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Are asset price data informative about
news shocks?
A DSGE perspective

Abstract

Standard economic intuition suggests that asset prices are more sensitive to news than other economic aggregates. This has led many researchers to conclude that asset price data would be very useful for the estimation of business cycle models containing news shocks. This paper shows how to formally evaluate the information content of observed variables with respect to unobserved shocks in structural macroeconomic models. The proposed methodology is applied to two different real business cycle models with news shocks. The contribution of asset prices is found to be relatively small. The methodology is general and can be used to measure the informational importance of observables with respect to latent variables in DSGE models. Thus, it provides a framework for systematic treatment of such issues, which are usually discussed in an informal manner in the literature.

Non-technical summary

Structural macroeconomic models, usually referred to as dynamic stochastic general equilibrium (DSGE) models, are one of the main tools of quantitative macroeconomics. Macroeconomists use them to formalize their reasoning about how the world works, to assess the relative importance of different economic forces, and to provide prescriptions on economic policy. An important requirement for such models to be useful in practice is that their parameters are estimated from data. In addition to parameters, when taking models to the data, researchers are also interested in estimating various unobserved variables such as output gap, natural rate of interest, as well as different exogenous shocks driving the economy. In order to assess the credibility of estimated models, it is important to understand whether there is sufficient information in the data about the objects of interest - parameters and unobserved variables, and what the main sources of such information are. However, as models grow in size and complexity, it has become impossible to answer these questions by reasoning alone.

This paper makes both a methodological and a substantive contribution. On the methodological side, it shows how to assess a DSGE model's implications regarding the contribution of information of observed variables with respect to unobserved shocks or other unobserved endogenous variables. Such issues are frequently discussed in a heuristic fashion in the DSGE literature. The main purpose here is to show how to approach them in a systematic manner. Intuitively, information can be interpreted as the reduction of uncertainty about an unknown quantity. This is made precise by using well-established measures of uncertainty, mutual information and information gains developed in information theory. The transfer of information is quantified by comparing different probability distributions, e.g. distributions of shocks conditional on nested sets of observables. The required distributions are completely characterized by the underlying structural model, and in the class of linearized Gaussian DSGE models, the required quantities are available in closed form.

The application part of the paper evaluates the information content of asset price variables in two estimated real business cycle models featuring news shocks. The models are taken from Schmitt-Grohé and Uribe (2012) and Avdjiev (2016), and differ mainly in the number of fundamental shocks and in the way news shocks are introduced. The asset price variables considered are the value of the representative firm, which in the data is matched to stock price indices, and the risk-free real interest rate. For both models the

results suggest relatively small contributions of asset prices with respect to news shocks. While including asset prices as observables increases the amount of information about some news shocks, their marginal contributions are comparable to the contributions of non-asset price variables, such as hours worked, total factor productivity or the relative price of investment. The only news shocks with respect to which asset prices, specifically the risk-free interest rate, are found to contribute more information than any other variable are the news about the stationary neutral productivity shock.

1 Introduction

There is a general tendency in the study of business cycles towards estimating different types of models using a common set of macroeconomic aggregates. Perhaps the main reason for this is the desire to let models compete on the same ground and have results that are easy to compare with the rest of the literature. At the same time, as models evolve and new features are introduced, it sometimes appears necessary to expand the number and type of variables used to estimate them.

One of the important recent developments has been the idea that news shocks could be a significant driver of business cycles. The traditional explanation of business cycles is that they are caused by exogenous unanticipated changes in economic fundamentals. Following the work of Beaudry and Portier (2004, 2006), a lot of research has been devoted to the question whether anticipated changes in future fundamentals, or news shocks, could also be an important source of aggregate fluctuations.

News shocks are usually introduced in dynamic stochastic general equilibrium models (DSGE) models by adding anticipated components to innovations driving exogenous shock processes. From an econometric point of view, this raises the question of whether standard macroeconomic variables are sufficiently informative to estimate models with news, or different type of data are required. A common approach in many recent studies has been to estimate news-driven DSGE models using only variables that are also standard in the estimation of models without news.[1] There are also some notable exceptions. For instance Davis (2007) uses term structure data, Hirose and Kurozumi (2012), Milani and Rajbhandari (2012), and Miyamoto and Nguyen (2015) use data on expectations, and Malkhozov and Tamoni (2015), Avdjiev (2016) and Görtz and Tsoukalas (2016) use asset price data. The authors of these papers contend that the variables they use are particularly informative with respect to news shocks, and that without such variables it is difficult to identify and estimate accurately news shocks and their contribution to business cycle fluctuations.

No formal evidence is given to support these claims. For instance, the argument for using asset price data is based on the observation that asset prices are very responsive to changes in information, e.g. to news. Because of that, asset price data are perceived as being more informative about news shocks compared to other macroeconomic variables, which, due to various real and nominal rigidities, are less sensitive to news. Similar

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[1]In fact, it is a common practice to introduce news shocks to models that have previously been estimated without news, and estimate them using the same set of observables.

arguments can also be found in the structural VAR literature where asset prices, and in particular stock price data, often play a central role in the identification of news shocks.[2]

There are two potential problems with this line of reasoning when applied to the estimation of news-driven DSGE models. First, the identification of news derives from model-implied restrictions on the relationship between the unobserved shocks and the variables used to estimate the model. Thus, the information content of different variables depends on how news shocks are introduced and propagate in the particular model, and not on what the propagation mechanism is believed to be in reality. Second, if news are important for aggregate fluctuations, and not just for fluctuations in stock prices, then macroeconomic aggregates should be informative about news shocks. Since DSGE models impose many more identifying restrictions than SVARs, there could be enough information to separate news from other sources of fluctuations on the basis of standard macroeconomic variables.

This paper makes both a methodological and a substantive contribution. On the methodological side, it shows how to assess a DSGE model's implications regarding the contribution of information of observed variables with respect to unobserved shocks. Such issues are frequently discussed in a heuristic fashion in the DSGE literature. The main purpose here is to show how to approach them in a systematic manner. Intuitively, information can be interpreted as the reduction of uncertainty about an unknown quantity. This is made precise by using well-established measures of uncertainty, mutual information and information gains developed in information theory. The transfer of information is quantified by comparing different probability distributions, e.g. distributions of shocks conditional on nested sets of observables. The required distributions are completely characterized by the underlying structural model, and in the class of linearized Gaussian DSGE models, the required quantities are available in closed form. The application part of the paper evaluates the information content of asset price variables in two estimated real business cycle models featuring news shocks. The models are taken from Schmitt-Grohé and Uribe (2012) and Avdjiev (2016), and differ mainly in the number of fundamental shocks and in the way news shocks are introduced. The asset price variables considered are the value of the representative firm, which in the data is matched to stock price indices, and the risk-free real interest rate. For both models the results suggest relatively small contributions of asset prices with respect to news shocks.

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[2]See, for instance Beaudry and Portier (2006) Barsky and Sims (2011), Kurmann and Otrok (2013), Barsky et al. (2014).

While including asset prices as observables increases the amount of information about some news shocks, their marginal contributions are comparable to the contributions of non-asset price variables, such as hours worked, total factor productivity or the relative price of investment. The only news shocks with respect to which asset prices, specifically the risk-free interest rate, are found to contribute more information than any other variable are the news about the stationary neutral productivity shock.

In terms of methodology, this paper is related to a large literature on measuring the relative importance of variables in scientific models. A common application of this type of analysis is to determine the relative importance of individual regressors in explaining the behavior of response variables (Kruskal (1987)). The use of information-theoretic measures in that context dates back at least to Theil (1987), who uses a decomposition of Gaussian mutual information to quantify the contribution of independent explanatory variables in multivariate regressions.[3] A comprehensive treatment of the subject from an information theory perspective is given in Retzer et al. (2009), who characterize the importance of variables by the extent to which their use reduces uncertainty about predicting the response variable. Another important area of application is the study of causal relationships in the analysis of time series. Following the seminal work of Granger (1969), the notion of causality has been associated with the question of whether knowledge of past values of one time series helps improve the forecasts of another. While most of the early work on this topic focused on how to test for the existence and direction of causality, Geweke (1982, 1984) show how to quantify the strength of causal influence. Geweke's measures are based on the magnitude of the reduction of forecast uncertainty, measured by the mean square forecast errors of the predicted variable, due to using past values of the causal variable. In that sense, measuring Granger causality can be interpreted as quantifying the contribution of information by observed variables – past observations of the cause variable, with respect to unobserved ones – the future values of the predicted variable, conditional on a set of other observed variables – the past values of the predicted variable.[4] This is precisely the meaning of conditional mutual information, and, as Barnett et al. (2009) show, when the join distribution of the variables is Gaussian, Geweke's measures of strength of causality are equivalent to the "transfer entropy" of

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[3]See also Theil and Chung (1988) where the analysis is extended to systems of simultaneous equations, and Soofi (1992), who applies the same ideas to determine the relative importance of predictors in logit models.

[4]In his Nobel prize acceptance lecture Granger defined causality as follows: (1) The cause occurs before the effect; (2) The cause contains information about the effect that is unique, and is in no other variable.

Schreiber (2000), which is an information-theoretic measure of the transfer of information between two stochastic processes.[5] Extensions to non-linear and non-Gaussian models involve replacing the forecast error variances with entropic measures of uncertainty (see Amblard and Michel (2011)). In a recent article Jarociński and Maćkowiak (2017) develop new analytical results for Granger causality in Bayesian vector autoregressions (VAR), and show how to use them for selecting the relevant variables to include in VAR models.

Instead of strength of causality, the purpose of the measures presented in this paper is to quantify the amount of information that realizations of observed variables contribute with respect to contemporaneous but unobserved realizations of structural shocks (or other latent variables). Since mathematically there is no difference between unobserved future realizations of observed variables and unobserved contemporaneous realizations of latent variables, the proposed measures of information gains are analogous, with minor modifications, to the Granger causality strength measures of Geweke (1982, 1984) in the case of linearized Gaussian DSGE models, and to non-linear Granger causality measures in the general case.

The paper is also related to a growing literature on the feasibility of recovering structural shocks using reduced form models. Building upon the work of Hansen and Sargent (1980, 1991) and Lippi and Reichlin (1993, 1994), most of the research on this topic has focused on the issue of invertibility (or fundamentalness) in structural vector autoregressions, i.e. whether shocks from general equilibrium models can be recovered from the residuals of VARs (see Alessi et al. (2011) and Giacomini (2013) for useful overviews of this literature). Conditions for invertibility are discussed in Fernandez-Villaverde et al. (2007), Ravenna (2007), Franchi and Vidotto (2013), Franchi and Paruolo (2015)), while Giannone and Reichlin (2006) and Forni and Gambetti (2014) discuss how to test for lack of invertibility of structural VARs. Invertibility issues that are specific to DSGE models with news shocks are discussed in Leeper et al. (2013) and Blanchard et al. (2013). More recently, Soccorsi (2016) and Sala et al. (2016) proposed measures of the degree of non-invertibility, which quantify the discrepancies between true shocks and shocks obtained using non-fundamental VARs.[6]

Similar to that literature, the analysis in the present paper can be used to determine

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[5]See also Pourahmadi and Soofi (2000) who use conditional mutual information to quantify the information worth of past observations for predicting future values of univariate time series.

[6]Simulation evidence that non-invertible VARs may in some cases produce good approximations of the true structural shocks are provided in Sims (2012) and Beaudry et al. (2015).

if the shocks in a DSGE model can be recovered from a set of observed model variables. Furthermore, similar to Soccorsi (2016) and particularly Sala et al. (2016), a measure of the degree to which any individual shock, and more generally, any unobserved exogenous or endogenous model variable, can be recovered is provided. In particular, the proposed measures of information gains are defined with respect to a particular unobserved variable and show how much of the prior uncertainty about it is removed due to observing a set of model variables. An important difference with the invertibility literature is that the analysis here is based on the true data generating process characterized by a structural model, and not on approximations of it, such as a VAR. The proposed information gain measures are, in their general form, meaningful and useful when applied to non-linear DSGE models, while the invertibility conditions and measures in the existing literature are specific to linearized models. In the context of linearized DSGE models, the information gain measures could be interpreted as upper bounds on the amount of information about a shock (or the degree of information sufficiency in the terminology of Sala et al. (2016)) available in a VAR.

More importantly, while the existing research on invertibility is concerned with the usefulness of VAR–based tools for empirical validation of structural models, the purpose of the analysis presented here is to understand the properties of DSGE models in terms of how information transfers between observed and unobserved model variables. Therefore, identifying the main sources of information is of greater interest than what the total amount of information about a given shock is. To that end, I define and apply measures of conditional information gains that quantify the amount of additional information contributed by a variable or several variables, given the information contained in another set of observed variables. As the analysis of the models considered in the paper shows, the conclusions one draws may be very different depending on what the conditional variables are. For instance, asset prices are found to be unconditionally very informative with respect to wage markup news shocks in the model of Schmitt-Grohé and Uribe (2012), but conditional on observing other macro variables, the information gains are small. At the same time, asset prices may be conditionally quite informative about certain productivity news shocks even though the unconditional information gains are close to zero. These findings are a reflection of the fact that information contained in different variables is not necessarily independent and could be overlapping in some cases while complementary in others. A somewhat extreme example of this phenomenon is the finding that output growth is informationally completely redundant in the model

of Schmitt-Grohé and Uribe (2012) and nearly redundant in the model of Avdjiev (2016). In general, information contained in different variables tends to be partially redundant with respect to some shocks and complementary with respect to others. A novel measure of pairwise information complementarity is introduced in the paper and used to determine the sign and assess the degree of complementarity among observed variables with respect to unobserved ones. In particular, the measure is used to clarify the nature of the interactions between asset prices and other macroeconomic variables in terms of information they convey with respect to news shocks.

Even though the focus of this paper is on evaluating the informational importance of observed variables with respect to unobserved shocks, an alternative interpretation of the issue is in terms of information about model parameters. Specifically, one could argue that asset prices are important for news shocks in the sense that observing such variables would significantly reduce the estimation uncertainty of parameters characterizing the distributions of these shocks. To evaluate the contribution of information by variables with respect to parameters, I compute efficiency gains by comparing the values of the Cramér-Rao lower bounds (hereafter denoted by CRLB)) conditional on different sets of observed variables. The same approach is used by Wei (1978a,b) and Palm and Nijman (1984) to measure the effect of having missing observations due to temporal aggregation, and by Iskrev (2010) to assess the importance of different observables with respect to individual parameters in DSGE models. In a related study Canova et al. (2014) propose an alternative method for selecting the most informative subset of observables for singular models. Simulation-based evidence on the relative performance of Canova et al. (2014) approach and the CRLB-based predictions can be found in Iskrev and Ritto (2016).

The remainder of the paper is organized as follows. Section 2 gives an overview of the relevant information-theoretic concepts, and defines measures of information gains with respect to latent variables, and efficiency gains with respect to parameters. The proposed measures are then applied, in Section 3, to evaluate the information content of asset prices in two different DSGE models containing news shocks. Section 4 concludes.

2 Measures of information and information gains

A DSGE model completely characterizes the joint probability distribution of a $n_{\boldsymbol{y}}$ vector of *observed* endogenous variables $\boldsymbol{y}$, and a $n_{\boldsymbol{z}}$ vector of *unobserved* endogenous variables and exogenous shocks $\boldsymbol{z}$. Note that in practice the dimension of each of these vectors is

a function of a sample size T. For notational simplicity I suppress the dependence on T throughout this section unless it is necessary to make it explicit. The joint distribution function of $\boldsymbol{y}$ and $\boldsymbol{z}$ is parameterized in terms of a $n_{\boldsymbol{\theta}}$ vector of structural parameters $\boldsymbol{\theta}$, characterizing technology, preferences, and the properties of the exogenous variables. Both $\boldsymbol{\theta}$ and $\boldsymbol{z}$ are typically unknown and unobserved, and the only source of empirical information about them are the measurements of $\boldsymbol{y}$. The purpose of this section is to show how to quantify the amount of information contained in a sample of data, and how to evaluate the contributions of individual observed variables.

One way to approach these questions would be to adopt a Bayesian perspective and treat $\boldsymbol{z}$ as part of the parameter vector to be estimated. Then, the amount of information provided by a sample would be with respect to $(\boldsymbol{\theta}, \boldsymbol{z})$ jointly. While conceptually feasible, this approach would be very challenging in practice in the present context, given the large dimension of $\boldsymbol{z}$ and the complicated form of the conditional distribution of $(\boldsymbol{\theta}, \boldsymbol{z})$ given $\boldsymbol{y}$. Therefore, in most of this section I treat $\boldsymbol{\theta}$ as known and measure sample information and information gains about $\boldsymbol{z}$ conditional on $\boldsymbol{\theta}$. At the end of the section I discuss the issue of measuring sample information about $\boldsymbol{\theta}$.

