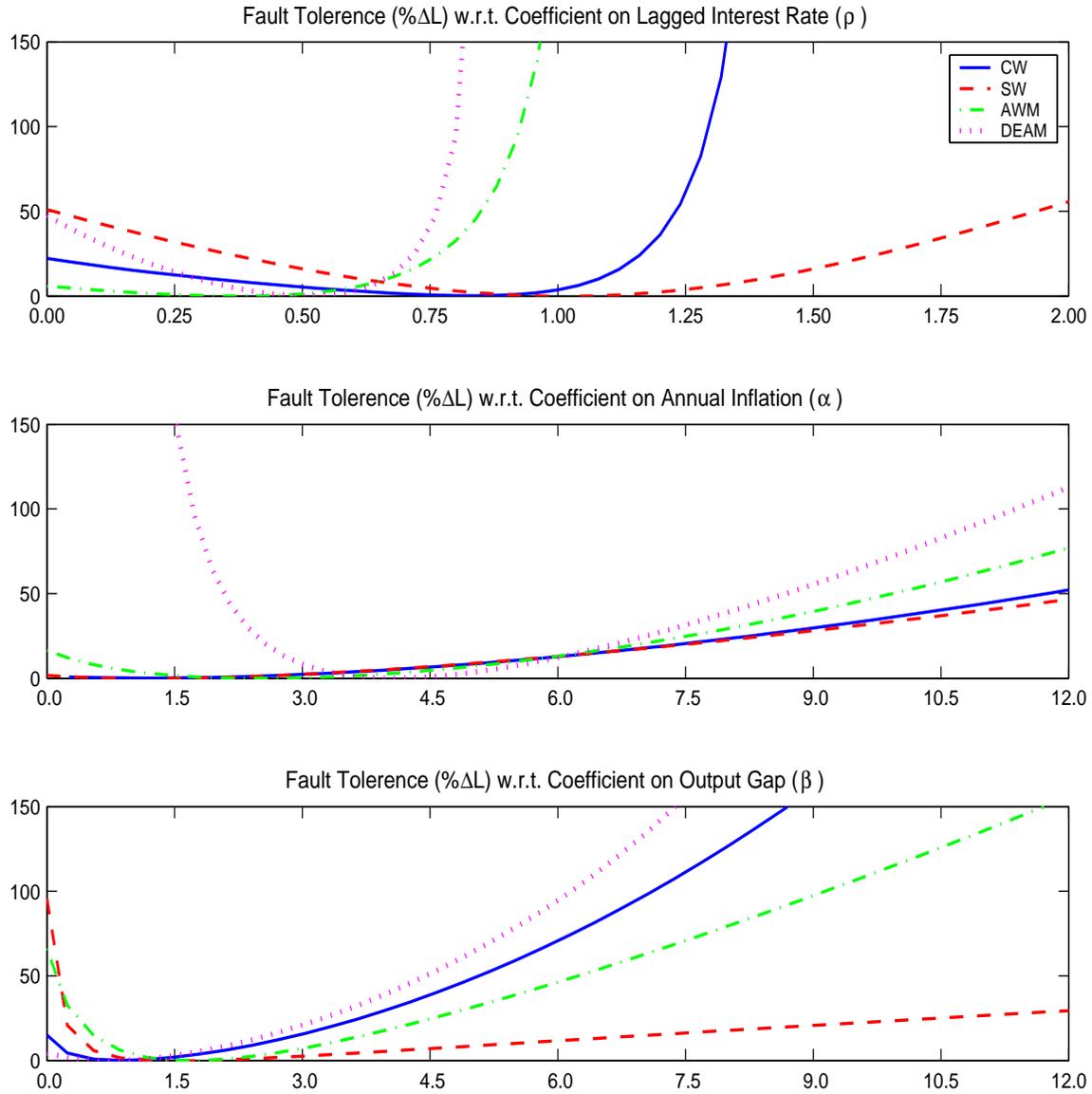
Figure 2 depicts the fault tolerances of our four models for the case $\theta = \kappa = 0$ and $\lambda = 1/3$ (i.e., for the outcome-based rules obtained with a moderate weight on output stabilisation).¹⁹ Each curve shows the percentage-point change in the policy-maker's loss function under the optimised rule as a single parameter is varied, with its minimum of zero attained at the optimised value itself. As can be seen in the figure, while any single parameter may be varied over a relatively broad range of values without deteriorating dramatically the performance of the individual model concerned, there is hardly any overlapping region of high *mutual* fault tolerance for all four models under examination.

Regarding the fault tolerances with respect to the smoothing coefficient ρ (displayed in the upper panel of the figure), the two forward-looking models perform best when ρ is close to unity, while the performance for both the AWM and DEAM deteriorates dramatically in this region, eventually resulting in instrument instability for the DEAM. In contrast, the AWM prefers a ρ coefficient of about 0.5 and the DEAM a coefficient even lower of about 0.25. Values of ρ in this region, however, tend to yield indeterminate equilibria for the forward-looking models, notably for the CW model. With respect to the response coefficient α (depicted in the middle panel), the forward-looking models and the AWM seem mutually tolerant to variations in α in the region of 0.5 to 2. The DEAM, however, behaves very differently in its optimal prescription for α , demanding a dramatically higher value of about 6. As shown in the lower panel, the only region of comparatively high mutual tolerance seems to exist with respect to variations in the response coefficient β in the rather narrow range of 2.5 to 3. While the DEAM favours a strong response to the output gap in the range of 2.5 to 7.5, the three other models perform satisfactorily as a group only for coefficients in the range of 1 to 3, with the CW model constraining the upper bound of this range.

Interestingly, as shown in Figure 3, the four models exhibit considerably larger regions of mutual fault tolerance when the policy-maker follows a forecast-based rule with $\theta = 4$ and $\kappa = 0$. In this case, variations in ρ in the range of 0.5 to 0.7 result in a reasonable

¹⁹For other values of the preference parameter λ the results are qualitatively similar and available on request from the authors.

Figure 3: Fault-Tolerance Analysis of Forecast-Based Interest-Rate Rules



Notes: For $\lambda = 1/3$ and for each model, the figure indicates the percentage-point change in the policy-maker's loss function ($\% \Delta \mathcal{L}$) under the optimised forecast-based interest-rate rule ($\theta = 4, \kappa = 0$) as a single parameter (ρ, α or β) of the optimised rule is varied, holding the other two parameters fixed at their respective optimised values.

performance of all four models. Similarly, there are regions of mutual tolerance with respect to variations in α and β , the regions being centred at 3.5 and 1, respectively.

5 Designing Robust Interest-Rate Rules

The fault-tolerance analysis in the previous section has provided an indication under which circumstances a robust interest-rate rule might exist for our set of euro area models. However, to the extent that fault-tolerance analysis rests on sub-optimal variations in a single policy-rule parameter, holding fixed the other parameters at their optimised values, we finally proceed to use a more formal approach that allows taking into account the interaction amongst all policy-rule parameters to identify the operating characteristics of interest-rules that are likely to yield satisfactory outcomes across our models.

In search of such robust rules we follow the Bayesian approach outlined in LWW (1999, 2003) and optimise the response coefficients of the three-parameter family of interest-rate rules across our four models simultaneously by minimising a weighted average of the loss functions associated with the individual models,

$$\bar{\mathcal{L}} = \sum_{m \in \mathcal{M}} \omega_m \mathcal{L}_m,$$

where ω_m denotes the weight attached to any given model $m \in \mathcal{M} \subseteq \{\text{CW, SW, AWM, DEAM}\}$ with $\omega_m > 0$ and $\sum \omega_m = 1$. For $\omega_m = 1/|\mathcal{M}|$, the average loss function corresponds to the policy-maker's expected loss function when he has uniform prior beliefs as to which model in \mathcal{M} is a plausible representation of the euro area economy.