2.1 Information about latent variables

A well-established measure of information about random variables is the information-theoretic entropy introduced by Shannon (1948). Entropy is a measure of the uncertainty associated with a random variable, and the amount of information about that variable is measured as the reduction in uncertainty, i.e. entropy, relative to some base distribution. Specifically, let $f(\boldsymbol{z})$ be the probability density function of $\boldsymbol{z}$. For notational simplicity throughout this subsection I suppress the dependence on $\boldsymbol{\theta}$. The entropy $\mathrm{H}(\boldsymbol{z})$ of $f(\boldsymbol{z})$ is defined as

$$\mathrm{H}(\boldsymbol{z}) := -\int f(\boldsymbol{z}) \ln\left(f(\boldsymbol{z})\right) d\boldsymbol{z} = -\operatorname{E} \ln f(\boldsymbol{z}). \tag{2.1}$$

Similarly, if $f(\boldsymbol{y}, \boldsymbol{z})$ is the joint probability density function of $\boldsymbol{y}$ and $\boldsymbol{z}$, the joint entropy $\mathrm{H}(\boldsymbol{y}, \boldsymbol{z})$ of $f(\boldsymbol{y}, \boldsymbol{z})$ is defined as

$$\mathrm{H}(\boldsymbol{y}, \boldsymbol{z}) := -\int f(\boldsymbol{y}, \boldsymbol{z}) \ln\left(f(\boldsymbol{y}, \boldsymbol{z})\right) d\boldsymbol{y} d\boldsymbol{z} = -\operatorname{E} \ln f(\boldsymbol{y}, \boldsymbol{z}) \tag{2.2}$$

The difference between joint and marginal entropies

$$\mathrm{H}(\boldsymbol{z}|\boldsymbol{y}) = \mathrm{H}(\boldsymbol{y}, \boldsymbol{z}) - \mathrm{H}(\boldsymbol{y}) \tag{2.3}$$

defines the conditional entropy of $\boldsymbol{z}$ given $\boldsymbol{y}$. It measures the amount of uncertainty about $\boldsymbol{z}$ that remains once $\boldsymbol{y}$ is observed. Note that $\mathrm{H}(\boldsymbol{z}|\boldsymbol{y})$ can be computed as in (2.1) using the conditional density $f(\boldsymbol{z}|\boldsymbol{y})$ of $\boldsymbol{z}$ given $\boldsymbol{y}$. It can be shown (see for instance Granger and Lin (1994)) that $\mathrm{H}(\boldsymbol{z}) \geq \mathrm{H}(\boldsymbol{z}|\boldsymbol{y})$ with equality if and only if $f(\boldsymbol{y}, \boldsymbol{z}) = f(\boldsymbol{y})f(\boldsymbol{z})$. Hence, unless $\boldsymbol{y}$ and $\boldsymbol{z}$ are independent, observing $\boldsymbol{y}$ provides information about $\boldsymbol{z}$. The amount of uncertainty about $\boldsymbol{z}$ that is removed by observing $\boldsymbol{y}$ is known as the mutual information of $\boldsymbol{y}$ and $\boldsymbol{z}$, i.e.[7]

$$\mathrm{I}(\boldsymbol{y}, \boldsymbol{z}) = \mathrm{H}(\boldsymbol{z}) - \mathrm{H}(\boldsymbol{z}|\boldsymbol{y}). \tag{2.4}$$

$\mathrm{I}(\boldsymbol{y}, \boldsymbol{z})$ is a measure of information in the sense that it quantifies the expected reduction in uncertainty about one of the variables due to observing the other one. From $\mathrm{H}(\boldsymbol{z}) \geq \mathrm{H}(\boldsymbol{z}|\boldsymbol{y})$ it follows that mutual information is positive unless $\boldsymbol{y}$ and $\boldsymbol{z}$ are independent in which case it is zero. On the other hand, if the variables are perfectly dependent i.e. there exists a one-to-one function g such that $\boldsymbol{z} = g(\boldsymbol{y})$, observing $\boldsymbol{y}$ is equivalent to observing $\boldsymbol{z}$. In that case $\mathrm{I}(\boldsymbol{y}, \boldsymbol{z}) = \infty$ (see Granger and Lin (1994, Theorem 2)). It is common in practice to normalize the measure to be in the interval [0, 1]. For instance, Joe (1989) proposed the following transformation

$$\mathrm{I}^*(\boldsymbol{y}, \boldsymbol{z}) = 1 - \exp\left(-2\mathrm{I}(\boldsymbol{y}, \boldsymbol{z})\right) \tag{2.5}$$

as a generalized measure of dependence between two or more random variables. The same transformation is used in Granger and Lin (1994) as a criterion for determining the number of significant lags in nonlinear time series models. The reason why the particular form in (2.5) is chosen is that, for a bivariate Gaussian distribution, $\mathrm{I}^*(\boldsymbol{y}, \boldsymbol{z}) = \rho^2$, where ρ is the linear correlation coefficient between $\boldsymbol{y}$ and $\boldsymbol{z}$. Furthermore, when $\boldsymbol{y}$ and $\boldsymbol{z}$ are

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[7]Mutual information is defined as $\mathrm{I}(\boldsymbol{y}, \boldsymbol{z}) := \int f(\boldsymbol{y}, \boldsymbol{z}) \ln \frac{f(\boldsymbol{y}, \boldsymbol{z})}{f(\boldsymbol{y})f(\boldsymbol{z})} d\boldsymbol{y} d\boldsymbol{z}$ and measures the distance between the joint distribution of $\boldsymbol{y}$ and $\boldsymbol{z}$ and the distribution when the variables are independent. See Cover and Thomas (2006) for more details on the properties of entropy and mutual information.

jointly Gaussian, the transformation in (2.5) results in the following expression[8]

$$\mathrm{I}^*(\boldsymbol{y}, \boldsymbol{z}) = \frac{|\boldsymbol{\Sigma_z}| - |\boldsymbol{\Sigma_{z|y}}|}{|\boldsymbol{\Sigma_z}|}, \tag{2.6}$$

where $\boldsymbol{\Sigma_z}$ is the covariance matrix of the marginal probability density of $\boldsymbol{z}$, and $\boldsymbol{\Sigma_{z|y}}$ is the covariance matrix of the conditional probability density of $\boldsymbol{z}$ given $\boldsymbol{y}$. Hence, for Gaussian distributions, $\mathrm{I}^*(\boldsymbol{y}, \boldsymbol{z})$ measures the reduction in the generalized variance (Wilks (1932)) of vector $\boldsymbol{z}$ due to observing vector $\boldsymbol{y}$, as a fraction of the unconditional generalized variance of $\boldsymbol{z}$. However, as Peña and Rodríguez (2003) and others have noted, the generalized variance is not a dimensionless measure of the uncertainty of a (Gaussian) random vector. For instance, if $\boldsymbol{\Sigma_z}$ is a $n_{\boldsymbol{z}} \times n_{\boldsymbol{z}}$ diagonal matrix with $\sigma^2 < 1$ on the diagonal, $|\boldsymbol{\Sigma_z}| = \sigma^{2n_{\boldsymbol{z}}}$, implying exponential decline of uncertainty as the dimension of $\boldsymbol{z}$ grows. A dimensionless measure of variability proposed in Peña and Linde (2007) is the effective variance $\mathrm{V}_e(\boldsymbol{z})$, defined as

$$\mathrm{V}_e(\boldsymbol{z}) := |\boldsymbol{\Sigma_z}|^{1/n_{\boldsymbol{z}}}. \tag{2.7}$$

When the elements of $\boldsymbol{z}$ are independent, i.e. $\boldsymbol{\Sigma_z}$ is diagonal, the effective variance is equal to the geometric average of the variances of the elements of $\boldsymbol{z}$. In the general case, $\mathrm{V}_e(\boldsymbol{x})$ is equal to the geometric average of the eigenvalues of $\boldsymbol{\Sigma}$. Adopting the effective variance as a scalar measure of the uncertainty associated with Gaussian distributions yields the following measure of the information gained about $\boldsymbol{z}$ from observing $\boldsymbol{y}$:

$$\mathrm{IG}_{\boldsymbol{z}}(\boldsymbol{y}) = \left(\frac{|\boldsymbol{\Sigma_z}|^{1/n_{\boldsymbol{z}}} - |\boldsymbol{\Sigma_{z|y}}|^{1/n_{\boldsymbol{z}}}}{|\boldsymbol{\Sigma_z}|^{1/n_{\boldsymbol{z}}}} \right) 100. \tag{2.8}$$

The interpretation of $\mathrm{IG}_{\boldsymbol{z}}(\boldsymbol{y})$ is the following: it measures the reduction in uncertainty about vector $\boldsymbol{z}$ due to observing vector $\boldsymbol{y}$, as a percent of the unconditional (prior) uncertainty about $\boldsymbol{z}$.

The measure in (2.8) can be generalized for non-Gaussian distribution by noting that $\mathrm{V}_e(\boldsymbol{x})$ is equal to a particular transformation of the entropy $\mathrm{H}(\boldsymbol{z})$ when $\boldsymbol{z}$ is Gaussian. Specifically, Shannon (1948) defined the entropy power $\mathrm{N}(\boldsymbol{z})$ of a vector $\boldsymbol{z}$ with entropy

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[8]This follows from the result that the entropy of a $n_{\boldsymbol{v}}$–dimensional Gaussian variable $\boldsymbol{v} \sim \mathbb{N}(\boldsymbol{\mu_v}, \boldsymbol{\Sigma_v})$ is $\mathrm{H}(\boldsymbol{v}) = 0.5 \left(\ln(2\pi e)^{n_{\boldsymbol{v}}} + \ln|\boldsymbol{\Sigma_v}| \right)$. Therefore, the mutual information of $\boldsymbol{y}$ and $\boldsymbol{z}$ is $\mathrm{I}(\boldsymbol{y}, \boldsymbol{z}) = \mathrm{H}(\boldsymbol{z}) - \mathrm{H}(\boldsymbol{z}|\boldsymbol{y}) = .5 \ln \left(\frac{|\boldsymbol{\Sigma_z}|}{|\boldsymbol{\Sigma_{z|y}}|} \right)$.

$H(\boldsymbol{z})$ to be

$$N(\boldsymbol{z}) := \frac{1}{2\pi e} \exp\left(\frac{2}{n_{\boldsymbol{z}}} H(\boldsymbol{z})\right), \tag{2.9}$$

which for $\boldsymbol{z} \sim \mathbb{N}(\boldsymbol{\mu_z}, \boldsymbol{\Sigma_z})$ implies $N(\boldsymbol{z}) = |\boldsymbol{\Sigma_z}|^{1/n_{\boldsymbol{z}}}$. Similarly, the conditional entropy power of $\boldsymbol{z}$ given $\boldsymbol{y}$ is $N(\boldsymbol{z}|\boldsymbol{y}) = |\boldsymbol{\Sigma_{z|y}}|^{1/n_{\boldsymbol{z}}}$. Note that, unlike entropy which can be negative (for continuous variables), entropy power is always non-negative, and is therefore a more appealing measure of uncertainty. Thus, $IG_{\boldsymbol{z}}(\boldsymbol{y})$ can be defined for non-Gaussian distribution as in (2.8), replacing the effective variance with entropy power. It can also be expressed in terms of mutual information using the following transformation:

$$IG_{\boldsymbol{z}}(\boldsymbol{y}) = \left(1 - \exp\left(-\frac{2}{n_{\boldsymbol{z}}} I(\boldsymbol{y}, \boldsymbol{z})\right)\right) 100. \tag{2.10}$$

Hence $IG_{\boldsymbol{z}}(\boldsymbol{y})$ is a simple modification of the transformation in (2.5) that allows information gains to be compared for vectors of different dimensions.

In the context of DSGE models, one is often interested in the information content of one or more observed variables with respect to a particular latent variable. Hence, the relevant information gain measure is of the form $IG_{\boldsymbol{z}^j}(\boldsymbol{y}^i)$, where $\boldsymbol{z}^j$ is a $n_{\boldsymbol{z}^j}$ sub-vector of $\boldsymbol{z}$ containing the realization of the latent variable we are interested in, and $\boldsymbol{y}^i$ is a $n_{\boldsymbol{y}^i}$ sub-vector of $\boldsymbol{y}$ containing the observations of the variable or variables whose information content we want to assess. The required quantities, i.e. entropy (2.1) and mutual information (2.4), are obtained in exactly the same way as before, replacing the joint distributions with their marginal counterparts. Furthermore, now we can distinguish between conditional and unconditional information gains from knowing $\boldsymbol{y}^i$ with respect to $\boldsymbol{z}^j$. The unconditional information gain is given as before by $IG_{\boldsymbol{z}^j}(\boldsymbol{y}^i)$ and measures the reduction in uncertainty about $\boldsymbol{z}^j$ due to observing $\boldsymbol{y}^i$ relative to observing no data at all. It is often more interesting to know the marginal contribution of $\boldsymbol{y}^i$, given the information about $\boldsymbol{z}^j$ contained in other observed variables. One way to define a conditional information gain of $\boldsymbol{y}^i$ with respect to $\boldsymbol{z}^j$, given $\bar{\boldsymbol{y}}^i := \boldsymbol{y} \setminus \boldsymbol{y}^i$ is to replace the mutual information $I(\boldsymbol{y}^i, \boldsymbol{z}^j)$ in (2.10) with the conditional mutual information $I(\boldsymbol{y}^i, \boldsymbol{z}^j | \bar{\boldsymbol{y}}^i) = H(\boldsymbol{z}^j | \bar{\boldsymbol{y}}^i) - H(\boldsymbol{z}^j | \boldsymbol{y})$; this would tell us how much of the uncertainty about $\boldsymbol{z}^j$ that remains after $\bar{\boldsymbol{y}}^i$ is observed is removed by observing also $\boldsymbol{y}^i$.[9] Note, however, that the gains would be relative to the conditional uncertainty about $\boldsymbol{z}^j$ given $\bar{\boldsymbol{y}}^i$. Therefore,

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[9]The notation $A = B \setminus C$ is used to define A as the subset of B that excludes the set C.

that measure is not comparable to $\text{IG}_{\boldsymbol{z}^j}(\boldsymbol{y}^i)$ in (2.10), which is in terms of percent of the unconditional uncertainty about $\boldsymbol{z}^j$. A conditional measure which is comparable to (2.8) in the Gaussian case can be defined as

$$\text{IG}_{\boldsymbol{z}^j}(\boldsymbol{y}^i|\overline{\boldsymbol{y}}^i) = \left(\frac{|\boldsymbol{\Sigma}_{\boldsymbol{z}^j|\overline{\boldsymbol{y}}^i}|^{1/n_{\boldsymbol{z}^j}} - |\boldsymbol{\Sigma}_{\boldsymbol{z}^j|\boldsymbol{y}}|^{1/n_{\boldsymbol{z}^j}}}{|\boldsymbol{\Sigma}_{\boldsymbol{z}^j}|^{1/n_{\boldsymbol{z}^j}}} \right) 100. \tag{2.11}$$

The interpretation of $\text{IG}_{\boldsymbol{z}^j}(\boldsymbol{y}^i|\overline{\boldsymbol{y}}^i)$ is the following: it shows the amount of uncertainty about $\boldsymbol{z}^j$ left after observing $\overline{\boldsymbol{y}}^i$ that is removed by observing also $\boldsymbol{y}^i$, as a percent of the unconditional uncertainty about $\boldsymbol{z}^j$. As before, for non-Gaussian distributions the (conditional) effective variances are replaced with the respective (conditional) entropy powers.

Even though the information gain measures in (2.8) and (2.11) are defined with respect to the T-dimensional vector of all realizations of the latent variable, we can similarly measure information gains with respect to particular subsets of realizations. For instance, we can define information gains with respect to individual realizations of the latent variable. In that case we use the marginal conditional distributions of the realizations. When the distribution is Gaussian, the conditional variances which appear in the information gain measures can can be obtained by running the Kalman smoother for different combinations of observed variables. Note, however, that the Kalman smoother only provides the diagonal elements of the conditional covariance matrices in (2.8) and (2.11). In general, these matrices have non-zero off-diagonal entries since the elements of $\boldsymbol{z}^j$ are conditionally dependent, even if the latent variable itself is an i.i.d. process.

The use of the information gain measures presented above can be summarized as follows: the unconditional measure (2.8) tells us how informative a set of observed variables is as a whole with respect to a given unobserved endogenous variable or exogenous shock. If $\text{IG}_{\boldsymbol{z}^j}(\boldsymbol{y}) \approx 0$ the information about $\boldsymbol{z}^j$ after observing $\boldsymbol{y}$ is nearly the same as prior to observing any data. For instance, saying that standard macroeconomic variables are not very informative about news shocks can be expressed as the unconditional information gains of such variables (as a set) with respect to news shocks being close to zero. On the other hand, if $\text{IG}_{\boldsymbol{z}^j}(\boldsymbol{y}) = 100$, observing $\boldsymbol{y}$ is sufficient to completely recover the realizations of the variable represented by $\boldsymbol{z}^j$. The conditional information gain measure (2.11) can be used to determine how much of the overall information content of $\boldsymbol{y}$ is contributed by each individual variable or subsets of variables. Therefore, the

claim that asset prices contribute a lot of additional information about news shocks can be verified by showing that the information gains of asset prices with respect to news shocks conditional on standard macroeconomic variables are large. In general, by comparing conditional information gains, one could rank observed variables in terms of their relative informativeness with respect to each latent variable. In the remainder of this section I discuss how to measure the relative importance of the observed variables with respect to the unknown parameters of the model.

2.2 Information about parameters

The purpose of this section is to evaluate the contribution of each observed variable in terms of the amount of information they provide about the parameter vector $\boldsymbol{\theta}$ as a whole and each individual parameter. I approach this as a missing data problem (see e.g. Dempster et al. (1977) and Palm and Nijman (1984)), and compare the expected information content of complete and incomplete samples. In the present context a complete sample means observing an $n_{\boldsymbol{y}_T}$ vector $\boldsymbol{y}_T$, while an incomplete sample means observing $\bar{\boldsymbol{y}}_T^i$, that is, all variables except the one indexed by i. Intuitively, the distribution of the incomplete sample is less informative than the distribution of complete sample in the sense that the uncertainty about $\boldsymbol{\theta}$ is reduced to a lesser extent as a consequence of observing $\bar{\boldsymbol{y}}_T^i$ compared to observing $\boldsymbol{y}_T$ (see Rao (2002, p.331)).[10] A standard measure of the expected amount of information contained in a distribution is the Fisher information matrix (FIM). Asymptotically, i.e. as T tends to infinity, the inverse of the FIM is equal to the covariance matrix of the distribution of the ML estimator of $\boldsymbol{\theta}$. Hence, the expected loss of information can be measured by comparing the asymptotic variances of MLE using complete and incomplete samples. Furthermore, by the Cramér-Rao theorem the inverse of FIM is a lower bound on the covariance matrix of any unbiased estimator of $\boldsymbol{\theta}$. Thus, the loss of information can also be assessed as a function of the sample size, by measuring the differences between Cramér-Rao lower bounds with complete and incomplete samples.

For consistency with the previous section, I evaluate the contributions of observables in terms of efficiency gains, i.e. the reduction in expected estimation uncertainty about parameters when a variable (or a group of variables) is observed, relative to when it is not observed. Specifically, let $\boldsymbol{\Omega}_{\boldsymbol{\theta}}(\boldsymbol{y})$ and $\boldsymbol{\Omega}_{\boldsymbol{\theta}}(\bar{\boldsymbol{y}}^i)$ be the (asymptotic or finite-sample)

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[10]See Meng and Xie (2014) for an interesting discussion of why this is true for likelihood based estimation approaches, but not in general.

CRLBs for $\boldsymbol{\theta}$ associated with the complete and incomplete samples. Note that, for large T, the MLE of $\boldsymbol{\theta}$ is approximately gaussian random vector with mean equal to the true value of $\boldsymbol{\theta}$, and covariance matrix given by the CRLB. Hence, $|\boldsymbol{\Omega}_{\boldsymbol{\theta}}|^{1/n_{\boldsymbol{\theta}}}$ can be interpreted as the large-sample approximation of the entropy power of the MLE of $\boldsymbol{\theta}$. Following the discussion in the previous section, I define the efficiency gain with respect to $\boldsymbol{\theta}$ from observing $\boldsymbol{y}^i$ relative to observing $\bar{\boldsymbol{y}}^i$ as follows:

$$
\mathrm{EG}_{\boldsymbol{\theta}}(\boldsymbol{y}^i|\bar{\boldsymbol{y}}^i) = \left(\frac{|\boldsymbol{\Omega}_{\boldsymbol{\theta}}(\bar{\boldsymbol{y}}^i)|^{1/n_{\boldsymbol{\theta}}} - |\boldsymbol{\Omega}_{\boldsymbol{\theta}}(\boldsymbol{y})|^{1/n_{\boldsymbol{\theta}}}}{|\boldsymbol{\Omega}_{\boldsymbol{\theta}}(\bar{\boldsymbol{y}}^i)|^{1/n_{\boldsymbol{\theta}}}} \right) 100. \tag{2.12}
$$

The interpretation is similar to that of the information gains in the previous section. $\mathrm{EG}_{\boldsymbol{\theta}}(\boldsymbol{y}^i|\bar{\boldsymbol{y}}^i)$ shows the increase in (asymptotic) efficiency of the MLE of $\boldsymbol{\theta}$ due to observing $\boldsymbol{y}^i$ as a percent of the estimation efficiency when only $\bar{\boldsymbol{y}}^i$ is observed. I use *efficiency gain* instead of *information gain* to emphasize the fact that, unlike the previous section, the gains here are in terms of the uncertainty associated with the distribution of the estimator of $\boldsymbol{\theta}$, instead of the parameter itself, which is non-random.

Wei (1978a,b) uses a similar measure to assess the information loss due to aggregation of time series. The only difference is that he does not exponentiate the determinants of the asymptotic covariance matrices of MLE for aggregated and disaggregated samples. As explained earlier, the measure in (2.12) has the advantage of being comparable for vectors of different sizes. In particular, suppose we are interested in the marginal contribution of information from a variable with respect to individual parameters. Let $\boldsymbol{\Omega}^{k,k}$ be the k-th diagonal element of $\boldsymbol{\Omega}^{k,k}$, i.e. the CRLB for θ_k. Then, the efficiency gain with respect to θ_k from observing $\boldsymbol{y}^i$ is given by

$$
\mathrm{EG}_{\theta_k}(\boldsymbol{y}^i|\bar{\boldsymbol{y}}^i) = \left(\frac{\boldsymbol{\Omega}_{\boldsymbol{\theta}}^{k,k}(\bar{\boldsymbol{y}}^i) - \boldsymbol{\Omega}_{\boldsymbol{\theta}}^{k,k}(\boldsymbol{y})}{\boldsymbol{\Omega}_{\boldsymbol{\theta}}^{k,k}(\bar{\boldsymbol{y}}^i)} \right) 100. \tag{2.13}
$$

An equivalent measure, formulated in terms of efficiency loss instead of efficiency gain, is used in Palm and Nijman (1984) to assess the loss of efficiency with respect to individual parameters due to missing observations in dynamic regression models. More broadly, FIM-based criteria similar to (2.12) and (2.13) are widely used in the experiment design literature to select an optimal design, i.e. a design which maximizes, according to a given criterion, the amount of information that an experimenter can expect to learn about the parameters through an experiment (see e.g. Silvey (1980) and Pronzato and Pázman (2013)).

3 Asset prices and news shocks

This section evaluates the contribution of information by asset price variables in DSGE models containing news shocks. In particular, I am interested in validity of the following two claims: (1) standard macroeconomic variables are uninformative about news shocks; and (2) asset prices contribute a lot of information about news shocks. Clearly it is not possible to give a single general answer as to whether these statements are true or not under all circumstances. Instead, the main purpose here is to demonstrate how the measures from Section 2 can be used to study the information properties of observables in the context of a particular environment. I consider two versions of the standard real business cycle model augmented with real rigidities in consumption, investment, capital utilization, and wage setting. The first version is taken from Schmitt-Grohé and Uribe (2012) (SGU henceforth) who estimate it without asset price data. The second version is from Avdjiev (2016) and differs from the SGU specification mainly in the way news shocks are introduced into the model and in the use of asset price data for estimation. In what follows, I first outline the main features of each model, and then apply the information measures presented in Section 2 to assess the contribution of information by asset prices with respect to news shocks in these models.

3.1 Schmitt-Grohé and Uribe (2012) model

The model economy is populated by a continuum of identical agents each maximizing the following lifetime utility function

$$\mathrm{E}_0 \sum_{t=0}^{\infty} \beta^t \zeta_t \frac{\left[C_t - bC_{t-1} - \psi H_t^\theta S_t\right]^{1-\sigma} - 1}{1 - \sigma}, \tag{3.1}$$

where ζ_t is a preference shock, C_t is consumption, H_t is hours worked, and S_t is a geometric average of past habit-adjusted consumption: $S_t = (C_t - bC_{t-1})^\gamma S_{t-1}^{1-\gamma}$. The household budget constraint is given by

$$C_t + A_t I_t + T_t = W_t H_t + r_t u_t K_t + P_t, \tag{3.2}$$

where A_t is a non-stationary investment specific productivity growing at rate μ_t^a. The variable T_t denotes lump-sum taxes, W_t is the wage rate, r_t is rental rate of capital, u_t is capacity utilization, K_t is capital stock, and P_t denotes profit. The law of motion for

capital stock is

$$K_{t+1} = (1 - \delta(u_t))K_t + z_t^I I_t \left[1 - \frac{\kappa}{2}\left(\frac{I_t}{I_{t-1}} - \mu^I\right)\right], \tag{3.3}$$

where I_t is investment, δ is the rate of depreciation – an increasing function of the rate of capacity utilization u_t, κ is a parameter that determines the convexity of the investment adjustment cost function, μ^I is is the steady state growth rate of investment, and z_t^I is a stationary investment specific productivity shock.

Final good Y_t is produced with the following production function:

$$Y_t = z_t(u_t K_t)^{\alpha_k}(X_t H_t)^{\alpha_h}(X_t L)^{1-\alpha_k-\alpha_h}, \tag{3.4}$$

where z_t is a stationary neutral productivity shock, L is a fixed factor of production,[11] and X_t is a non-stationary neutral productivity growing at rate μ_t^x.

The labor input H_t, which is used by final-good-producing firms, is obtained by combining differentiated labor services H_{jt} supplied by monopolistically competitive labor unions,

$$H_t = \left[\int_0^1 H_{jt}^{\frac{1}{1+\mu_t}}dj\right]^{1+\mu_t}, \tag{3.5}$$

where μ_t is a wage markup shock with steady state value $\mu > 1$.

Each period the government spends an amount G_t, financed with lump-sum taxes. G_t is determined exogenously and is assumed to grow at rate X_t^G, defined as a smoothed version of the trend in Y_t, given by $X_t^Y = X_t A_t^{\alpha_k/(\alpha_k-1)}$.

Each of the seven shocks is driven by three independent innovations, two anticipated and one unanticipated. More precisely, the process governing shock x_t for $x = \mu^a, \mu^x, z^I, z, \mu, g, \zeta$ is given by

$$\ln(x_t/x) = \rho_x \ln(x_{t-1}/x) + \sigma_x^0 \varepsilon_{x,t}^0 + \sigma_x^4 \varepsilon_{x,t-4}^4 + \sigma_x^8 \varepsilon_{x,t-8}^8, \tag{3.6}$$

where $\varepsilon_{x,t}^j$ for $j = 0, 4, 8$ are independent standard normal random variables. The anticipated innovations $\varepsilon_{x,t-4}^4$ and $\varepsilon_{x,t-8}^8$ are known to agents in periods $t-4$ and $t-8$, respectively. Thus, they are interpreted as news shocks.

SGU report results based on estimation of the model using quarterly data on seven

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[11]The fixed factor of production generates decreasing returns to scale in the two variable factors of production K_t and H_t. As shown by Jaimovich and Rebelo (2009) this allows for a positive response of the value of the firm to future expected increases in productivity.

macroeconomic series: the growth rate of per capita real GDP ($y_t := \triangle \ln Y_t$) contaminated with a measurement error, the growth rates of real consumption ($c_t := 100 \triangle \ln C_t$), real investment ($i_t := 100 \triangle \ln A_t I_t$), real government expenditure ($g_t := 100 \triangle \ln G_t$), and hours ($h_t := 100 \triangle \ln H_t$), and the growth rates of the relative price of investment ($a_t := 100 \triangle \ln A_t$) and of total factor productivity ($tfp_t := 100 \triangle \ln TFP_t$).[12]

In addition to these variables, the model makes predictions about the behavior of two asset price variables: the value of the firm and the risk-free real interest rate. The value of the firm V^F can be computed as

$$V_t^F = Y_t - W_t H_t - A_t I_t + \beta E_t \frac{\Lambda_{t+1}}{\Lambda_t} V_{t+1}^F, \tag{3.7}$$

where Λ_t is the Lagrange multiplier associated with the household's budget constraint. The risk-free real interest rate is given by

$$R_t = \frac{1}{\beta} \frac{\Lambda_t}{E_t \Lambda_{t+1}}. \tag{3.8}$$

In estimation, the value of the firm can be matched to stock price data. In particular, $v_t^f := \triangle \ln V_t^F$ can be represented with the growth rate of the real per capita value of the stock market. Similarly, data on $r_t := \log R_t$ can be obtained by deflating the nominal rate on the three-month Treasury bill by the inflation rate implied by the GDP deflator.

The main reason SGU give for not using stock price data in the estimation is that models such as the one described here are not well suited for explaining the behavior of stock prices. Avdjiev (2016), whose model I consider in Section 3.2, uses data on both v^f and r, but introduces measurement errors in the series in order to account for discrepancies between the model variables and their empirical counterparts. His argument is that, even though imperfectly measured, the asset price implications of the model contain useful information about news shocks that standard macroeconomic variables alone do not.

Here, I abstract from the issue of whether v^f and r have adequate empirical counterparts. The question I am interested in is whether observing these model variables, if such data were available, would provide a significant amount of additional information with respect to news shocks. This question is addressed next.

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[12]The growth rate of total factor productivity in the model is given by $tfp_t = 100 \left(\triangle \ln z_t + (1 - \alpha_k) \ln \mu_t^x \right)$.

Table 1: Information content of asset prices: innovations

	innovation	IG($\bar{\boldsymbol{y}}$)	IG($v^f, r\|\bar{\boldsymbol{y}}$)	IG($v^f\|\bar{\boldsymbol{y}}$)	IG($r\|\bar{\boldsymbol{y}}$)	IG(v^f)	IG(r)
$\varepsilon_{\mu^a}^0$	non-stat. investment-specific prod.	26.3	3.7	3.5	0.1	0.2	0.1
$\varepsilon_{\mu^a}^4$	non-stat. investment-specific prod. 4q	38.4	3.2	3.0	0.3	0.1	0.1
$\varepsilon_{\mu^a}^8$	non-stat. investment-specific prod. 8q	34.0	3.3	3.1	0.3	0.1	0.1
$\varepsilon_{\mu^x}^0$	non-stat. neutral prod.	26.9	19.9	14.6	4.3	18.4	2.2
$\varepsilon_{\mu^x}^4$	non-stat. neutral prod. 4q	2.1	8.6	2.3	5.0	0.6	1.4
$\varepsilon_{\mu^x}^8$	non-stat. neutral prod. 8q	2.3	8.9	2.0	5.6	0.6	1.6
$\varepsilon_{z^I}^0$	stat. investment-specific prod.	84.0	9.5	7.0	5.0	0.9	0.9
$\varepsilon_{z^I}^4$	stat. investment-specific prod. 4q	10.3	23.3	17.8	8.3	0.8	1.7
$\varepsilon_{z^I}^8$	stat. investment-specific prod. 8q	16.5	33.3	26.7	11.1	1.6	2.8
ε_z^0	stat. neutral prod.	71.7	6.5	2.6	3.3	42.2	8.5
ε_z^4	stat. neutral prod. 4q	2.6	11.9	1.5	8.9	0.8	2.3
ε_z^8	stat. neutral prod. 8q	2.7	12.0	1.5	9.0	0.8	2.3
ε_μ^0	wage markup	9.7	27.4	1.9	21.6	3.4	0.6
ε_μ^4	wage markup 4q	52.9	5.0	1.7	3.5	15.1	42.3
ε_μ^8	wage markup 8q	34.4	4.6	2.3	2.5	9.8	27.5
ε_g^0	government spending	28.8	2.6	0.3	2.0	0.7	0.1
ε_g^4	government spending 4q	47.9	1.9	0.5	1.1	0.6	1.8
ε_g^8	government spending 8q	18.6	0.9	0.3	0.5	0.3	0.7
ε_ζ^0	preference	16.3	5.3	1.6	3.2	0.6	0.1
ε_ζ^4	preference 4q	16.0	1.3	0.8	0.2	0.3	0.9
ε_ζ^8	preference 8q	60.7	2.7	1.2	0.7	1.2	3.4

Note: $\bar{\boldsymbol{y}}$ contains all observed variables ($\boldsymbol{y}$) except asset prices (v^f and r). The information gain $\text{IG}_\varepsilon(\boldsymbol{x})$ measures the reduction in uncertainty about variable ε due to observing variable $\boldsymbol{x}$, in per cent of the prior (unconditional) uncertainty. The conditional information gain $\text{IG}_\varepsilon(\boldsymbol{x}|\boldsymbol{z}) = \text{IG}_\varepsilon(\boldsymbol{x}, \boldsymbol{z}) - \text{IG}_\varepsilon(\boldsymbol{z})$ measures the additional reduction in uncertainty from observing $\boldsymbol{x}$ given that $\boldsymbol{z}$ is observed.

3.1.1 Information about news shocks

Following the notation in Section 2, let $\boldsymbol{y}$ be a vector collecting the observations of all observable variables (including v^f and r), and $\bar{\boldsymbol{y}}$ be the vector of observations of the variables used in the baseline estimation of SGU, i.e. $\bar{\boldsymbol{y}} = \boldsymbol{y} \setminus (v^f, r)$. Note that $\boldsymbol{y}$ is a $T \times 9$ dimensional vector, and $\bar{\boldsymbol{y}}$ is a $T \times 7$ dimensional vector. The purpose of this section is to evaluate the information gains from observing v^f, r, or both, with respect to news shocks, which in this model are represented by the anticipated innovations to the seven fundamental shocks. There are 14 such innovations, each one of which is a T dimensional vector. I set $T = 207$, which is the sample size in SGU.

SGU solve the model by log-linear approximation of the equilibrium conditions around steady state. The linearity of the solution together with the assumption that the

structural innovations and the measurement error in output growth are Gaussian, implies that the joint distribution of (any subset of) the innovations, shocks, state and observed variables is also Gaussian. This fact is used in SGU to compute the likelihood function required for estimation of the model parameters with classical and Bayesian methods. In addition, it implies that the information gains measures discussed in Section 2.1 can be computed analytically for a given set of parameter values. In what follows I parameterize the model using the maximum likelihood estimates reported in Schmitt-Grohé and Uribe (2012) (see Table 8 in the Appendix). As I explain in more details at the end of this section, the main conclusions do not change in any significant way if the mean or the mode of the posterior distribution are used instead.

Table 1 presents the results for all innovations – anticipated and unanticipated. The first two columns show the unconditional gains from observing $\bar{\boldsymbol{y}}$, and the additional gains from observing both v^f and r, conditional on $\bar{\boldsymbol{y}}$ being observed. Note that the information gains from observing all nine variables are given by $\mathrm{IG}_\varepsilon(\boldsymbol{y}) = \mathrm{IG}_\varepsilon(\bar{\boldsymbol{y}}) + \mathrm{IG}_\varepsilon(v^f, r|\bar{\boldsymbol{y}})$. The results show that none of the innovations, anticipated or unanticipated, can be fully recovered from the observed variables, even when v^f and r are among them. The largest reduction of uncertainty is with respect to the unanticipated stationary investment-specific productivity innovations (ε_{zI}^0) – by about 94%, and the unanticipated stationary neutral productivity innovations (ε_z^0) – by about 78%. In terms of anticipated innovations, i.e. news shocks, the information gains are largest with respect to the 8–quarter ahead preference shock – about 63%, and the 4–quarter ahead wage markup shock – about 58%. However, the contribution of information by asset prices with respect to these shocks is fairly modest. The largest gains due to observing v^f and r are with respect to news about the stationary investment-specific productivity shocks. They are about 23% with respect to ε_{zI}^4 and 33% with respect to ε_{zI}^8. Other news shocks for which the contribution of asset prices is non-trivial are the stationary and non-stationary neutral productivity shocks. The gains are about 12% and 9%, respectively.

The relative contributions of the two asset price variables can seen from the third and fourth columns of the table, which report the additional gains from observing either v^f or r, conditional on $\bar{\boldsymbol{y}}$ being observed. Even though both asset price variables contribute a substantial amount of information about ε_{zI}^4 and ε_{zI}^8, the gains from observing v^f are significantly larger. At the same time, r is the more informative of the two variables with respect to the news components of the stationary and non-stationary neutral productivity shocks.

The last two columns show the information gains from observing either v^f or r, relative to having no data at all. Interestingly, the gains are very small with respect to most news shocks, including the stationary investment-specific productivity shocks and the neutral productivity shocks. This means that almost all of the information which asset prices contribute with respect to these shocks comes from the interactions of v^f and r with variables in $\bar{\boldsymbol{y}}$. That is, the information comes from cross-moments of asset prices and macro variables rather than the own moments of asset prices. Note that the opposite is true in the case of the news components in the wage markup shock. The unconditional gains from observing v^f or r are much larger than the conditional gains. This implies that most of the information provided by either one of the asset price variables is also contained in other observed variables.[13]

The results in Table 1 raise the question of how v^f and r compare to other observables in terms of the amount of information they provide about news shocks. To answer this question, I compute conditional information gains for each variable in $\boldsymbol{y}$. That is, I evaluate $\mathrm{IG}_\varepsilon(x|\boldsymbol{y}^x)$ where x is one of the nine observables, and $\boldsymbol{y}^x$ contains all observables (including v^f and r) except x. The results are shown in Figure 1. Note that hours worked and TFP each contribute more information with respect to the stationary investment-specific productivity news shocks compared to v^f or r. The relative price of investment is by far the most informative variable with respect to the news components in the non-stationary investment-specific productivity shocks, while government expenditure and consumption are, respectively, the most informative variables about government spending and preference news shocks. The anticipated innovations to the stationary neutral productivity shocks are the only news shocks for which an asset price variable, specifically the risk-free rate, contributes significantly more information than any other variable.