Panel A of Table 3 reports the response coefficients of outcome and forecast-based rules optimised across all four models simultaneously assuming uniform prior beliefs and indicates the performance of these rules in terms of the percentage-point change in the losses associated with the individual models themselves. Again, the comparison is made with respect to the losses under the fully optimal policies.

Starting with the outcome-based rules with $\theta = \kappa = 0$ it turns out that the robust policies are heavily weighted towards the DEAM, with the optimised coefficients close to those implied by the DEAM alone (see Table 1 above). Specifically, the robust policies

Table 3: The Stabilisation Performance of Bayesian Robust Interest-Rate Rules

θ	κ	λ	ρ	α	β	Robust rule evaluated in			
						CW	SW	AWM	DEAM
A. Optimisation across All Models									
0	0	0	0.54	3.38	2.28	46	38	58	64
		1/3	0.58	3.22	2.71	28	22	46	60
		1	0.58	3.21	3.33	28	30	45	58
		3	0.54	3.33	4.48	29	50	47	56
4	0	0	0.60	3.28	0.49	26	33	25	22
		1/3	0.62	3.27	1.16	11	22	25	28
		1	0.60	3.46	1.90	10	29	25	34
		3	0.54	3.76	3.16	11	42	24	43
B. Optimisation across All Aggregate Models									
0	0	0	0.71	0.76	0.55	14	38	33	
		1/3	0.63	0.64	1.72	8	17	24	
		1	0.64	0.42	2.78	8	17	22	
		3	0.64	0.37	4.37	10	18	20	
4	0	0	0.72	1.26	0.39	20	43	20	
		1/3	0.64	1.40	1.46	8	19	17	
		1	0.62	1.38	2.56	8	19	17	
		3	0.62	1.42	4.17	9	20	16	

Notes: For each choice of the inflation and output-gap forecast horizons (θ and κ) and for each preference parameter (λ), this table indicates the jointly optimised interest-rate response coefficients (ρ , α and β) and the percentage-point change in the contribution of the individual model m to the policy-maker's overall loss function ($\% \Delta \mathcal{L}_m$) compared with its loss under the fully optimal policy.

prescribe a degree of interest-rate smoothing in the range of 0.5 to 0.6, while the responses to inflation and the output gap are quite aggressive. The former is relatively stable at around 3, while the latter varies quite a bit, namely in the range of 2 to 4, depending on the weight given to output stabilisation. In the light of the fault-tolerance analysis reported above, this outcome is not really surprising, since, in the absence of regions of mutual tolerance with respect to some parameter, the least tolerant model is supposed to be most influential

in shaping the characteristics of the robust policy with respect to that parameter.²⁰ As a result, the performance of the robust policies designed for our set of models is rather poor for all models except for the DEAM, as can be seen when comparing the outcomes under the robust policies with the performance measures reported in Table 1 above.

Turning to the forecast-based rules with $\theta = 4$ and $\kappa = 0$, the performance of the robust policies is found to be to be more satisfactory across models. Yet again, this finding is not surprising in the light of the fault-tolerance analysis above indicating the existence of regions of relatively high mutual tolerance for all three parameters. However, the optimised coefficients of the robust rules appear to be largely influenced by the DEAM again.

To the extent that the robust policies for the full set of models are heavily weighted towards the DEAM, panel B of Table 3 also reports results obtained when optimising across all aggregate models, but excluding the DEAM. In this case, the robust policies are characterised by a uniformly higher degree of interest-rate smoothing (in a range of 0.6 to 0.7) and, overall, far less aggressive responses to inflation and the output gap. As expected, the performance of the robust policies designed for the two forward-looking models (CW and SW) and the AWM alone appears more balanced across these models when compared to the performance measures reported in Table 1.

6 Sensitivity Analysis

Now we briefly summarise some additional sensitivity analysis regarding the results presented above. First, we consider the implications of changing the weight μ on the variability of interest-rate changes in the policy-maker's loss function. For the preceding analysis we have chosen a weight of $\mu = 0.1$ which has been widely employed in policy evaluation exercises like ours. As shown in Table B-1 in the appendix, with a weight of $\mu = 0.01$ on interest-rate variability, the relative stabilisation performance of optimised rules is not significantly affected when compared to the baseline results reported in Table 1 above.