An important conclusion which emerges from Table 1 and Figure 1 is that the marginal contribution of information by a variable depends on which other variables are observed. Furthermore, in some cases the contribution is enhanced due to presence of other variables, while in other cases it is diminished. For instance, as we saw in Table 1, v^f alone provides very little information about $\varepsilon_{z^I}^4$ and $\varepsilon_{z^I}^8$. Conditional on observing all seven macro variables, however, the contribution of v^f is substantial. The opposite is true with respect to $\varepsilon_{\mu^x}^0$ and ε_z^0. This suggests that there exists a degree of positive

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[13]The unanticipated innovation to the non-stationary neutral productivity shock $\varepsilon_{\mu^x}^0$ is an example of a third possibility – where the information gains from observing v^f are relatively large, both conditionally and unconditionally.

	y	c	i	h	g	a	tfp	v^f	r
$\varepsilon_{\mu^a}^0$	0	2	2	3	2	21	4	4	0
$\varepsilon_{\mu^a}^4$	0	2	1	3	2	32	3	3	0
$\varepsilon_{\mu^a}^8$	0	2	1	3	2	30	3	3	0
$\varepsilon_{\mu^x}^0$	0	8	6	8	7	5	10	16	5
$\varepsilon_{\mu^x}^4$	0	1	1	1	1	0	3	4	6
$\varepsilon_{\mu^x}^8$	0	1	1	1	1	0	2	3	7
$\varepsilon_{z^I}^0$	0	6	37	9	5	2	8	5	2
$\varepsilon_{z^I}^4$	0	15	8	22	13	2	20	15	6
$\varepsilon_{z^I}^8$	0	22	13	32	19	6	29	22	7
ε_z^0	0	3	2	3	2	1	6	3	4
ε_z^4	0	0	0	0	0	0	2	3	10
ε_z^8	0	0	0	0	0	0	2	3	10
ε_μ^0	0	2	2	3	1	0	2	6	26
ε_μ^4	0	1	1	3	1	0	2	1	3
ε_μ^8	0	1	1	3	1	0	2	2	2
ε_g^0	0	0	0	0	8	0	0	1	2
ε_g^4	0	0	0	0	14	0	0	1	1
ε_g^8	0	0	0	0	6	0	0	0	1
ε_ζ^0	0	3	0	0	0	0	0	2	4
ε_ζ^4	0	3	0	0	0	0	0	1	1
ε_ζ^8	0	11	0	0	0	0	0	2	2
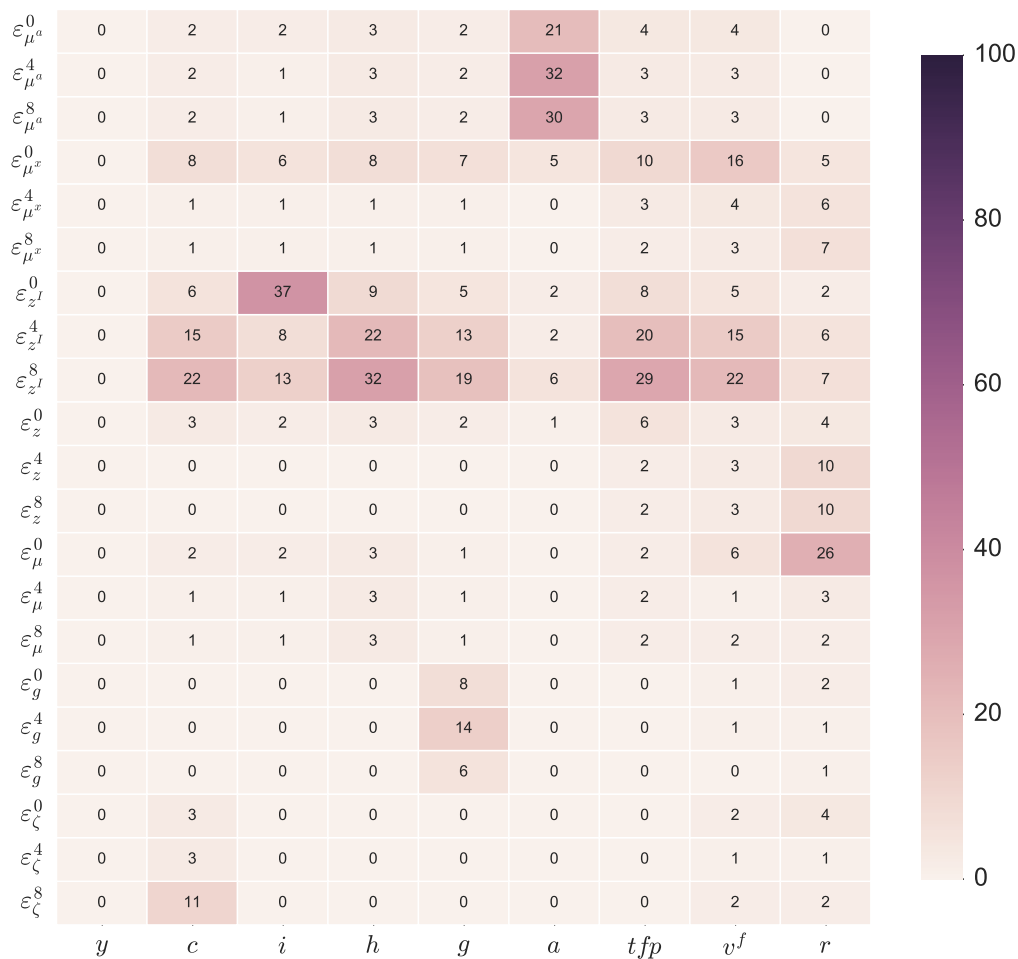
Figure 1: Conditional information gains at MLE of SGU.

information complementarity between v^f and (some of the) macro variables in the first case, and negative complementarity, or information redundancy, in the second. To find out how v^f interacts with each one of the macro variables, it is helpful to define a measure of (conditional) information complementarity between two variables. Specifically, let x be a member of $\bar{\boldsymbol{y}}$ and $\bar{\boldsymbol{y}}^x := \bar{\boldsymbol{y}} \setminus x$. Then, the conditional information complementarity with respect to variable ε between v^f and x can be defined as:

$$\mathrm{IC}_\varepsilon(v^f, x | \bar{\boldsymbol{y}}^x) = \frac{\mathrm{IG}_\varepsilon(v^f, x | \bar{\boldsymbol{y}}^x)}{\mathrm{IG}_\varepsilon(v^f | \bar{\boldsymbol{y}}^x) + \mathrm{IG}_\varepsilon(x | \bar{\boldsymbol{y}}^x)} - 1. \tag{3.9}$$

Negative values indicate negative complementarity, or information redundancy, between

v^f and x, and positive values indicate positive complementarity between the two variables. Since the information gain is non-negative, we have $\mathrm{IC}_\varepsilon(v^f, x|\bar{\boldsymbol{y}}^x) \geq -1/2$, with equality when v^f and x are (conditionally on $\bar{\boldsymbol{y}}^x$) functionally dependent, in which case $\mathrm{IG}_\varepsilon(v^f, x|\bar{\boldsymbol{y}}^x) = \mathrm{IG}_\varepsilon(v^f|\bar{\boldsymbol{y}}^x) = \mathrm{IG}_\varepsilon(x|\bar{\boldsymbol{y}}^x)$.[14] A lack of information complementarity, i.e. $\mathrm{IC}_\varepsilon(v^f, x|\bar{\boldsymbol{y}}^x) = 0$ could occur if v^f and x are (conditionally on $\bar{\boldsymbol{y}}^x$) independent, and hence $\mathrm{IG}_\varepsilon(v^f, x|\bar{\boldsymbol{y}}^x) = \mathrm{IG}_\varepsilon(v^f|\bar{\boldsymbol{y}}^x) + \mathrm{IG}_\varepsilon(x|\bar{\boldsymbol{y}}^x)$. Note that instead of $\bar{\boldsymbol{y}}^x$ in (3.9) the conditioning could be with respect to any other set of variables, including the empty set which would show the unconditional complementarity between v^f and x.

Using Table 1, we can determine the degree of complementarity between v^f and r, conditionally on the seven macro variables. There is a positive complementarity with respect to the preference shock, the stationary and non-stationary neutral productivity shocks, and the government spending shock. At the same time there is a negative complementarity, or redundancy of information, with respect to the stationary and non-stationary investment-specific news shocks, and wage markup shock. Overall, the degree of complementarity, both positive and negative, is relatively week.

Figures 6 - 9 in the Appendix show results for conditional and unconditional information complementarity between v^f and r and each one of the macro variables. The main findings can be summarized as follows: (1) both v^f and r display very strong conditional complementarity with h and tfp, and relatively weaker, but still significant complementarity with c; (2) The complementarity is positive with respect to the news components in the stationary and non-stationary investment specific shocks, and, in the case of h and c, the stationary and non-stationary neutral productivity shocks. The complementarity is negative with respect to news about the wage markup and preference shocks; (3) The magnitude and even the sign of the information complementarity may change depending on the conditioning variables. For instance, unconditionally, v^f is strongly complementary only with tfp, and the complementarity is positive with respect to all news shocks except the two neutral productivity news shocks. r, on the other hand, is unconditionally strongly complementary primarily with h, and the complementarity is positive with respect to all news except the wage markup news shocks; (4) Conditionally, there is zero information complementarity between either v^f or r, on one hand, and y, on the other.

As noted earlier, it is not possible to recover without error the 21 anticipated and

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[14]Note that $\mathrm{IG}_\varepsilon(v^f, x|\bar{\boldsymbol{y}}^x) \geq \max\left(\mathrm{IG}_\varepsilon(v^f|\bar{\boldsymbol{y}}^x), \mathrm{IG}_\varepsilon(x|\bar{\boldsymbol{y}}^x)\right)$ and $\mathrm{IG}_\varepsilon(v^f, x|\bar{\boldsymbol{y}}^x) = 0$ implies $\mathrm{IG}_\varepsilon(v^f|\bar{\boldsymbol{y}}^x) = \mathrm{IG}_\varepsilon(x|\bar{\boldsymbol{y}}^x) = 0$. In that case $\frac{\mathrm{IG}_\varepsilon(v^f, x|\bar{\boldsymbol{y}}^x)}{\mathrm{IG}_\varepsilon(v^f|\bar{\boldsymbol{y}}^x) + \mathrm{IG}_\varepsilon(x|\bar{\boldsymbol{y}}^x)} = \frac{0}{0}$, which is taken to be equal to 1.

Table 2: Information content of asset prices: shocks

	shock	IG($\bar{\boldsymbol{y}}$)	IG($v^f, r \vert \bar{\boldsymbol{y}}$)	IG($v^f \vert \bar{\boldsymbol{y}}$)	IG($r \vert \bar{\boldsymbol{y}}$)	IG(v^f)	IG(r)
μ^a	nonstationary investment-specific prod.	100.0	0.0	0.0	0.0	0.2	0.2
μ^x	nonstationary neutral prod.	30.8	16.8	12.2	4.1	19.2	2.6
z^I	stationary investment-specific prod.	86.4	11.0	10.6	2.5	2.1	2.9
z	stationary neutral prod.	76.5	5.8	4.1	1.5	43.7	8.8
μ	wage markup	98.2	1.4	0.8	1.0	28.7	68.1
g	government spending	98.8	0.3	0.2	0.1	1.5	1.9
ζ	preference	98.3	1.3	0.7	0.5	2.2	3.7

Note: see note to Table 1

unanticipated innovations from either 7 or 9 observed variables. In fact, in many cases the information gains are small, meaning that the posterior uncertainty remains very close to the prior uncertainty. There are, however, only 7 structural shocks and it is natural to expect that they are easier to recover than the innovations. This is indeed the case, as can be seen in Table 2, which shows results from the same analysis as in Table 1, now applied to the structural shocks. With 9 observed variables the information gains exceed 97% for 5 of the shocks. The two shocks for which the gains are relatively small are the non-stationary neutral productivity – around 48%, and the stationary neutral productivity – around 82% with 9 observed variables. The asset price variables provide a significant amount of additional information with respect to the non-stationary neutral productivity and the stationary investment-specific productivity shocks. Most of these gains are due to information in v^f. The information gains are 100% with respect to the non-stationary investment-specific productivity, meaning that the realizations of μ_t^a can be completely recovered from the observed variables. This is a consequence of the assumption that the technology which converts consumption into investment goods is linear. As a result, in equilibrium the growth rate of the relative price of investment is equal to non-stationary investment-specific productivity shock. Hence, observing the price of investment alone is sufficient to fully recover μ_t^a for all t. None of the other shocks can be fully recovered from the observed variable, although the information gains exceed 99% in the case of wage markup, government expenditures, and preference shocks.

3.1.2 Information about parameters

This section evaluates the information content of asset prices with respect to the news shock–related parameters in the model. It supplements the analysis in Schmitt-Grohé and Uribe (2012) who show that the parameters are identified from the second-order moments of the seven variables used in estimation.[15] It is clear that having additional observed variables would increase the amount of information. The purpose of the following analysis is to provide a quantitative assessment of the size of the gains from observing v^f, r, or both, and to compare them to the gains from other observables.

As discussed in Section 2.2, the information content of a variable (or a set of variables) x with respect to estimated parameters is measured in terms of efficiency gains, which are computed using the parameter CRLBs with and without x. The differences between the values of the bounds reflect the information content of the model-impled restrictions on the joint distribution of x and the other observables. Hence, parameters for which these restrictions are more informative will see a greater reduction in the values of their lower bounds, i.e. larger efficiency gains.

The results are presented in Table 3. As also discussed in Section 2.2, the gains are in terms of reduction in uncertainty as a per cent of the uncertainty conditional on observing $\bar{y}$. Overall, the efficiency gains are substantial, in the order of between 90% and 97% for parameters of news shocks when both v^f and r are included. The gains are smaller but still significant when only one of the asset price variables is observed, and tend to be larger if that variable is v^f. These results seem to suggest that asset prices are indeed very informative with respect to news shock–related parameters. However, this does not imply that v^f and r are more informative than other observables. To find out if they are, one has to compare the efficiency gains from observing asset prices to the gains from other variables. Figure 2 does that for each one of the nine variables in $\boldsymbol{y}$. Note that, unlike in Table 3, the efficiency gains are now relative to eight, not seven, observables. For instance, the gains from observing r are relative to observing all other variables, including v^f. As a result, they are generally much smaller than before, especially with respect to news shocks parameters. This means that once v^f is observed, r adds relatively little new information about these parameters. At the same time, the efficiency gains due to v^f remain substantial, although not as large as in Table 3.

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[15]Even though Schmitt-Grohé and Uribe (2012) de-mean the data, this does not result in loss of information since all parameters for which first-order moments are informative are assumed to be known, i.e. are calibrated and not estimated.

Table 3: Efficiency gains (%)

	parameter	v^f, r	v^f	r
θ	Frisch elasticity of labor supply	83	61	78
γ	wealth elasticity of labor supply	51	35	28
κ	investment adjustment cost	95	94	59
δ_2/δ_1	capacity utilization cost	99	97	88
b	habit in consumption	75	66	27
ρ_{xg}	government spending	34	17	20
ρ_z	AR stationary neutral productivity	85	66	67
ρ_{μ^a}	AR non-stationary investment-specific productivity	40	37	2
ρ_g	AR government spending	52	48	42
ρ_{μ^x}	AR non-stationary neutral productivity	87	72	60
ρ_μ	AR wage markup	77	69	14
ρ_ζ	AR preference	28	19	9
ρ_{z^I}	AR stationary investment-specific productivity	96	92	78
σ_z^0	std. stationary neutral productivity 0	87	59	83
σ_z^4	std. stationary neutral productivity 4	93	73	72
σ_z^8	std. stationary neutral productivity 8	90	73	64
$\sigma_{\mu^a}^0$	std. non-stationary investment-specific productivity 0	95	95	43
$\sigma_{\mu^a}^4$	std. non-stationary investment-specific productivity 4	97	96	74
$\sigma_{\mu^a}^8$	std. non-stationary investment-specific productivity 8	96	96	68
σ_g^0	std. government spending 0	97	80	95
σ_g^4	std. government spending 4	91	89	52
σ_g^8	std. government spending 8	91	89	55
$\sigma_{\mu^x}^0$	std. non-stationary neutral productivity 0	78	50	67
$\sigma_{\mu^x}^4$	std. non-stationary neutral productivity 4	94	78	71
$\sigma_{\mu^x}^8$	std. non-stationary neutral productivity 8	90	74	58
σ_μ^0	std. wage markup 0	99	70	97
σ_μ^4	std. wage markup 4	90	84	52
σ_μ^8	std. wage markup 8	90	85	48
σ_ζ^0	std. preference 0	98	89	97
σ_ζ^4	std. preference 4	90	88	39
σ_ζ^8	std. preference 8	91	88	50
$\sigma_{z^I}^0$	std. stationary investment-specific productivity 0	92	91	66
$\sigma_{z^I}^4$	std. stationary investment-specific productivity 4	96	93	81
$\sigma_{z^I}^8$	std. stationary investment-specific productivity 8	92	88	72

Note: The efficiency gain $\text{EG}_{\theta_i}(\boldsymbol{x}|\bar{\boldsymbol{y}})$, for (1) $\boldsymbol{x} = (v^f, r)$, (2) $\boldsymbol{x} = v^f$, or (3) $\boldsymbol{x} = r$, is defined as the reduction in the value of CRLB for θ_i when all variables are observed, as a per cent of the value of the CRLB when all variables except those in $\boldsymbol{x}$ are observed.