²⁰In fact, the DEAM is rather intolerant to even small deviations from the optimised coefficients implied by the DEAM alone, as can be seen in Figure 2. Further to this, the decisive role of the DEAM also relates to the fact that the baseline level of the loss for the DEAM is relatively high when compared with the baseline losses for the other models (see Table A in the appendix).

However, with the variability in interest-rate changes penalised less, there are a number of noticeable differences with regard to the pattern of the optimised coefficients. First, the response coefficients to inflation and the output gap are a good bit larger; and second, for the backward-looking models the optimal degree of interest-rate smoothing is found to be even lower. However, despite these changes in the operating characteristics of the optimised rules, we observe, by comparing the performance measures reported in Table B-2 with those in Table 2, that the robustness properties of the optimised rules (or the lack thereof) are broadly unaffected if the weight on interest-rate variability is lowered to $\mu = 0.01$. Finally, as documented in Table B-3 compared to Table B-1, jointly optimised interest-rate rules are yet again found to be weighted towards the DEAM, with the relatively favourable performance of robust forecast-based rules being less clear-cut though.

Regarding the sensitivity of our results with respect to using a ‘real-time’ information set with $\theta = \kappa = -1$, Table C-1 shows that, as expected, the performance of real-time-based rules tends to deteriorate relative to that of outcome-based rules. For the more backward-looking models, this deterioration is rather pronounced (up to 20 and 34 percentage points for DEAM and AWM, respectively). Similarly, as shown in Table C-2, the robustness of real-time-based rules tends to be inferior to that of outcome-based ones, resulting in a somewhat larger deterioration of performance across models. Finally, as indicated in Table C-3, the performance of the robust real-time-based rules is slightly inferior across models as well.

7 Conclusions

In this paper, we examined the performance and robustness of optimised interest-rate rules in four models of the euro area which differ considerably in terms of size, degree of aggregation, relevance of forward-looking behavioural elements and adherence to micro-foundations. Based on our examination, we conclude that simple interest-rate rules that are optimised for a given model may perform satisfactorily in models with a not too dissimilar structure but may result in a dramatic deterioration of performance in models with markedly different features. In particular, rules that are designed for largely forward-looking models tend to

perform poorly in predominantly backward-looking models, although the reverse is not necessarily true. In view of this asymmetry, we find that the operating characteristics of robust rules are likely to be heavily weighted towards backward-looking models. Accordingly, we find that a forecast-based rule, which relates the short-term interest rate to the one-year ahead forecast of inflation and the contemporaneous output gap and, importantly, which allows for only a moderate degree of smoothing, may have a chance to perform comparatively well across our set of models.

While other model features such as variable and country coverage and adherence to micro-foundations are apparently of relevance as well, the nature of the expectation formation mechanism embedded in the various models seems to be of key importance for explaining our results. This in turn suggests that future research that aims at casting light on the empirical relevance of forward-looking behavioural elements in macroeconomic models may considerably enhance the reliability and usefulness of interest-rate rules for model-based evaluations of monetary policy.

Of course, in the case that a policy rule prescribed to set the interest rate in response to forecasts of future inflation, we assumed in our analysis that these forecasts happened to be consistent with the structure of the particular model in which the performance of the forecast-based rule was evaluated. Similarly, the measure of the output gap used when evaluating the rule was consistent with the output-gap concept employed in that particular model. To the extent that the monetary policy-maker faces uncertainty regarding the reliability of the inflation forecast itself or the correct measurement of the output gap these additional sources of uncertainty may heighten the risks associated with relying too heavily on a rule optimised for any particular model.²¹ Extensions of our study along these directions are left for future research.

²¹Indeed, the analysis in Coenen (2003) shows that erroneously relying on the false forecasting model may result in a significant deterioration of the stabilisation performance of a forecast-based rule, even when the rule itself is designed under the assumption that the structure of the economy is known. The consequences of relying on alternative, possibly inconsistent output-gap concepts is analysed in Smets and Wouters (2002).