Comparing the results across all variables shows that h and tfp tend to be as informative with respect to news shocks–related parameters as v^f and r. Only in the cases of the neutral productivity shocks – both stationary and non-stationary, are the asset price variables the most informative ones, with tfp being close next best. Therefore, we can conclude that, although very informative about most model parameters, the two asset price variables in this model are not in any way uniquely important for the identification of news shocks–related parameters.
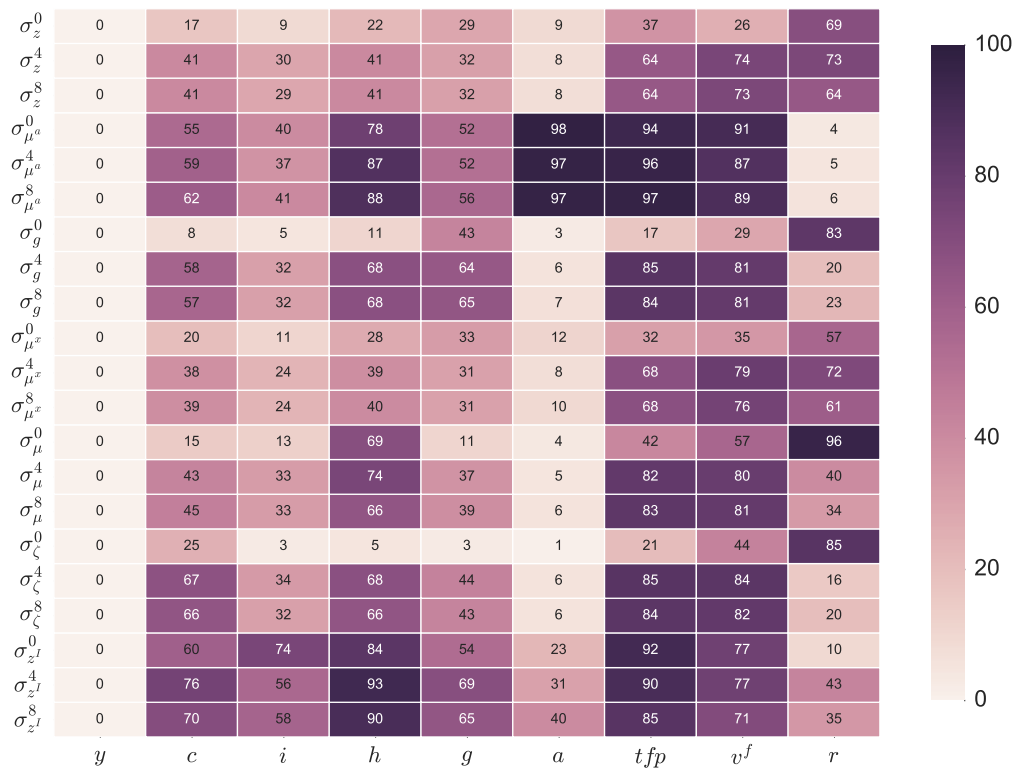
	y	c	i	h	g	a	tfp	v^f	r
σ_z^0	0	17	9	22	29	9	37	26	69
σ_z^4	0	41	30	41	32	8	64	74	73
σ_z^8	0	41	29	41	32	8	64	73	64
$\sigma_{\mu^a}^0$	0	55	40	78	52	98	94	91	4
$\sigma_{\mu^a}^4$	0	59	37	87	52	97	96	87	5
$\sigma_{\mu^a}^8$	0	62	41	88	56	97	97	89	6
σ_g^0	0	8	5	11	43	3	17	29	83
σ_g^4	0	58	32	68	64	6	85	81	20
σ_g^8	0	57	32	68	65	7	84	81	23
$\sigma_{\mu^x}^0$	0	20	11	28	33	12	32	35	57
$\sigma_{\mu^x}^4$	0	38	24	39	31	8	68	79	72
$\sigma_{\mu^x}^8$	0	39	24	40	31	10	68	76	61
σ_μ^0	0	15	13	69	11	4	42	57	96
σ_μ^4	0	43	33	74	37	5	82	80	40
σ_μ^8	0	45	33	66	39	6	83	81	34
σ_ζ^0	0	25	3	5	3	1	21	44	85
σ_ζ^4	0	67	34	68	44	6	85	84	16
σ_ζ^8	0	66	32	66	43	6	84	82	20
$\sigma_{z^I}^0$	0	60	74	84	54	23	92	77	10
$\sigma_{z^I}^4$	0	76	56	93	69	31	90	77	43
$\sigma_{z^I}^8$	0	70	58	90	65	40	85	71	35

Figure 2: Efficiency gains at MLE of SGU.

Redundancy of output. An interesting result that emerged from the above analysis is that output growth data does not contribute any additional information with respect to either latent variables (i.e. innovations and shocks) or the free parameters in the model. In other words y is redundant given the other observed variables. In fact, it can be shown that, as long as the growth rates of consumption, investment and government expenditures are observed, the output growth variable is only informative with respect to

one parameter – the standard deviation of the measurement error $\sigma_{g^y}^{me}$. Two assumptions in SGU are responsible for this result: (1) several model parameters are known, and (2) output is the only variable observed with measurement error. Relaxing either one of these assumptions would make output growth informative. For more details, see Iskrev (2015).

To summarize, the analysis in this section shows that the two asset price variables in the SGU model are not particularly informative about either the realizations of news shocks or parameters related to news shocks. Macroeconomic aggregates, such as hours worked, TFP, or the relative price of investment, are about as informative with respect to news shocks as are the value of the firm (stock prices) or the risk-free interest rate. Needless to say, this is a conclusion about the properties of the estimated SGU model. Making any changes that affect the way news shocks propagate throughout the economy could alter the results. In particular, different values of the structural parameters could imply a much larger information content of asset prices. As already mentioned, using the median of the posterior distribution reported in SGU does not change the main conclusions regarding the informativeness of v^f and r. This can be seen in Figure 10 in the Appendix, which shows conditional information gains for all variables at the posterior median. In addition, Figures 11 and 12 do the same for two other parameterizations of the SGU model (see also Table 10). The first one comes from Herbst and Schorfheide (2014) who estimate the same model with the same set of observables as SGU using a different (and arguably superior) estimation approach. The second one is from Miyamoto and Nguyen (2015) who estimate the same model using, in addition to the variables in SGU, also forecasts of one to four quarters ahead output growth rates. As can be seen in the figures, overall the results imply even smaller information gains with respect to news shocks due to v^f and r.

3.2 Avdjiev (2016) model

The second model I consider is taken from Avdjiev (2016). It is also a real business cycle model sharing many of the features of the SGU model. A brief summary of these features is provided below.

The representative agent maximizes the following utility function:

$$\mathrm{E}_0 \sum_{t=0}^{\infty} \beta^t \frac{\left[(C_t - \theta_c C_{t-1})(l_t - \theta_l l_{t-1})^\chi\right]^{1-\gamma} - 1}{1 - \gamma}, \tag{3.10}$$

where C_t is consumption, l_t is leisure, β is the discount factor, γ is the inverse of the intertemporal elasticity of substitution, χ determines the Frisch elasticity of labor supply, θ_c and θ_l are parameters determining the degrees of habit persistence in consumption and leisure, respectively. Output is produced using:

$$Y_t = Z_t(u_t K_t)^\alpha (X_t h_t)^{1-\alpha}, \tag{3.11}$$

where K_t is the existing capital stock, $h_t = 1 - l_t$ is hours worked, u_t is the rate of capacity utilization, Z_t is a stationary neutral productivity shock, and X_t is a non-stationary neutral productivity shock.

The law of motion for the stock of capital is:

$$K_{t+1} = (1 - \delta(u_t))K_t + \Omega_t \left[I_t - \frac{1}{2\delta_0 \eta} \left(\frac{I_t}{K_t} - \tau \right)^2 K_t \right], \tag{3.12}$$

where I_t is investment, δ is the rate of depreciation and is an increasing function of the rate of capacity utilization, Ω_t is a stationary investment-specific productivity shock, τ is the steady-state level of the investment-capital ratio, η is the elasticity of the investment-capital ratio with respect to Tobin's q, and δ_0 is the steady-state capital depreciation rate.

There is no government in this economy and output is used for either consumption or investment:

$$Y_t = C_t + I_t A_t, \tag{3.13}$$

where A_t is a non-stationary investment specific productivity shock.

The main departure from the SGU model is in the way news shocks are introduced into the model. In particular, the specification of shock precesses in (3.6) is replaced with

$$
\begin{aligned}
\ln(x_t/x) &= \rho_x^l \ln(x_{t-1}/x) + (1 - \rho_x^l) \ln(x_{t-1}^{LR}) + \sigma_{x,u} \varepsilon_{x,t}^u \\
\ln(x_t^{LR}) &= \rho_x^{LR} \ln(x_{t-1}^{LR}) + \sigma_{x,LR} \varepsilon_{x,t}^{LR},
\end{aligned}
\tag{3.14}
$$

where ε_x^u and ε_x^{LR} are independent standard normal random variables. Avdjiev (2016) further assumes that $0 < \rho_x^l < 1$ and $\rho_x^{LR} = 0.999$, which implies that $\ln(x_t^{LR})$ can be interpreted as the long-run component of $\ln(x_t/x)$.[16] Therefore, ε_x^{LR} is the anticipated

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[16]Note that if $\rho_x^{LR} = 1$ then $\lim_{s \to \infty} \mathrm{E}_t \ln(x_{t+s}/x) = \ln(x^{LR})$.

Table 4: Information content of asset prices: innovations

	innovation	IG($\bar{y}$)	IG($v^f, r \mid \bar{y}$)	IG($v^f \mid \bar{y}$)	IG($r \mid \bar{y}$)	IG(v^f)	IG(r)
ε_x^u	non-stat. neutral prod.	92.4	5.4	0.1	5.4	3.3	0.3
ε_x^{LR}	non-stat. neutral prod. LR news	0.2	0.2	0.1	0.1	0.1	0.0
ε_a^u	non-stat. investment-specific prod.	99.5	0.4	0.3	0.0	1.7	0.8
ε_a^{LR}	non-stat. investment-specific prod. LR news	42.8	44.7	36.9	3.6	60.5	1.8
ε_z^u	stat. neutral prod.	94.8	4.0	0.4	3.8	1.8	52.7
ε_z^{LR}	stat. neutral prod. LR news	37.2	48.0	9.5	43.0	12.4	31.8
ε_ω^u	stat. investment-specific prod.	57.8	35.4	35.3	1.1	7.5	3.7
ε_ω^{LR}	stat. investment-specific prod. LR news	0.0	0.0	0.0	0.0	0.0	0.0

Note: see the note to Table 1. $\bar{y}$ includes the growth rates of output, consumption, and investment, hours worked, and the relative price of investment.

change in the long-run value of the shock. The model contains only four of the seven fundamental shocks present in the SGU model, namely: stationary and non-stationary neutral productivity shocks and stationary and non-stationary investment-specific productivity shocks. All shocks evolve as in (3.14), implying that there are four different long-run components and eight exogenous innovations, four of which are interpreted as long run (LR) news shocks.

Avdjiev (2016) argues that the long-run specification of news shocks fits the data better than the specification in (3.6). Importantly, Avdjiev (2016) uses asset price data to estimate the model. The two asset price variables used are the growth rate of the total stock market valuation and the real risk-free rate. These variables are assumed to be noisy measures of v^f and r, which are defined as in section 3.1. In addition, five macroeconomic variables are used in the estimation: the growth rates of output (y_t), consumption (c_t), and investment (i_t), hours worked (h_t), and the relative price of investment (a_t).

3.2.1 Information about news shocks

I proceed along the lines of the analysis carried out in section Section 3.1.1. Note that now $\boldsymbol{y}$ is a $T \times 7$ dimensional vector, and $\bar{\boldsymbol{y}} = \boldsymbol{y} \backslash (v^f, r)$ is a $T \times 5$ dimensional vector. I set $T = 236$, which is the sample size in Avdjiev (2016), and assume that $\boldsymbol{\theta}$ is equal to the median of the posterior distribution reported in Avdjiev (2016) (see Table 11 in the Appendix).

The results are presented in Table 4. Including asset prices among the observables

leads to significant information gains with respect to two of the news shocks – the anticipated innovations in the non-stationary investment-specific productivity shock ε_a^{LR}, and the stationary neutral productivity shock ε_z^{LR}. Almost all of the gains in the first case are due to including v^f, while in the second most of the information is contributed by r. However, neither one of the innovations can be fully recovered from $\boldsymbol{y}$. The total information gains are around 88% for ε_a^{LR} and 85% for ε_z^{LR}. The respective unconditional gains reported in the last two columns are relatively large, implying that, in contrast to the SGU model, v^f and r contribute significant amounts of non-redundant information with respect to ε_a^{LR} and ε_z^{LR}. There is essentially no information in the set of observables as a whole about the news components of the other two shocks – the non-stationary neutral productivity shock and the stationary investment-specific productivity shock. This can be understood from the observation that the standard deviations of these innovations are estimated to be very small compared to the standard deviations of the unanticipated innovations to the same shocks.[17] Furthermore, since the stationary investment-specific productivity shock is estimated to be very persistent, the coefficient on the long-run component in (3.14) is close to zero, making ε_ω^{LR} very difficult to identify.

In addition to the two news shocks components, asset prices, and in particular v^f, contribute a significant amount of information with respect to the unanticipated innovations to the stationary investment specific productivity shock ε_ω^u. The small size of the unconditional gain implies that the contribution of v^f is largely a result of the interactions of that variable with variables in $\bar{\boldsymbol{y}}$.

To find out how the contributions of v^f and r compare to other variable, Figure 3 presents conditional information gains for each one of the seven observables. The results show that v^f and r are indeed the most informative variables with respect to the two identified news shocks. In the case of ε_z^{LR}, the conditional information gain from observing hours worked is somewhat larger than the gain from including v^f, but is smaller than the information gain from observing r. The relative price of investment is the only other observable with a positive marginal contribution. None of the macro variables makes a positive contribution with respect to ε_a^{LR}. Note that, as in section 3.1, the gains from each variable are conditional on information contained in the remaining six variables. This is why the results for v^f and r are different from the values in Table 4 (columns 3 and 4). In particular, the information gains with respect to ε_a^{LR} due to either v^f or r are larger when the conditioning set includes the other asset

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[17]The posterior median estimates are: $\sigma_x^{LR} = 0.01$ vs. $\sigma_x^u = 1.05$ and $\sigma_\omega^{LR} = 0.07$ vs. $\sigma_\omega^u = 9.97$.
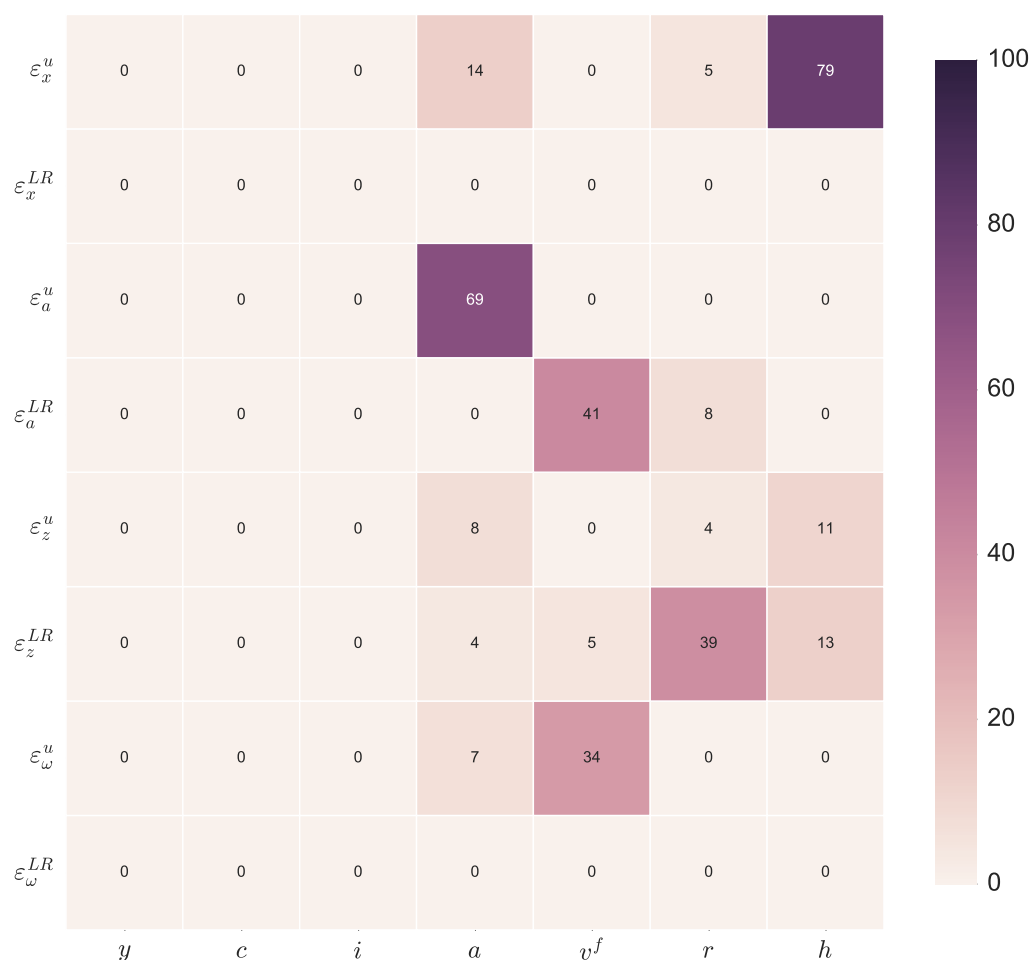
Figure 3: Conditional information gains in the model of Avdjiev (2016).

price variable compared to when it does not. This indicates a positive conditional information complementarity between v^f and r with respect to that shock. At the same time, there is a negative complementarity with respect to the news component in the stationary neutral productivity shock.[18] Additional results from conditional and unconditional information complementarity analysis are presented in Figures 13 – 16 of the Appendix. There is a significant information complementarity between v^f and a with respect to the news components in two of the shocks – negative with respect to the stationary neutral productivity shock, and positive with respect to the stationary

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[18]Another way to see this is by comparing the joint information gains to the sum of the individual gains in Table 4.

Table 5: Information content of asset prices: shocks

	shock	IG($\bar{\boldsymbol{y}}$)	IG($v^f, r|\bar{\boldsymbol{y}}$)	IG($v^f|\bar{\boldsymbol{y}}$)	IG($r|\bar{\boldsymbol{y}}$)	IG(v^f)	IG(r)
μ_x	non-stat. neutral prod.	93.3	4.9	0.1	4.9	3.3	0.4
μ_x^{LR}	non-stat. neutral prod. LR comp.	0.8	0.4	0.1	0.3	0.1	0.0
μ_a	non-stat. investment-specific prod.	100.0	0.0	0.0	0.0	5.2	3.5
μ_a^{LR}	non-stat. investment-specific prod. LR comp.	44.3	43.5	35.9	3.5	60.7	3.3
z	stat. neutral prod.	95.9	3.0	0.8	2.5	4.6	63.1
z^{LR}	stat. neutral prod. LR comp.	37.8	47.5	9.4	42.5	12.4	31.7
ω	stat. investment-specific prod.	57.7	35.3	35.3	1.1	7.5	3.7
ω^{LR}	stat. investment-specific prod. LR comp.	0.0	0.0	0.0	0.0	0.0	0.0

Note: see note to Table 1.

investment-specific productivity shock. There is also a positive complementarity between v^f and h with respect to the stationary neutral productivity shock. In the case of r, the only significant complementarity is with a – positive with respect to the news component in the non-stationary neutral productivity shock.