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Appendix

Table A: Detailed Results for the Optimised Interest-Rate Rules

A. The Forward-Looking Euro Area Models											
θ	κ	λ	CW				SW				
			σ_π	σ_y	$\sigma_{\Delta i}$	\mathcal{L}	σ_π	σ_y	$\sigma_{\Delta i}$	\mathcal{L}	
0	0	0	1.33	2.30	0.80	1.83	0.93	2.47	0.47	0.95	
		1/3	1.45	1.07	0.82	2.54	1.06	0.60	0.87	1.33	
		1	1.48	0.91	1.26	3.17	1.08	0.40	1.21	1.48	
		3	1.48	0.83	1.93	4.65	1.09	0.28	1.68	1.71	
4	0	0	1.35	2.09	0.79	1.89	0.94	2.44	0.51	0.98	
		1/3	1.47	1.02	0.83	2.58	1.07	0.58	0.87	1.34	
		1	1.48	0.90	1.26	3.18	1.08	0.40	1.21	1.48	
		3	1.49	0.83	1.91	4.65	1.09	0.29	1.64	1.70	
B. The Backward-Looking Euro Area Models											
θ	κ	λ	AWM				DEAM				
			σ_π	σ_y	$\sigma_{\Delta i}$	\mathcal{L}	σ_π	σ_y	$\sigma_{\Delta i}$	\mathcal{L}	
0	0	0	1.09	1.57	1.04	1.30	2.15	1.68	3.69	5.97	
		1/3	1.07	1.17	1.74	1.90	2.17	1.60	3.62	6.86	
		1	1.07	0.91	2.50	2.59	2.22	1.50	3.59	8.45	
		3	1.07	0.69	3.52	3.52	2.36	1.36	3.68	12.48	
4	0	0	1.04	1.59	1.01	1.19	1.89	1.58	3.29	4.64	
		1/3	1.02	1.16	1.69	1.78	1.90	1.51	3.24	5.44	
		1	1.03	0.90	2.43	2.46	1.95	1.43	3.23	6.87	
		3	1.04	0.69	3.42	3.65	2.07	1.31	3.34	10.56	

Notes: For each choice of the inflation and output-gap forecast horizons (θ and κ), for each preference parameter (λ) and for each model, this table indicates the unconditional standard deviations of the target variables (σ_π , σ_y and $\sigma_{\Delta i}$) and the value of the policy-maker's loss function (\mathcal{L}).

Table B-1: The Stabilisation Performance of Optimised Interest-Rate Rules Generated with a Lower Weight of $\mu = 0.01$ on Interest-Rate Variability

A. The Forward-Looking Euro Area Models											
θ	κ	λ	CW				SW				
			ρ	α	β	$\% \Delta \mathcal{L}$	ρ	α	β	$\% \Delta \mathcal{L}$	
0	0	0	0.98	2.98	0.25	1	1.03	1.71	0.16	2	
		1/3	0.75	1.26	2.29	5	0.99	1.92	5.25	9	
		1	0.73	0.74	4.09	4	1.02	0.83	11.22	6	
		3	0.69	0.44	6.54	3	1.00	0.84	20.93	4	
4	0	0	2.75	29.26	-0.24	5	2.32	18.26	-0.06	4	
		1/3	0.79	3.30	2.14	7	1.01	3.40	4.73	9	
		1	0.73	1.96	4.14	4	1.00	2.49	10.32	7	
		3	0.68	1.33	6.62	3	1.00	1.72	20.42	4	

B. The Backward-Looking Euro Area Models											
θ	κ	λ	AWM				DEAM				
			ρ	α	β	$\% \Delta \mathcal{L}$	ρ	α	β	$\% \Delta \mathcal{L}$	
0	0	0	0.17	3.05	3.00	24	0.11	13.83	8.33	41	
		1/3	0.42	2.03	6.57	12	0.02	13.24	9.11	42	
		1	0.51	1.37	9.71	9	0.00	11.88	9.65	42	
		3	0.55	0.84	14.55	6	0.00	9.94	10.22	41	
4	0	0	0.23	6.76	1.16	11	0.39	10.58	1.53	9	
		1/3	0.30	5.57	4.69	5	0.27	10.43	2.30	12	
		1	0.37	4.53	8.08	4	0.15	10.28	3.33	16	
		3	0.44	3.53	13.10	4	0.00	9.83	5.12	19	

Notes: For each choice of the inflation and output-gap forecast horizons (θ and κ), for each preference parameter (λ) and for each model, this table indicates the optimised interest-rate response coefficients (ρ , α and β) and the percentage-point change in the policy-maker's loss function ($\% \Delta \mathcal{L}$) compared with the loss under the fully optimal policy.

Table B-2: The Robustness of Optimised Interest-Rate Rules Generated with a Lower Weight of $\mu = 0.01$ on Interest-Rate Variability

A. Rules Optimised for the Forward-Looking Euro Area Models								
θ	κ	λ	CW rule evaluated in			SW rule evaluated in		
			SW	AWM	DEAM	CW	AWM	DEAM
0	0	0	3	∞	∞	4	∞	∞
		1/3	12	36	420	13	34	∞
		1	13	29	2046	31	29	∞
		3	17	30	∞	67	16	∞
4	0	0	4	∞	∞	6	∞	∞
		1/3	12	30	704	13	43	∞
		1	12	21	567	25	23	∞
		3	16	23	1125	63	18	∞

B. Rules Optimised for the Backward-Looking Euro Area Models								
θ	κ	λ	AWM rule evaluated in			DEAM rule evaluated in		
			CW	SW	DEAM	CW	SW	AWM
0	0	0	28	30	556	57	29	44
		1/3	10	12	1454	31	26	19
		1	11	10	4291	33	47	14
		3	15	9	∞	39	92	17
4	0	0	18	33	824	27	30	15
		1/3	12	16	842	41	26	21
		1	9	13	1237	17	45	33
		3	10	12	4551	26	88	54

Notes: For each choice of the inflation and output-gap forecast horizons (θ and κ), for each preference parameter (λ) and for each model, this table indicates the percentage-point change in the policy-maker's loss function ($\% \Delta \mathcal{L}$) when the rule optimised for model i is evaluated in model $j \neq i$, compared with the loss under the fully optimal policy for model j . The notation " ∞ " indicates that the implemented rule results in instability.

Table B-3: The Stabilisation Performance of Robust Outcome-Based Interest-Rate Rules Generated with a Lower Weight of $\mu = 0.01$ on Interest-Rate Variability

θ	κ	λ	ρ	α	β	Robust rule evaluated in				
						CW	SW	AWM	DEAM	
A. Optimisation across All Models										
0	0	0	0.42	8.54	5.81	39	25	32	46	
		1/3	0.39	7.86	6.69	17	18	27	47	
		1	0.33	7.63	8.02	20	31	36	49	
		3	0.21	7.54	10.31	26	60	53	49	
4	0	0	0.47	8.62	1.19	33	28	14	45	
		1/3	0.45	8.14	3.17	10	17	13	38	
		1	0.38	8.31	4.93	10	23	16	37	
		3	0.26	8.56	7.56	12	39	22	39	
B. Optimisation across All Aggregate Models										
0	0	0	0.56	2.73	1.53	21	43	32		
		1/3	0.59	1.74	4.78	7	11	14		
		1	0.63	1.04	7.03	6	10	12		
		3	0.61	0.65	10.37	6	11	10		
4	0	0	0.64	4.78	0.81	5	29	16		
		1/3	0.57	3.77	4.07	2	8	7		
		1	0.59	3.09	6.63	2	6	7		
		3	0.58	2.66	10.17	3	6	7		

Notes: For each choice of the inflation and output-gap forecast horizons (θ and κ) and for each preference parameter (λ), this table indicates the jointly optimised interest-rate response coefficients (ρ , α and β) and the percentage-point change in the contribution of the individual model i to the policy-maker's overall loss function ($\% \Delta \mathcal{L}_i$) compared with its loss under the fully optimal policy.