Another interesting result in Figure 3 is the apparent lack of information in y, i and c. In fact, the conditional information gains are positive but very small, suggesting near redundancy of these variables. This is easily explained by the observation that the economy's resource constraint (see equation (3.13)) implies linear dependence among y, i and c.[19] Stochastic singularity is avoided by assuming measurement errors in all variables. However, the size of the errors in y, i and c is very small, implying that any one of them is (nearly) redundant given the other two.

Table 5 reports results on the information content of asset prices with respect to the four structural shocks and their long-run components. The information gains are very similar to the ones with respect to the innovations, presented in Table 4, both in terms of the size of the gains and the contribution of each asset prices variable. This is to be expected given that shocks and innovations are closely linked to each other in this model.

3.2.2   Information about parameters

Table 6 reports parameter efficiency gains due to observing the two asset price variables. The gains with respect to the standard deviations of the four news shocks are between 25% and 86%. Similar to the information gains results in Table 4, v^f is relatively more informative for the parameters of the two investment-specific productivity shocks,

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[19]As in the SGU model, the observed investment series is defined as $i_t := \triangle \ln A_t I_t$.

Table 6: Efficiency gains (%)

	parameter	v^f, r	v^f	r
γ	inverse intertemporal elasticity of substitution	18	1	16
χ	Frisch elasticity of labor supply	99	44	98
θ_l	habit in leisure,	40	14	37
θ_c	habit in consumption,	36	10	26
δ_2	capacity utilization cost	88	83	26
η	investment adjustment cost	88	85	21
ρ_x^l	AR non-stationary neutral productivity	85	1	85
ρ_a^l	AR non-stationary investment-specific productivity	19	13	10
ρ_z^l	AR stationary neutral productivity	90	17	88
ρ_ω^l	AR stationary investment-specific productivity	52	47	15
$\sigma_{x,u}$	std. non-stationary neutral productivity	33	5	31
$\sigma_{x,LR}$	std. non-stationary neutral productivity LR news	25	1	25
$\sigma_{a,u}$	std. non-stationary investment-specific productivity	5	4	1
$\sigma_{a,LR}$	std. non-stationary investment-specific productivity LR news	69	54	17
$\sigma_{z,u}$	std. stationary neutral productivity	45	13	45
$\sigma_{z,LR}$	std. stationary neutral productivity LR news	64	24	50
$\sigma_{\omega,u}$	std. stationary investment-specific productivity	90	89	18
$\sigma_{\omega,LR}$	std. stationary investment-specific productivity LR news	86	86	10

Note: see note to Table 3.

while r is more informative about the parameters of the stationary and non-stationary neutral productivity shocks. Notice that this applies to all parameters of the same shock, including the autoregressive coefficients and the standard deviations of the unanticipated shocks.

It is worth pointing out that the news shock parameters, and in particular $\sigma_{x,LR}$ and $\sigma_{\omega,LR}$, are identified, in spite of the earlier finding that there is very little information about the realizations of the news components of the non-stationary neutral productivity and stationary investment-specific productivity shocks. Lack of identification would imply an infinite value of the CRLB. As can be seen in Table 12 in the Appendix, which shows the CRLBs with and without asset prices, they are all finite. The values for $\sigma_{\omega,LR}$, however, are very large, suggesting that the likelihood surface is in fact very flat with respect to that parameter. Two other parameters with extremely large values of the CRLB are the cost of capacity utilization parameter δ_2 and the Frisch elasticity of labor supply χ. Notice that, even though the values of the CRLBs of $\sigma_{\omega,LR}$ an δ_2 are

almost equal, the levels of uncertainty they imply are very different since $\delta_2 = 3.91$ while $\sigma_{\omega,LR} = 0.07$.

To find out how v^f and r compare to other observables, Figure 4 shows the efficiency gains due to each one of the seven variables. Only with respect to one of the news shock parameters – the standard deviation of the long-run news component in the non-stationary investment specific-productivity shock ($\sigma_{a,LR}$), is v^f significantly more informative than any other variable. The relative price of investment is about as informative as v^f with resect to the standard deviation of the long-run news component in the stationary investment-specific productivity shock ($\sigma_{\omega,LR}$), and is also by far the most informative variable with respect to the standard deviation of the long-run news component in the non-stationary neutral productivity shock ($\sigma_{x,LR}$). Lastly, hours worked is the most informative variable with respect to the standard deviation of the long-run news component in the stationary neutral productivity shock ($\sigma_{z,LR}$).

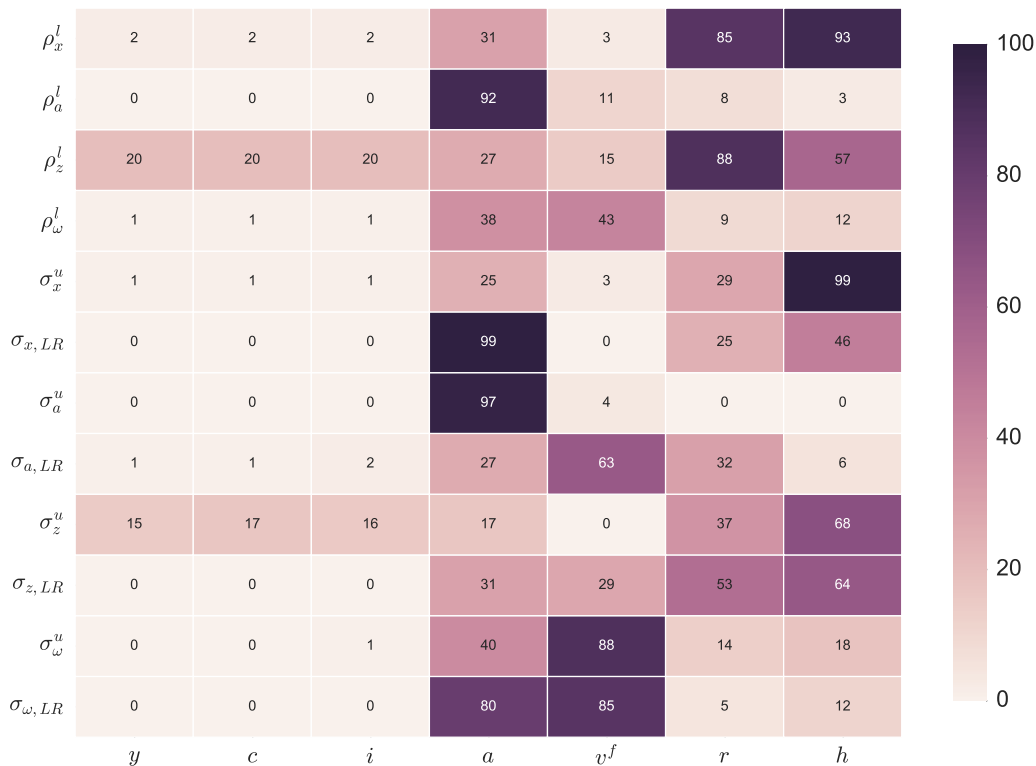|	y	c	i	a	v^f	r	h
ρ_x^l	2	2	2	31	3	85	93
ρ_a^l	0	0	0	92	11	8	3
ρ_z^l	20	20	20	27	15	88	57
ρ_ω^l	1	1	1	38	43	9	12
σ_x^u	1	1	1	25	3	29	99
$\sigma_{x,LR}$	0	0	0	99	0	25	46
σ_a^u	0	0	0	97	4	0	0
$\sigma_{a,LR}$	1	1	2	27	63	32	6
σ_z^u	15	17	16	17	0	37	68
$\sigma_{z,LR}$	0	0	0	31	29	53	64
σ_ω^u	0	0	1	40	88	14	18
$\sigma_{\omega,LR}$	0	0	0	80	85	5	12

Figure 4: Efficiency gains in the model of Avdjiev (2016).

It should be noted that the these results are obtained under the assumption that the

Table 7: Information content of asset prices: innovations

	innovation	IG($\bar{y}$)	IG($v^f,r|\bar{y}$)	IG($v^f|\bar{y}$)	IG($r|\bar{y}$)	IG(v^f)	IG(r)
ε_x^u	non-stat. neutral prod.	92.6	5.4	0.2	5.4	3.3	0.3
ε_x^{LR}	non-stat. neutral prod. LR news	0.3	0.1	0.0	0.1	0.1	0.0
ε_a^u	non-stat. investment-specific prod.	99.8	0.1	0.1	0.1	1.7	0.8
ε_a^{LR}	non-stat. investment-specific prod. LR news	78.8	15.0	6.4	10.0	60.5	1.8
ε_z^u	stat. neutral prod.	95.5	3.4	0.1	3.4	1.8	52.7
ε_z^{LR}	stat. neutral prod. LR news	48.0	40.1	1.8	39.7	12.4	31.8
ε_ω^u	stat. investment-specific prod.	93.8	3.6	3.6	0.1	7.5	3.7
ε_ω^{LR}	stat. investment-specific prod. LR news	0.0	0.0	0.0	0.0	0.0	0.0

Note: see the note to Table 1. $\bar{y}$ includes the growth rates of output, consumption, investment, *and TFP*, hours worked, and the relative price of investment.

standard deviations of the measurement errors are known. Without it the efficiency gains cannot be computed since the measurement error parameters are not identified unless the respective variables are observed. This does not affect the conclusions regarding the contributions of asset prices, but does inflate the efficiency gains with respect to ρ_z^l and $\sigma_{z,u}$ due to y, c, and i.[20]

The role of TFP. The results in this section suggest a much greater and more distinct role of asset prices with respect to news shocks in the model of Avdjiev (2016) compared to the SGU model. In particular, v^f and r are found to be considerably more informative than any other observed variable with respect to two of the news shocks – the long-run news components of the non-stationary investment-specific productivity shock (ε_a^{LR}) and the stationary neutral productivity shock (ε_z^{LR}). One possible explanation of this finding is that TFP growth is assumed to be observed in the analysis of the SGU model but not for the model in this section. Since that variable was found to be quite informative with respect to several anticipated innovations in the SGU model, it is possible that the contribution of v^f and r in the model of Avdjiev (2016) is exaggerated by its exclusion. To examine this possibility, Table 7 reevaluates the information content of asset prices assuming that $\bar{y}$ contains tfp in addition to the other five macro variables. The only major change compared to Table 4 is with respect to the long-run news component in the non-stationary investment-specific productivity shock (ε_a^{LR}) and the unanticipated innovation to the stationary investment-specific productivity shock (ε_ω^u). In both cases

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[20]There are also relatively large and approximately equal efficiency gains with respect to the inverse intertemporal elasticity of substitution γ and the habit in consumption θ_c due to y, c, and i.

the conditional contribution of information by asset prices is much smaller when $\bar{\boldsymbol{y}}$ includes tfp. Furthermore, the reduction is almost entirely due to the much smaller contribution of v^f. In the case of ε_a^{LR} the conditional information gain of v^f decreases from 37% to 15%, while at the same time the information gain of r increases from 3.6% to 10%. This implies that there is a negative conditional complementarity between v^f and tfp, and a positive conditional complementarity between r and tfp with respect to ε_a^{LR}. The same type of complementarity between asset prices and tfp is found with respect to the stationary neutral productivity shock (ε_z^{LR}). However, since the relative contribution of v^f is much smaller, the overall information gain of asset prices with respect to that shock remains large.

Figure 5 presents the conditional information gains of all eight variables. r is slightly more informative than tfp, h, v^f and a with respect to ε_a^{LR}; it is, however, by far the most informative variable with respect to ε_a^{LR}. Comparing the results against those presented in Figure 3 shows that the inclusion of tfp has also a significant impact on the contribution of information by h and a. For instance, the conditional gain of h with respect to the non-stationary neutral productivity shock (ε_x^u) declines from 80% when tfp is excluded from $\bar{\boldsymbol{y}}$ to 1% when it is included. This means that, conditional on the other observables, h and tfp are close substitutes in terms of information they contribute about ε_x^u. Similarly, there is a strong negative complementarity between tfp and a with respect to the non-stationary investment-specific productivity shock (ε_a^u).

The consequences, in terms of efficiency gains, of adding tfp as an observable are very similar: the contribution of v^f is much smaller than before with respect to most parameters including $\sigma_{a,LR}$, for which it is the most informative variable when tfp is unobserved. The relative importance of r, on the other hand, generally increases, and it becomes the variable with the largest contribution with respect to $\sigma_{z,LR}$. A complete set of results can be seen in Figure 17 of the Appendix.

To summarize, when tfp is among the observed variables, of the two asset prices only r contributes significantly more information about one of the news shocks than any other observable. As in in section 3.1, that shock is the stationary neutral productivity news shock. Due to the relatively smaller number of shocks in the Avdjiev (2016) model, however, the information gained from observing r is substantially larger than in the SGU model.
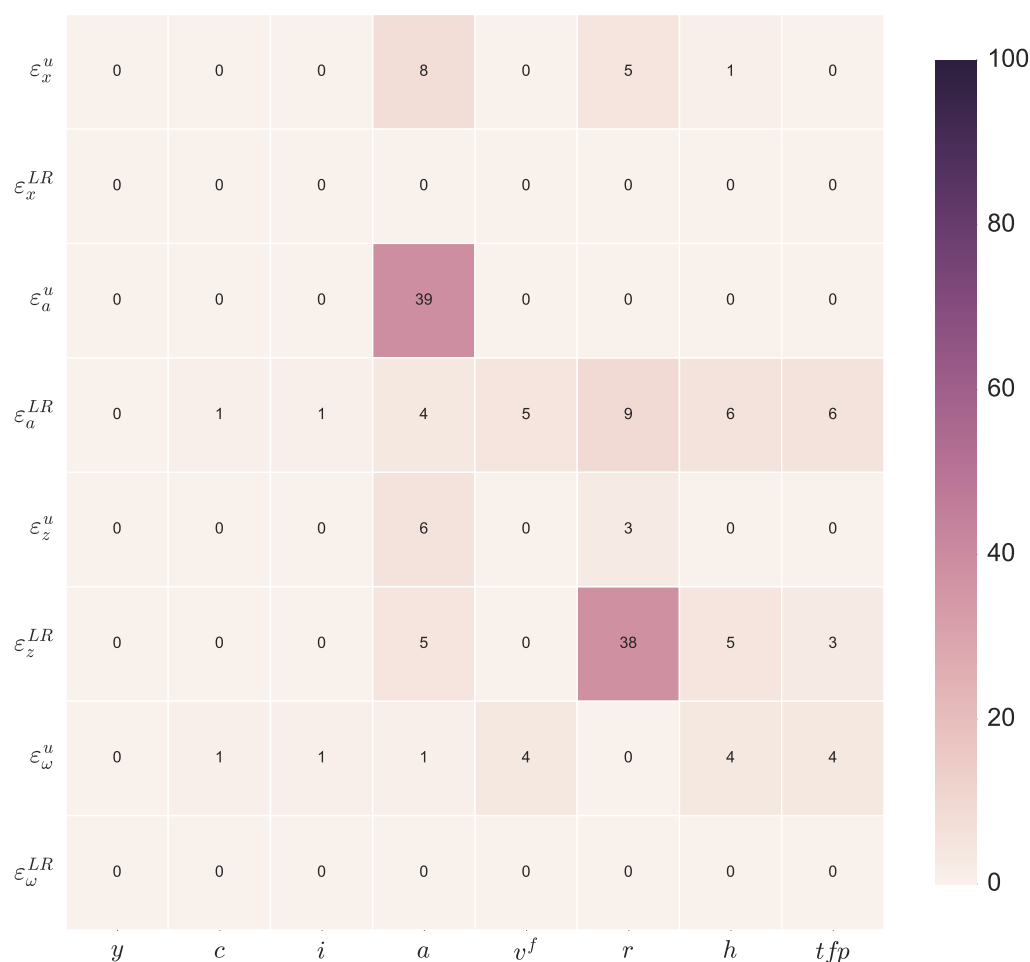
Figure 5: Conditional information gains in the model of Avdjiev (2016) when tfp is observed.

4 Conclusion

The informational importance of observed variables with respect to shocks in business cycle models is often asserted without formal justification. This paper has proposed a general framework for evaluating the contribution of information that different variables make with respect to specific shocks. An application to two examples of DSGE models containing news shocks revealed relatively modest contribution of information by asset prices. A necessary caveat to these results is that they are entirely conditional on the particular models considered. Making changes in the way shocks are introduced and

propagate, or in the way asset prices are modeled is likely to have an impact on the conclusions regarding the informational value of different observables. Indeed, this is an example of one of the intended purposes of the analysis developed in this paper, namely, checking whether models are consistent with our intuition about how the real world works. Finding out that they are not provides useful directions for their improvement.

The analysis in this paper can be extended in several directions. With regards to news-driven DSGE models, it would be interesting to know whether observing expectations provides significantly more information than observing asset prices. In terms of the methodology itself, more research is needed on how to perform this type of analysis in non-linear and non-Gaussian models. In particular, the information gains measures are, in general, not available in closed form, and would have to be estimated using simulated data.