Table C-1: The Stabilisation Performance of Optimised Interest-Rate Rules Based on a Real-Time Information Set with $\theta = \kappa = -1$

A. The Forward-Looking Euro Area Models								
λ	CW				SW			
	ρ	α	β	$\% \Delta \mathcal{L}$	ρ	α	β	$\% \Delta \mathcal{L}$
0	0.95	0.79	0.11	2	1.02	0.79	0.08	3
1/3	0.76	0.48	0.91	6	0.98	0.56	1.38	11
1	0.74	0.29	1.58	5	0.96	0.35	2.62	12
3	0.72	0.28	2.43	6	0.98	0.00	3.44	20

B. The Backward-Looking Euro Area Models								
λ	AWM				DEAM			
	ρ	α	β	$\% \Delta \mathcal{L}$	ρ	α	β	$\% \Delta \mathcal{L}$
0	0.42	0.99	1.11	34	0.17	6.07	4.26	88
1/3	0.27	0.82	2.16	40	0.13	6.06	4.46	85
1	0.26	0.54	3.19	55	0.07	6.02	4.77	81
3	0.25	0.34	4.60	84	0.00	5.79	5.30	74

Notes: For each preference parameter (λ) and for each model, this table indicates the optimised interest-rate response coefficients (ρ , α and β) and the percentage-point change in the policy-maker's loss function ($\% \Delta \mathcal{L}$) compared with the loss under the fully optimal policy.

Table C-2: The Robustness of Optimised Interest-Rate Rules Based on a Real-Time Information Set with $\theta = \kappa = -1$

A. Rules Optimised for the Forward-Looking Euro Area Models

λ	CW rule evaluated in			SW rule evaluated in		
	SW	AWM	DEAM	CW	AWM	DEAM
0	6	∞	∞	4	∞	∞
1/3	18	80	1388	14	766	1417
1	24	103	∞	23	872	∞
3	38	157	∞	ME	∞	∞

B. Rules Optimised for the Backward-Looking Euro Area Models

λ	AWM rule evaluated in			DEAM rule evaluated in		
	CW	SW	DEAM	CW	SW	AWM
0	20	36	2345	93	71	140
1/3	11	29	∞	61	50	106
1	ME	38	∞	59	67	110
3	ME	58	∞	57	115	143

Notes: For each preference parameter (λ) and for each model, this table indicates the percentage point change in the policy-maker's loss function ($\% \Delta \mathcal{L}$) when the rule optimised for model i is evaluated in model $j \neq i$, compared with the loss under the fully optimal policy for model j . The notation "ME" indicates that the implemented rule yields multiple equilibria; the notation " ∞ " indicates that the implemented rule results in instability.

Table C-3: The Stabilisation Performance of Robust Outcome-Based Interest-Rate Rules Based on a Real-Time Information Set with $\theta = \kappa = -1$

λ	ρ	α	β	Robust rule evaluated in			
				CW	SW	AWM	DEAM
A. Optimisation across All Models							
0	0.41	3.62	2.52	48	44	81	103
1/3	0.41	3.57	2.88	31	30	80	95
1	0.39	3.62	3.46	33	44	95	89
3	0.32	3.75	4.54	37	76	125	82
B. Optimisation across All Aggregate Models							
0	0.65	0.78	0.61	14	39	40	
1/3	0.51	0.64	1.70	8	22	44	
1	0.47	0.57	2.68	9	29	60	
3	0.41	0.59	4.10	13	45	88	

Notes: For each preference parameter (λ), this table indicates the jointly optimised interest-rate response coefficients (ρ , α and β) and the percentage-point change in the contribution of the individual model i to the policy-maker's overall loss function ($\% \Delta \mathcal{L}_i$) compared with its loss under the fully optimal policy.