A   Appendix

A.1   Schmitt-Grohé and Uribe (2012) model

Table 8: Parameter values, SGU (2012) model

	parameter	MLE	posterior median
θ	Frisch elasticity of labor supply	5.39	4.74
γ	wealth elasticity of labor supply	0.00	0.00
κ	investment adjustment cost	25.07	9.11
δ_2/δ_1	capacity utilization cost	0.44	0.34
b	habit in consumption	0.94	0.91
ρ_{xg}	government spending	0.74	0.72
ρ_z	AR stationary neutral productivity	0.96	0.92
ρ_{μ^a}	AR non-stationary investment-specific productivity	0.48	0.48
ρ_g	AR government spending	0.96	0.96
ρ_{μ^x}	AR non-stationary neutral productivity	0.27	0.38
ρ_μ	AR wage markup	0.98	0.98
ρ_ζ	AR preference	0.10	0.17
ρ_{z^I}	AR stationary investment-specific productivity	0.21	0.47
σ_z^0	std. stationary neutral productivity 0	0.62	0.65
σ_z^4	std. stationary neutral productivity 4	0.11	0.11
σ_z^8	std. stationary neutral productivity 8	0.11	0.09
$\sigma_{\mu^a}^0$	std. non-stationary investment-specific productivity 0	0.16	0.21
$\sigma_{\mu^a}^4$	std. non-stationary investment-specific productivity 4	0.20	0.16
$\sigma_{\mu^a}^8$	std. non-stationary investment-specific productivity 8	0.19	0.16
σ_g^0	std. government spending 0	0.53	0.62
σ_g^4	std. government spending 4	0.69	0.57
σ_g^8	std. government spending 8	0.43	0.37
$\sigma_{\mu^x}^0$	std. non-stationary neutral productivity 0	0.45	0.38
$\sigma_{\mu^x}^4$	std. non-stationary neutral productivity 4	0.12	0.08
$\sigma_{\mu^x}^8$	std. non-stationary neutral productivity 8	0.12	0.10
σ_μ^0	std. wage markup 0	1.51	0.50
σ_μ^4	std. wage markup 4	3.93	4.79
σ_μ^8	std. wage markup 8	3.20	0.51
σ_ζ^0	std. preference 0	2.83	4.03
σ_ζ^4	std. preference 4	2.76	1.89
σ_ζ^8	std. preference 8	5.34	2.21
$\sigma_{z^I}^0$	std. stationary investment-specific productivity 0	34.81	11.72
$\sigma_{z^I}^4$	std. stationary investment-specific productivity 4	11.99	1.93
$\sigma_{z^I}^8$	std. stationary investment-specific productivity 8	14.91	5.50

Note: The values are taken from Table II of Schmitt-Grohé and Uribe (2012)

Table 9: CRLBs

	parameter	$\bar{y}$	y
θ	Frisch elasticity of labor supply	1.65135	0.27551
γ	wealth elasticity of labor supply	0.00002	0.00001
κ	investment adjustment cost	30.63677	1.50300
δ_2/δ_1	capacity utilization cost	0.03112	0.00040
b	habit in consumption	0.00018	0.00004
ρ_{xg}	government spending	0.04158	0.02751
ρ_z	AR stationary neutral productivity	0.00178	0.00026
ρ_{μ^a}	AR non-stationary investment-specific productivity	0.00371	0.00222
ρ_g	AR government spending	0.00116	0.00055
ρ_{μ^x}	AR non-stationary neutral productivity	0.15107	0.02009
ρ_μ	AR wage markup	0.00045	0.00011
ρ_ζ	AR preference	0.00685	0.00491
ρ_{z^I}	AR stationary investment-specific productivity	0.02235	0.00100
σ_z^0	std. stationary neutral productivity 0	0.03879	0.00488
σ_z^4	std. stationary neutral productivity 4	2.09192	0.15462
σ_z^8	std. stationary neutral productivity 8	1.51431	0.14918
$\sigma_{\mu^a}^0$	std. non-stationary investment-specific productivity 0	0.03482	0.00177
$\sigma_{\mu^a}^4$	std. non-stationary investment-specific productivity 4	0.04562	0.00156
$\sigma_{\mu^a}^8$	std. non-stationary investment-specific productivity 8	0.04740	0.00167
σ_g^0	std. government spending 0	0.61389	0.02131
σ_g^4	std. government spending 4	1.25121	0.11185
σ_g^8	std. government spending 8	3.22258	0.27854
$\sigma_{\mu^x}^0$	std. non-stationary neutral productivity 0	0.09638	0.02098
$\sigma_{\mu^x}^4$	std. non-stationary neutral productivity 4	1.43272	0.08717
$\sigma_{\mu^x}^8$	std. non-stationary neutral productivity 8	0.75869	0.07645
σ_μ^0	std. wage markup 0	6.52819	0.07706
σ_μ^4	std. wage markup 4	4.78828	0.46297
σ_μ^8	std. wage markup 8	6.02596	0.59652
σ_ζ^0	std. preference 0	59.14528	0.98231
σ_ζ^4	std. preference 4	99.49705	9.82559
σ_ζ^8	std. preference 8	33.00313	3.02169
$\sigma_{z^I}^0$	std. stationary investment-specific productivity 0	70.24558	5.52009
$\sigma_{z^I}^4$	std. stationary investment-specific productivity 4	104.96769	4.48185
$\sigma_{z^I}^8$	std. stationary investment-specific productivity 8	44.03072	3.50932

Note: $\boldsymbol{y}$ includes all observables, $\bar{\boldsymbol{y}} = \boldsymbol{y} \setminus (v^f, r)$. The bounds are computed for the MLE values in Table 8 with $T = 207$.

Table 10: Information content of asset prices: different estimates of SGU model

	innovation	A. SGU median		B. HS(2014)		C. MN(2015)	
		$IG(\bar{\boldsymbol{y}})$	$IG(v^f,r\vert\bar{\boldsymbol{y}})$	$IG(\bar{\boldsymbol{y}})$	$IG(v^f,r\vert\bar{\boldsymbol{y}})$	$IG(\bar{\boldsymbol{y}})$	$IG(v^f,r\vert\bar{\boldsymbol{y}})$
$\varepsilon_{\mu^a}^0$	non-stationary investment-specific prod.	47.6	8.8	46.5	1.8	92.7	0.0
$\varepsilon_{\mu^a}^4$	non-stationary investment-specific prod. 4q	25.8	10.7	26.6	2.0	3.1	0.1
$\varepsilon_{\mu^a}^8$	non-stationary investment-specific prod. 8q	26.0	9.1	26.1	1.9	4.1	0.1
$\varepsilon_{\mu^x}^0$	non-stationary neutral prod.	24.6	39.9	41.2	45.9	47.4	43.6
$\varepsilon_{\mu^x}^4$	non-stationary neutral prod. 4q	1.3	8.2	3.1	9.9	3.3	4.7
$\varepsilon_{\mu^x}^8$	non-stationary neutral prod. 8q	1.9	11.1	5.5	13.2	7.9	7.0
$\varepsilon_{z^I}^0$	stationary investment-specific prod.	89.1	5.7	81.4	10.4	73.3	12.9
$\varepsilon_{z^I}^4$	stationary investment-specific prod. 4q	1.7	3.8	4.0	4.8	16.2	9.0
$\varepsilon_{z^I}^8$	stationary investment-specific prod. 8q	14.6	30.1	12.8	15.7	4.8	3.0
ε_z^0	stationary neutral prod.	80.2	9.0	81.5	10.9	33.3	29.4
ε_z^4	stationary neutral prod. 4q	2.5	17.6	3.5	14.5	10.4	3.5
ε_z^8	stationary neutral prod. 8q	1.8	12.9	2.9	12.2	43.0	14.6
ε_μ^0	wage markup	1.4	7.2	5.6	21.1	52.1	20.1
ε_μ^4	wage markup 4q	96.4	1.2	84.5	3.0	1.0	0.5
ε_μ^8	wage markup 8q	1.1	0.3	8.5	2.1	47.7	21.9
ε_g^0	government spending	43.5	3.2	42.7	2.4	93.9	2.7
ε_g^4	government spending 4q	37.1	3.5	33.5	2.3	0.5	0.1
ε_g^8	government spending 8q	15.2	1.6	18.3	1.2	0.6	0.1
ε_ζ^0	preference	61.2	7.2	42.2	9.9	79.5	19.5
ε_ζ^4	preference 4q	13.9	3.4	17.6	3.4	0.2	0.1
ε_ζ^8	preference 8q	18.8	4.5	20.7	3.9	0.2	0.0

Note: See the note to Table 1. The information gains are evaluated at three point estimated of the SGU model: (1) the posterior median in SGU, (2) the posterior mean in Herbst and Schorfheide (2014), and (3) the posterior median in Miyamoto and Nguyen (2015).

	y	c	i	h	g	a	tfp
$\varepsilon_{\mu^a}^{0}$	0	1.8	0.81	13	1.4	-0.13	29
$\varepsilon_{\mu^a}^{4}$	0	1.7	0.64	14	1.2	-0.1	41
$\varepsilon_{\mu^a}^{8}$	0	1.9	0.74	14	1.4	-0.07	33
$\varepsilon_{\mu^x}^{0}$	0	3.2	1.5	7.2	1.1	0.58	0.09
$\varepsilon_{\mu^x}^{4}$	0	1.3	0.63	3.9	1.1	0.1	1.1
$\varepsilon_{\mu^x}^{8}$	0	1	0.6	3	1.2	0.14	0.63
$\varepsilon_{z^I}^{0}$	0	1.3	-0.16	3.2	1.3	-0.05	0.35
$\varepsilon_{z^I}^{4}$	0	1.5	0.07	6.6	1.1	0.09	5.8
$\varepsilon_{z^I}^{8}$	0	1.2	0.08	4.5	1.1	0.16	4.2
ε_{z}^{0}	0	3.4	1.4	4.9	0.65	0.7	-0.45
ε_{z}^{4}	0	1.3	0.72	3.3	0.94	0.1	0.27
ε_{z}^{8}	0	1.2	0.82	3.1	1.1	0.2	0.2
ε_{μ}^{0}	0	0.03	0.05	-0.44	0.1	0.04	-0.21
ε_{μ}^{4}	0	-0.22	-0.13	-0.46	-0.12	0.01	-0.44
ε_{μ}^{8}	0	-0.06	0.04	-0.44	0.1	0.09	-0.39
ε_{g}^{0}	0	1.1	0.51	2.6	-0.38	0.02	0.43
ε_{g}^{4}	0	0.88	0.39	1.5	-0.31	0.02	0.56
ε_{g}^{8}	0	1	0.48	1.6	-0.3	0.11	0.74
ε_{ζ}^{0}	0	-0.39	0.29	-0.1	0.31	0.04	-0.16
ε_{ζ}^{4}	0	-0.35	0.24	-0.18	0.24	0	-0.26
ε_{ζ}^{8}	0	-0.37	0.18	-0.35	0.06	-0.02	-0.41

Figure 6: Conditional pairwise complementarity between v^f and macro variables at MLE in Schmitt-Grohé and Uribe (2012)

	y	c	i	h	g	a	tfp
$\varepsilon_{\mu^a}^0$	0	0.55	0.28	0.79	0.41	-0.01	1.1
$\varepsilon_{\mu^a}^4$	0	0.93	0.49	3.2	0.42	-0.02	3.2
$\varepsilon_{\mu^a}^8$	0	0.78	0.41	2.2	0.42	-0.01	2.4
$\varepsilon_{\mu^x}^0$	0	0.3	0.13	1.6	0.27	0	-0.05
$\varepsilon_{\mu^x}^4$	0	0.38	0.19	2.5	0.28	0.02	0.13
$\varepsilon_{\mu^x}^8$	0	0.33	0.17	2	0.26	0.01	0.12
$\varepsilon_{z^I}^0$	0	0.69	-0.02	2.2	0.43	-0.04	0.5
$\varepsilon_{z^I}^4$	0	0.66	-0.03	2.9	0.3	0.03	1.4
$\varepsilon_{z^I}^8$	0	0.53	-0.07	1.9	0.29	0.04	1.1
ε_z^0	0	0.37	0.18	1.1	0.15	0	-0.3
ε_z^4	0	0.45	0.2	3.3	0.35	0.02	0.18
ε_z^8	0	0.43	0.19	2.9	0.34	0.02	0.17
ε_μ^0	0	0.8	0.33	2.1	0.49	0.02	3.1
ε_μ^4	0	-0.3	-0.24	-0.46	-0.22	-0.01	-0.43
ε_μ^8	0	-0.29	-0.23	-0.46	-0.21	-0.01	-0.42
ε_g^0	0	0.42	0.19	3	0.05	0.01	0.77
ε_g^4	0	0.28	0.17	1.3	-0.25	0.06	0.94
ε_g^8	0	0.17	0.12	0.8	-0.25	0.06	0.64
ε_ζ^0	0	0.3	0.15	1.5	0.35	0.02	0.88
ε_ζ^4	0	-0.29	-0.11	-0.26	0.04	0	-0.26
ε_ζ^8	0	-0.29	-0.1	-0.27	0.02	0	-0.28

Figure 7: Conditional pairwise complementarity between r and macro variables at MLE in Schmitt-Grohé and Uribe (2012)

	y	c	i	h	g	a	tfp
$\varepsilon^0_{\mu^a}$	0.1	0.1	0.2	0	-0.1	0	1.7
$\varepsilon^4_{\mu^a}$	0.1	0.2	0.1	0	0	0	1.6
$\varepsilon^8_{\mu^a}$	0.1	0.2	0.1	0	0	0	1.6
$\varepsilon^0_{\mu^x}$	-0.1	-0.1	-0.1	0	-0.1	0	-0.4
$\varepsilon^4_{\mu^x}$	-0.1	0	0	0	-0.1	0	-0.1
$\varepsilon^8_{\mu^x}$	0	0.1	0	0	-0.1	0	-0.1
$\varepsilon^0_{z^I}$	0.1	0.1	0	0.1	0.1	0	1.3
$\varepsilon^4_{z^I}$	0.3	0.5	0.1	0	0	0	1.7
$\varepsilon^8_{z^I}$	0.5	0.6	0.2	0.1	0	0	1.6
ε^0_z	-0.1	0	-0.1	0	0	0	-0.4
ε^4_z	0	0	0	0	0	0	-0.2
ε^8_z	0	0.1	0	0	0	0	-0.2
ε^0_μ	-0.1	-0.1	-0.1	0	0	0	1.7
ε^4_μ	0	-0.1	0	0	0	0	1.7
ε^8_μ	0	0	0	0	0	0	1.7
ε^0_g	0	-0.1	-0.1	0	0	0	1.7
ε^4_g	0	0	0	0	0	0	1.6
ε^8_g	0	0.1	0	0	0	0	1.7
ε^0_ζ	0	0.1	-0.1	0	0	0	1.7
ε^4_ζ	0	0	0	0	0	0	1.7
ε^8_ζ	0	0	0	0	0	0	1.7

Figure 8: Unconditional pairwise complementarity between v^f and macro variables at MLE in Schmitt-Grohé and Uribe (2012)
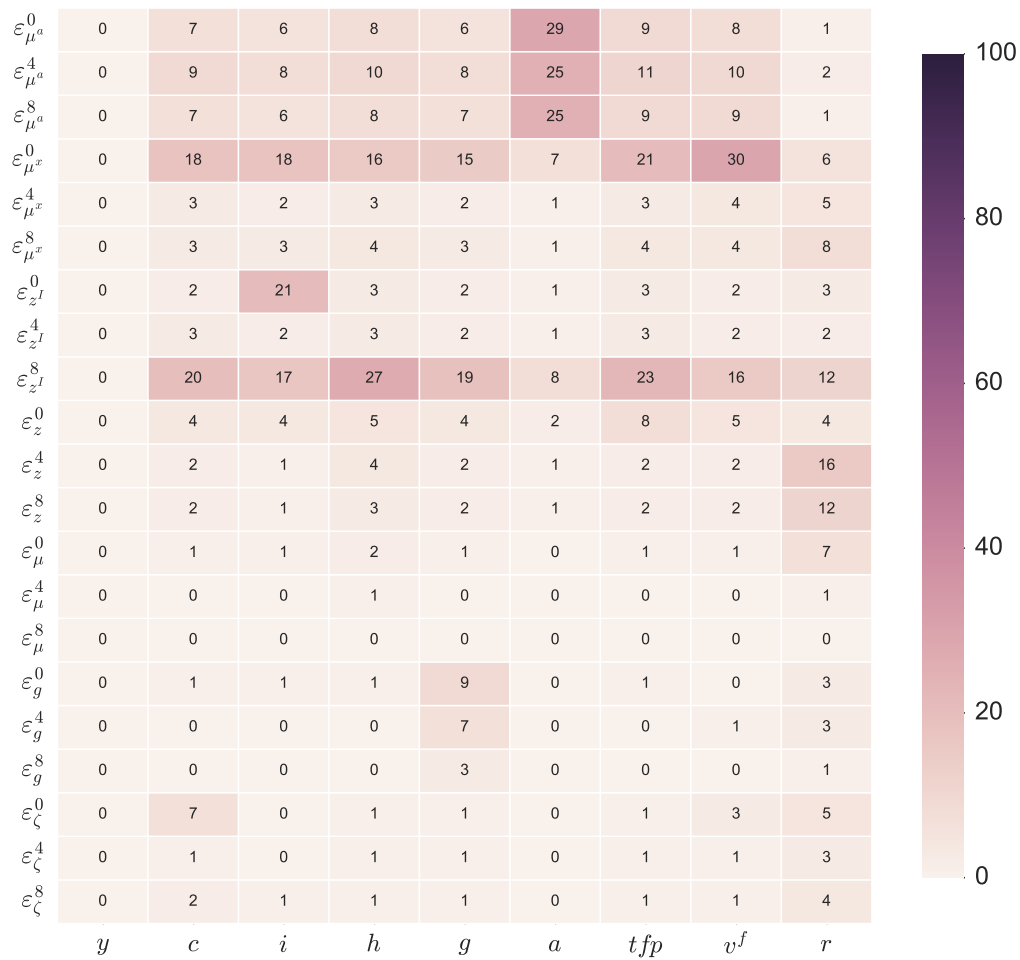
	y	c	i	h	g	a	tfp
$\varepsilon_{\mu^a}^{0}$	-0.05	0.06	-0.01	0.26	-0.15	0	0.74
$\varepsilon_{\mu^a}^{4}$	-0.1	0.04	-0.02	0.67	-0.06	0	0.23
$\varepsilon_{\mu^a}^{8}$	-0.1	0.06	-0.02	0.62	-0.05	0	0.22
$\varepsilon_{\mu^x}^{0}$	-0.12	-0.08	-0.09	0.25	-0.09	0.01	-0.03
$\varepsilon_{\mu^x}^{4}$	0.06	0.05	0.04	0.72	0.01	0	-0.03
$\varepsilon_{\mu^x}^{8}$	0.08	0.07	0.05	0.71	0.01	0	0
$\varepsilon_{z^I}^{0}$	0.06	0.28	0	0.42	0.04	0	0.43
$\varepsilon_{z^I}^{4}$	-0.1	0.15	-0.06	0.51	0.03	0	0.22
$\varepsilon_{z^I}^{8}$	-0.1	0.23	-0.07	0.44	0.03	0	0.36
ε_{z}^{0}	-0.13	-0.07	-0.09	0.29	0.09	0.01	-0.09
ε_{z}^{4}	0.05	0.03	0.03	0.8	0.02	0	-0.07
ε_{z}^{8}	0.06	0.04	0.03	0.79	0.02	0	-0.06
ε_{μ}^{0}	-0.18	-0.13	-0.1	0.17	0.05	0.01	0.62
ε_{μ}^{4}	0.04	0.01	0.01	-0.29	0.02	0	0.05
ε_{μ}^{8}	0.06	0.03	0.03	-0.28	0.02	0	0.06
ε_{g}^{0}	0.02	-0.12	-0.09	0.35	0.02	0.01	0.6
ε_{g}^{4}	-0.1	0.03	0.03	0.86	-0.03	0	0.06
ε_{g}^{8}	-0.11	0.05	0.03	0.85	-0.03	0	0.06
ε_{ζ}^{0}	0.02	0.03	-0.06	0.28	0.05	0.01	0.6
ε_{ζ}^{4}	-0.1	-0.04	0.04	0.82	0.02	0	0.07
ε_{ζ}^{8}	-0.1	-0.04	0.05	0.83	0.02	0	0.08

Figure 9: Unconditional pairwise complementarity between r and macro variables at MLE in Schmitt-Grohé and Uribe (2012)

	y	c	i	h	g	a	tfp	v^f	r
$\varepsilon_{\mu^a}^0$	0	7	6	8	6	29	9	8	1
$\varepsilon_{\mu^a}^4$	0	9	8	10	8	25	11	10	2
$\varepsilon_{\mu^a}^8$	0	7	6	8	7	25	9	9	1
$\varepsilon_{\mu^x}^0$	0	18	18	16	15	7	21	30	6
$\varepsilon_{\mu^x}^4$	0	3	2	3	2	1	3	4	5
$\varepsilon_{\mu^x}^8$	0	3	3	4	3	1	4	4	8
$\varepsilon_{z^I}^0$	0	2	21	3	2	1	3	2	3
$\varepsilon_{z^I}^4$	0	3	2	3	2	1	3	2	2
$\varepsilon_{z^I}^8$	0	20	17	27	19	8	23	16	12
ε_z^0	0	4	4	5	4	2	8	5	4
ε_z^4	0	2	1	4	2	1	2	2	16
ε_z^8	0	2	1	3	2	1	2	2	12
ε_μ^0	0	1	1	2	1	0	1	1	7
ε_μ^4	0	0	0	1	0	0	0	0	1
ε_μ^8	0	0	0	0	0	0	0	0	0
ε_g^0	0	1	1	1	9	0	1	0	3
ε_g^4	0	0	0	0	7	0	0	1	3
ε_g^8	0	0	0	0	3	0	0	0	1
ε_ζ^0	0	7	0	1	1	0	1	3	5
ε_ζ^4	0	1	0	1	1	0	1	1	3
ε_ζ^8	0	2	1	1	1	0	1	1	4

Figure 10: Conditional information gains at the posterior median in Schmitt-Grohé and Uribe (2012)
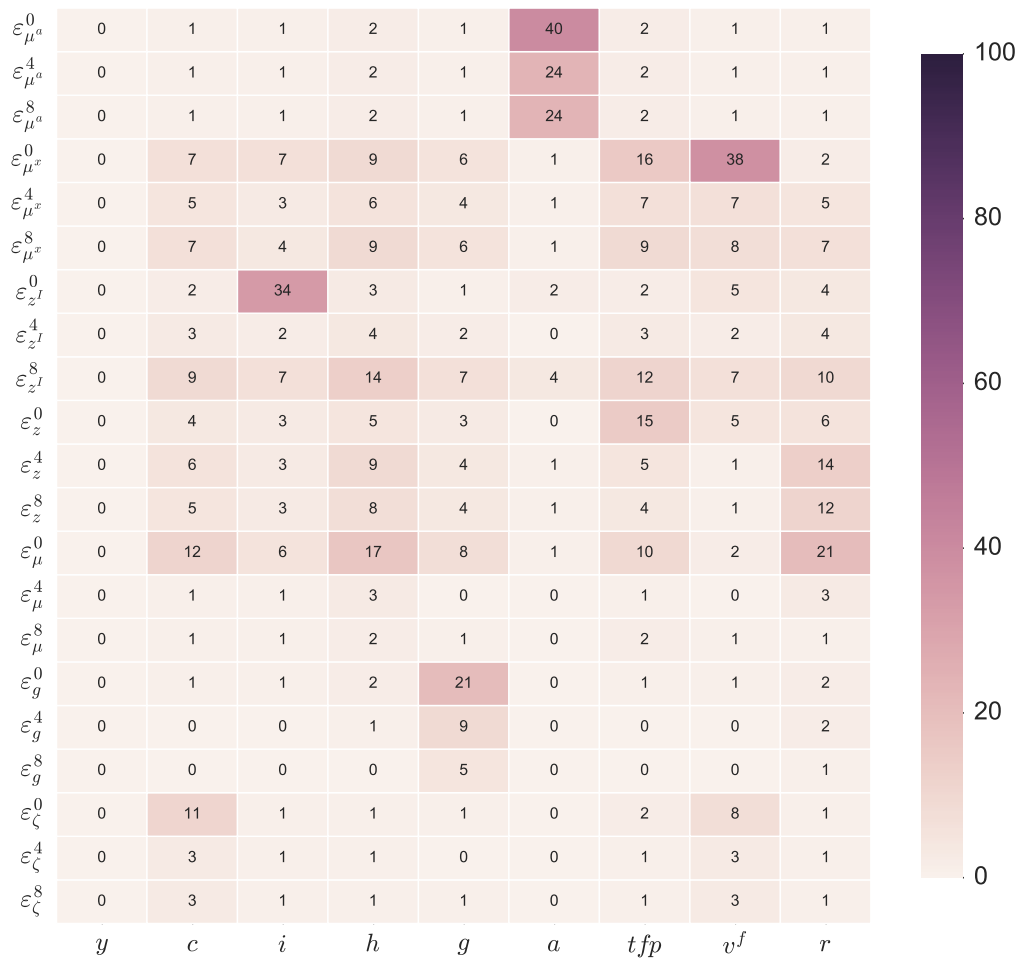
Figure 11: Conditional information gains at the posterior mean in Herbst and Schorfheide (2014)
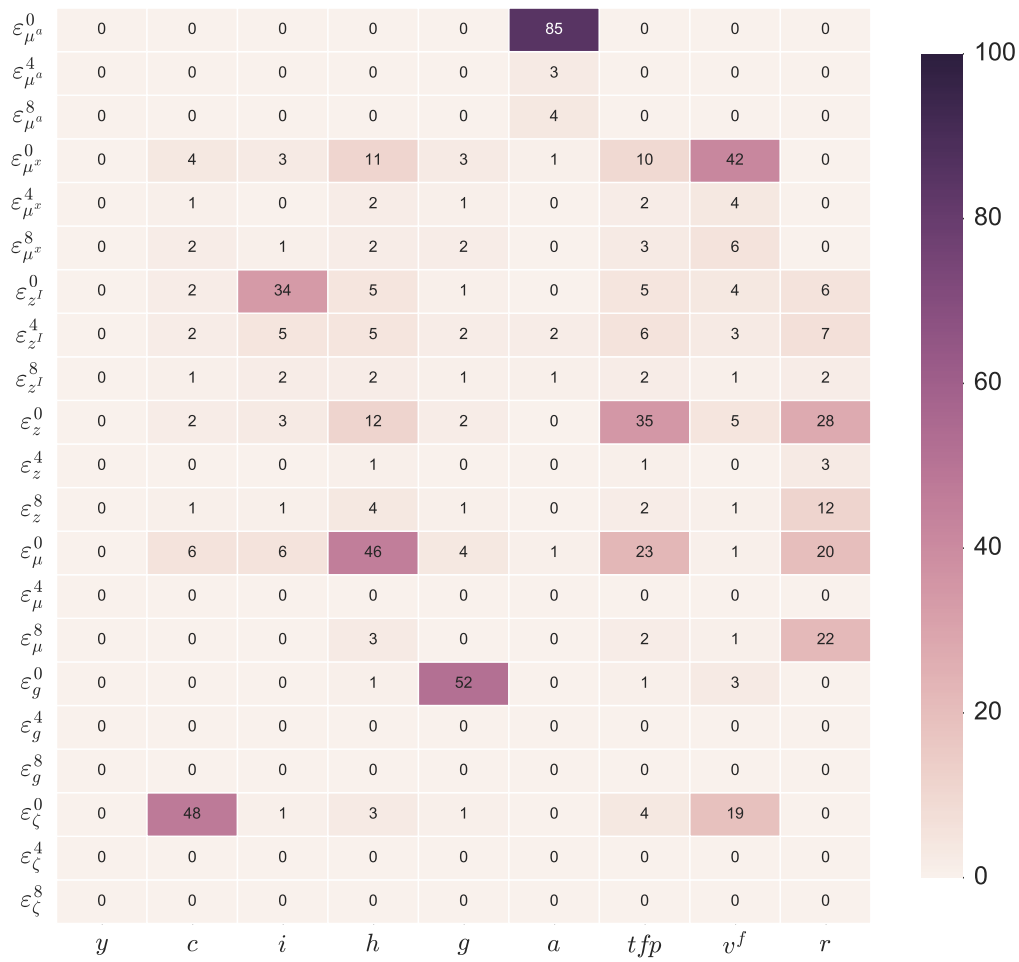
Figure 12: Conditional information gains at the posterior median in Miyamoto and Nguyen (2015)

A.2 Avdjiev (2016) model

Table 11: Parameter values, Avdjiev (2016) model

	parameter	value
γ	inverse intertemporal elasticity of substitution	0.90
χ	Frisch elasticity of labor supply	2.90
θ_l	habit in leisure,	0.12
θ_c	habit in consumption,	0.22
δ_2	capacity utilization cost	3.91
η	investment adjustment cost	0.29
ρ_x^l	AR non-stationary neutral productivity	0.01
ρ_a^l	AR non-stationary investment-specific productivity	0.32
ρ_z^l	AR stationary neutral productivity	0.57
ρ_ω^l	AR stationary investment-specific productivity	0.91
$\sigma_{x,u}$	std. non-stationary neutral productivity	1.05
$\sigma_{x,LR}$	std. non-stationary neutral productivity LR news	0.01
$\sigma_{a,u}$	std. non-stationary investment-specific productivity	0.95
$\sigma_{a,LR}$	std. non-stationary investment-specific productivity LR news	0.13
$\sigma_{z,u}$	std. stationary neutral productivity	0.93
$\sigma_{z,LR}$	std. stationary neutral productivity LR news	0.92
$\sigma_{\omega,u}$	std. stationary investment-specific productivity	9.97
$\sigma_{\omega,LR}$	std. stationary investment-specific productivity LR news	0.07

Note: The values are the posterior median estimates reported in Table D.2 of Avdjiev (2016).

Table 12: Cramér-Rao lower bounds, Avdjiev (2016) model.

	parameter	$\bar{\boldsymbol{y}}$	$\boldsymbol{y}$
γ	inverse intertemporal elasticity of substitution	0.00024	0.00020
χ	Frisch elasticity of labor supply	443.84281	6.00170
θ_l	habit in leisure,	0.00995	0.00601
θ_c	habit in consumption,	0.00006	0.00004
δ_2	capacity utilization cost	1057.97045	128.57305
η	investment adjustment cost	0.00609	0.00071
ρ_x^l	AR non-stationary neutral productivity	0.00439	0.00066
ρ_a^l	AR non-stationary investment-specific productivity	0.00461	0.00371
ρ_z^l	AR stationary neutral productivity	0.01160	0.00117
ρ_ω^l	AR stationary investment-specific productivity	0.00201	0.00097
$\sigma_{x,u}$	std. non-stationary neutral productivity	0.00548	0.00370
$\sigma_{x,LR}$	std. non-stationary neutral productivity LR news	0.00003	0.00002
$\sigma_{a,u}$	std. non-stationary investment-specific productivity	0.00206	0.00196
$\sigma_{a,LR}$	std. non-stationary investment-specific productivity LR news	0.00086	0.00027
$\sigma_{z,u}$	std. stationary neutral productivity	0.00391	0.00214
$\sigma_{z,LR}$	std. stationary neutral productivity LR news	0.02206	0.00790
$\sigma_{\omega,u}$	std. stationary investment-specific productivity	8.20461	0.79912
$\sigma_{\omega,LR}$	std. stationary investment-specific productivity LR news	965.05866	132.27654

Note: $\boldsymbol{y}$ includes all observables, $\bar{\boldsymbol{y}} = \boldsymbol{y} \setminus (v^f, r)$ The CRLBs are computed for the parameter values in Table 11 using $T = 236$.

	y	c	i	a	h
ε_x^u	0	0	-0.01	-0.03	-0.01
ε_x^{LR}	0	0	0	0.01	-0.01
ε_a^u	0	0	0	-0.03	0
ε_a^{LR}	0	0	0	-0.03	0
ε_z^u	0	0.08	0.02	-0.01	0.01
ε_z^{LR}	0	0	0	-0.15	0.13
ε_ω^u	0	0	0	0.09	-0.01
ε_ω^{LR}	0	0	0	0.16	0

Figure 13: Conditional pairwise complementarity between v^f and macro variables
Avdjiev (2016)
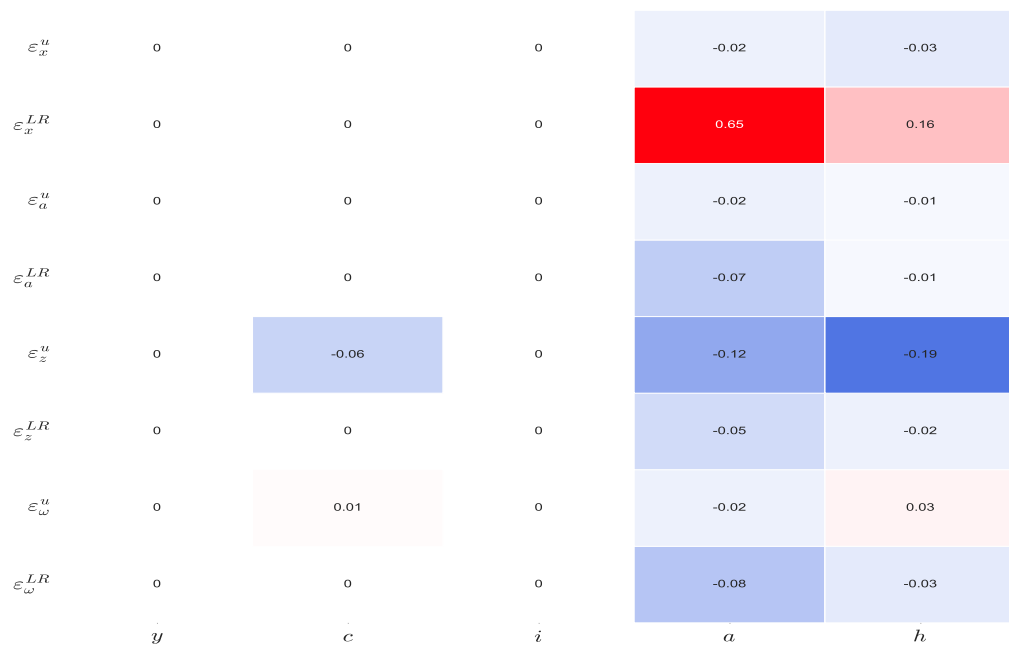
Figure 14: Conditional pairwise complementarity between r and macro variables
Avdjiev (2016)

Figure 15: Unconditional pairwise complementarity between v^f and macro variables
Avdjiev (2016)

Figure 16: Unconditional pairwise complementarity between r and macro variables Avdjiev (2016)
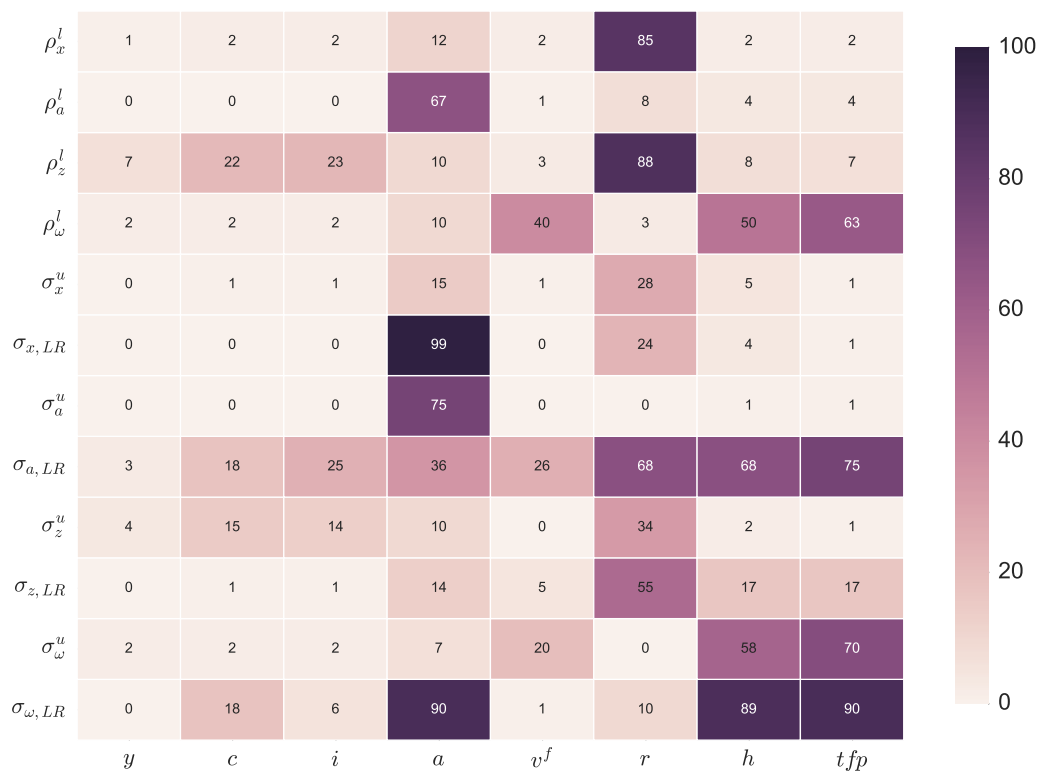
Figure 17: Efficiency gains in the model of Avdjiev (2016) when tfp is observed.

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